A Hybrid Algorithm for Multi-objective Test Case Selection

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Abstract—Testing is crucial to ensure the quality of software systems – but testing is an expensive process, so test managers try to minimise the set of tests to run to save computing resources and speed up the testing process and analysis. One problem is that there are different perspectives on what is a good test and it is usually not possible to compare these dimensions. This is a perfect example of a multi-objective optimisation problem, which is hard — especially given the scale of the search space here. In this paper, we propose a novel hybrid algorithm to address this problem. Our method is composed of three steps: a greedy algorithm to find quickly some good solutions, a genetic algorithm to increase the search space covered and a local search algorithm to refine the solutions. We demonstrate through a large scale empirical evaluation that our method is more reliable (better whatever the time budget) and more robust (better whatever the number of dimensions considered) — in the scenario with 4 objectives and a default execution time, we are 178% better in hypervolume on average than the state-of-the-art algorithms.

Index Terms—Multi-objective Optimisation, Hybrid-metahuristic, Search-based Software Engineering, Test Suite Selection,

I. INTRODUCTION

“Test early, test often”: one of the most iconic principles of modern software development methods consists in continuously testing software artefacts – in order to fix problems quickly. However, programs tend to have a large number of tests and running all of them becomes not practical (or feasible) as running and analysing tests is expensive in terms of resources (servers) and manpower [1]. Many techniques exist to address this problem, from test generation [2] to distributed testing [3], test case minimisation [4] to test case prioritisation [1]. In this paper, we address test selection [5], which can be defined as “find a minimal subset of all the tests that covers as much of the program as possible” — in order to speed up the testing process, and limit the impact on the material resources (i.e., servers) and human resources (tests results usually need to be analysed by developers/testers).

Coverage is the key here and there are multiple ways of computing it (see Section III), each of them telling something different about the program under test and there is no agreement on which one of them is the best (see Section II). Time is also a dimension of the problem, as running tests takes time: is it better to save 10 minutes or to spend these 10 minutes on stressing more the program with tests that focus on branch coverage? Do we need so many tests doing line coverage or should we save an hour of testing? Etc. This is a typical multi-objective problem: test resource managers want to make decisions based on good subsets of the tests, i.e., sets of tests that are better than any other possible set on a particular combination of objectives. Eventually, test resource managers look at the different possible sets and make a decision based on a local optimisation (e.g., favouring objective 1 which gives a bigger gain than objective 2 while the latter is usually more important etc.).

In such large search spaces, many optimisation techniques do not work well: exact solvers (e.g., MILP) only handle a single objective thus would require a scalarisation of some sort of the objectives, and do not scale well anyway. While greedy algorithms and neighbouring search algorithms are too poor (due to their guided and non-diverse search) or too slow (due to their local nature). Evolutionary algorithms (NSGA-II, MOEA/D), on the other hand, have recently proven to be better [6], [7], while hybrid algorithms, i.e., algorithms composed of various other algorithms, have not been studied extensively for this problem (with the notable exception of Yoo and Harman [6]). The main contribution of this paper is to perform a thorough study (based on similar data as the state-of-the-art [5], [7]) of the application of a three step method, that has recently proven to be good in large scale multi-objective problems [8], [9], [10], [11]. In particular, we introduce our own method, GREAP (for Greedy Evolutionary Algorithm Path-relinking), based on a greedy algorithm to find quickly some good solutions, a genetic algorithm to increase the search space covered and a local search algorithm to refine the solutions. We show that our solution is (i) more robust than the state-of-the-art to the number of objectives; (ii) is more effective (better quality and diversity); (iii) is more efficient (can work in tighter time budgets); and (iv) scales better when the size of the programs and the number of tests increase. In particular, we show that GREAP loses only 1% of quality when the time budget is reduced to 25% – while state-of-the-art algorithms lose 40+% (and they cannot find any solutions for 3 out of 10 subjects). We also show that GREAP is the only algorithm which always finds solutions when the number of objectives increases from 2 to 4 (quality reduced by only 9%). In general, for 4 objectives and a “normal” time budget (see Section V-E), GREAP is 178% better than the other algorithms (if we exclude the subjects for which the other algorithms cannot find any solutions) – see Table VI.

This paper is organised as follows: Section II presents the related work, Section III defines formally the problem; Section IV introduces our algorithm; Sections V and VI present the experimental setup and the results of the evaluation; and finally Section VII concludes the paper.
II. RELATED WORK

Testing software systems usually takes the form of creating and running test cases, which aim at checking whether the program under test is behaving as expected. Any wrong program logic is supposed to make the tests fail – while when tests pass, we assume the behaviour of the program under test is correct (as long as the tests are exhaustive and correct). The set of all test cases is called a test suite. Developers and testers have worked with all sorts of metrics to assess the quality of tests, and in particular coverage metrics are widely used. Test resource managers also consider resource consumption (e.g., tests execution time, financial cost of running the tests) as an important element. Creating tests is a skill- and labour-intensive tasks and automatic test generation [2], [12] is an important element. Creating tests is a skill- and labour resource managers also consider resource consumption (e.g., tests execution time, financial cost of running the tests) as an important element. Creating tests is a skill- and labour-intensive tasks and automatic test generation [2], [12] is the focus of a lot of interest in academia and industry. Software artefacts evolve constantly though: various stakeholders and developers change their opinions about what applications should do and how to achieve their goals, parts of the code are improved or re-factored, and so on. Tests are then used to ensure that nothing bad is introduced in the programs and they are executed very often against the evolving programs.

Three directions have been proposed to address this problem [13]: Test Case Minimisation [4] aims at providing subsets of the initial test suite by eliminating redundant tests [14], i.e., tests that can be forgotten with no major impact Test Case Prioritisation [15] aims at reordering the test suite, in order to find the best order in which to apply the tests and increase the chances of finding the defects at an early stage Test Case Selection, the one we address in this paper and the focus of the remaining of this paragraph, aims at selecting a subset of the original test suite which balances quality and cost of the test suite. Early works have often addressed the problem as a single objective, with one property fixed (either cost or quality) and the other property optimised. Fischer et al. [16] proposed a 0-1 integer programming problem formulation while Rothermel et al. [4]) later proposed a graphical representation of the problem. In 2001, an empirical comparison study by Mansour et al. [17] compared the early algorithms applied on test case selection. In 2007, Yoo and Harman [5] presented the first work on multi-objective test case selection and introduced the concept of Pareto efficiency of selected set of tests, that they solved using an evolutionary algorithm (i.e., NSGA-II [18]). They have later extended their study with different objective P for the problem, using a cluster-based evolutionary algorithm and consider four objectives (execution time and three quality measures); while Zheng et al. [7] evaluate MOEA/D for the problem, using a various number of coverage objectives (see Section III).

Now that the problem is widely considered multi-objective, the question of picking the right objectives becomes important. Indeed, when objectives are not independent, they have an impact on each other and optimising one may lead to optimising others – and in turn algorithms that optimise this “dominant” objective(s) have an advantage. It is not a surprise that the coverage metrics we propose in our study are not totally independent. After all, they all try to maximise how much of the program is tested. The relative impact of one on the others is not clear though and recent studies by Gregory Gay [19] show that there is a lot of research to be done in this domain – Gay’s work addresses another problem (namely test generation) but we think his conclusions can be extended to our work. In particular, Gay’s finding that simple objectives (line/branch coverage) are very efficient is a sign that they cannot be dismissed. Another of Gay’s conclusions is that combinations of objectives have unique results, that are difficult to achieve when using single-/mono-objectives. This also reinforces our ideas that the software testing field (and in particular test selection) needs multi-objective approaches.

III. PROBLEM DEFINITION

Test selection is an important test resource management problem where algorithms try to minimise the number of tests required to stress a software artefact. Each test in a test suite covers in some ways a part of the program and the general idea is to find the minimal set of tests that covers the whole program – or the largest part of the program. The general idea being that running less tests (or just the right number of tests) can improve the resource management.

There are various test coverage metrics: line coverage, instruction coverage, branch coverage, etc. In this paper, we select 3 of them in addition to the running time of the tests (see below the definition of the problem’s objectives). Each of these coverage metrics sees the program from a different perspective: for instance as a sequence of instructions (instruction coverage) or as a tree (branch coverage). Our approach is to assess algorithms that are designed to explore large multidimensional search spaces - and that is why we picked them. The choice of objectives is in this case of lesser importance.

If a subset of tests $T'$ covers, according to a coverage metric $c_j$, the element $p'_j \in P'$ of the program $P$ then we have the following equation: $c_j(T', p'_j) = 1$. We use this equation to assess how much of a program is covered by a set of tests, knowing that a program $P$ is made of all its elements $p'_j$. We say that a program $P$ is fully covered, according to coverage metric $c_j$, by a set of tests $T = \{t_1, t_2, \ldots, t_n\}$ (each $t_i \in T$, $T$ being the original, full, set of tests), if:

$$\forall p'_j \in P', \quad c_j(T, p'_j) = 1$$ (1)

As said in the introduction of this paper, we see this problem as a multi-objective optimisation problem, and we try 3 different combinations of objectives. Each of the different coverage metrics, as well as the time to run tests, is seen as a different objective $O_j \in O$.

The first coverage objective $O_1$ aims at maximising the line coverage $c_1$ of lines $p'_1 \in P'$ of the program $P$. The second coverage objective $O_2$ aims at maximising the branch coverage $c_2$ of code branches (control structures with all their branches executed at least once) $p'_2 \in P'$ of the program $P$. The last coverage objective $O_3$ is inspired by the modified condition /
decision coverage (MC/DC) where we keep two criteria and aim at maximising the MC/DC \( c_3 \) of decision coverage \( p_i \in P^3 \) of the program \( P \). We consider that a statement \( i \) is MC/DC covered if and only if the two following criteria are met: (i) each decision takes the value true and false during testing; and (ii) each condition takes the value true and false during testing – where a condition is a boolean atomic expression and a decision is a boolean expression composed of different boolean operators and conditions. The fourth and final objective \( O_4 \) in our work is the execution time of running all selected tests.

The multi-objective model of our problem can be described through the following formulation:

\[
\text{minimise : } O_j = -\sum_{p_i \in P^j} c_j(T, p_i) \quad \forall j \in \{1, 2, 3\}
\]

\[
O_4 = \sum_{i \in T} \text{cost}(t_i)
\]

subject to : \( T = \{t_1, t_2, \ldots, t_n\} \in \mathcal{P}(T) \)

The aim of multi-objective optimisation techniques is to find the set of Pareto optimal solutions [20] (a.k.a., Pareto front). A solution \( T' = \{t'_1, t'_2, \ldots, t'_n\} \in \mathcal{P}(T) \) is in the Pareto optimal set (also said as non-dominated) if and only if there is no solution \( T'' = \{t''_1, t''_2, \ldots, t''_n\} \in \mathcal{P}(T) \) with all objectives (\( c_i \)'s and cost in our case) better or equal than the objectives of \( T' \), with at least one objective strictly better. \( T' \) is said to be dominated by \( T'' \) if and only if \( \forall O_i \in O, O_i(T') \leq O_i(T'') \) and \( \exists O_k \in O \mid O_k(T') < O_k(T'') \). In short, each solution on the Pareto front is a good and makes a unique trade-off between the objectives – in the sense that no other currently found solution is better than this solution on all dimensions.

IV. GReedy Evolutionary Algorithm Pathfinder

Large and complex search spaces, such as the ones we are addressing in our work, are challenging for classical optimisation techniques. Random/greedy techniques generate a lot of poor solutions and do not work well; Local Search techniques do not progress quick enough in such large search spaces; exact solvers are mostly mono-objective and require complex scalarisation techniques and do not scale well. The solutions that seem the most promising are evolutionary algorithms [5], [7], sometimes combined with greedy algorithms [6]. However, they are known to improve the set of solutions quite slowly, due in part to the poor initial population (hence the use of greedy algorithms to bootstrap the evolutionary algorithms).

Our solution uses a three stage method [8], [11] composed of three optimisation algorithms applied successively: (i) first we use a modified GRASP [21] in order to ‘aggressively’ produce an initial population with good values – and also a good coverage of the non-dominated set of solutions (i.e., with good variety among the different solutions); (ii) the second phase is a classic evolutionary algorithm, NSGA-II [18], but applied to the population produced by the first phase. This phase aims to exploit information from GRASP and produce a good approximation of the Pareto set; and (iii) finally a third phase pushes locally and aggressively solutions from previous stages to the Pareto front; in our algorithm we used a path-relinking [22]. Each step is executed for a maximum given time based on the overall execution. The greedy part of the first phase and the third can also be interrupted if they achieve a certain goal (e.g., when GRASP generates enough initial solutions, or when the path-relinking has paired all solutions).

A. First Step: Greedy Algorithm

The aim of this first step is to produce the initial population of 100 individuals – required by GREAP’s second step (using NSGA-II). We use a modified GRASP algorithm [21] to create a first set of 80 solutions. The algorithm builds a solution from an empty subset of tests and at each iteration, the algorithm adds randomly one of the best tests (say, \( t_i \)) according to a particular utility function. The utility is the normalised sum of coverage values \( t_i \) can add to the solution, divided by the number of coverage objectives. This value is then multiplied by a direction \( \lambda \), then we subtract the sigmoid normalised cost of the test multiplied also by a direction \( 1 - \lambda \). This direction is modified to obtain solutions with different “perspectives” on the coverage, and cost, objectives.

Let \( T \subseteq T \) be the selected tests at a given iteration of the GRASP phase, with coverage objectives \( O_j', \forall j \in \{1, 2, 3\} \). Let \( O_j', \forall j \in \{1, 2, 3\} \) be the new coverage objectives when adding a test \( t_i \in T \setminus T \) to \( T \). We consider that \( g'(t_i) = O_j' - O_j' \), \( \forall j \in \{1, 2, 3\} \) the potential gain on each of the considered coverage objectives when adding \( t_i \) to the current set of selected tests \( T \). We also increase the running time of the set of tests when adding test \( t_i \), \( w^*(t_i) = O_j' - O_j' \). Finally, we define the utility \( U(t_i) \) of adding a test \( t_i \) to the selected ones as follows:

\[
\begin{align*}
x_1 &= \sum_{j \in \{1, 2, 3\}} \frac{g'(t_i)}{\max_{q \in \mathcal{P}(q(t_i))} q'(t_i)} \\
x_2 &= \frac{w^*(t_i)}{\max_{q \in \mathcal{P}(q(t_i))} w(t_i)} \\
U(t_i) &= x_1 \times \frac{1}{\lambda} - \frac{(1-\lambda)}{(1+e^{-\lambda})}
\end{align*}
\]

with \( \lambda \in [0, 1] \) being the value that allows the exploration of different directions in the search space. The first two \( \lambda \) directions picked are 0 and 1. The former builds a solution with no selected tests (so a cost objective of 0) and the latter with the maximum coverage in all objectives (not necessarily all tests). After that, the directions (values of \( \lambda \)) are chosen to spread the exploration as much as possible (splitting the space covered by 2 previous values of \( \lambda \)).

At each iteration, the algorithm picks a (new) test from the original test suite so that the utility function is increased at least a factor \( \alpha \leq 1 \). This factor allows the algorithm to pick good tests, increasing the overall values of the selected set of tests. The stopping criteria of the algorithm, i.e., the conditions that stop the algorithm from adding tests are: (i) no tests left to add, (ii) full coverage of lines, branches and MC/DCs or (iii) a negative utility for all the tests. In our implementation, we fixed the value of \( \alpha \) at 0.70. At the end of the algorithm, the set of solutions is made of diverse good solutions. After that, a path-relinking algorithm [23] is applied. For each pair of solutions (a.k.a., “parents”), the path-relinking “navigates” from one parent to the other by adding or removing a test at
a time. If any intermediary solution is not dominated by its parents, the algorithm adds it to the set of solutions.

Finally, to obtain a population of 100 solutions for the second phase, we sort and keep only the non-dominated solutions. If the number of non-dominated solutions is greater than 100, we keep solutions with the best crowding [18] (high variety), otherwise the algorithm takes all found solutions as initial population in the next step [24], [25].

B. Second Step: Evolutionary Algorithm

GREAP’s second step is an evolutionary algorithm, i.e., a stochastic optimisation method, inspired by natural evolution – in particular evolutionary algorithms implement ‘their’ version of the concepts of mutation, crossover and selection. In our algorithm, we use the Non-dominated Sorting Genetic Algorithm II (NSGA-II) [18]. It is a Pareto-based algorithm, which aims to select solutions using Pareto dominance and in case of non domination between two individuals use the density of the neighbourhood of individuals. The initial population is generated by the first step of our hybrid algorithm, which gives a good bootstrap to the evolutionary algorithm. Note that we use all individuals from the first step as seeds [24], unlike in [26], [27] where only few good individuals are added to the initial population.

C. Third Step: Path-relinking

Finally, the third step is a path-relinking applied on the result of the second phase. We use the same idea seen in the first step: for every pair of solutions, the path-relinking algorithm looks for intermediary (feasible) solutions between them by adding or removing tests (one at a time). The intermediary solutions are then added to the list of good solutions if they are non-dominated. The algorithm runs for a certain time budget or until there is no more pair of solutions that have not been tried. The aim of the path-relinking step of GREAP is to “fill in” the gaps between solutions belonging to the Pareto front and to push this front as much as possible. We picked this algorithm and not any other local search algorithm (e.g., PLS as in other related work using three step methods[8], [11]) as the search space in our problem is not too constrained and most intermediary solutions are feasible.

V. Experimental Setup

This section presents: the metrics, the subjects, the time budget, and the algorithms we compare GREAP against.

A. Metrics

Comparing different sets of non-dominated solutions in a multi-objective context is a well-known problem [28]. First of all, because of the complexity and the size of the problem, it is usually not possible to obtain the exact Pareto frontier, i.e., the exact solutions. Second of all, because of the difficulties to compare (and visualise) solutions in a multi-dimensional space. Different metrics have been proposed in the literature, often to measure the sets of non-dominated solutions from various perspectives – namely the quality of the sets of solutions and the spread of the sets of solutions. Some of the metrics require to have the exact set of non-dominated solutions (the ideal Pareto front). As we do not have this (it is in practice often impossible to obtain) we use a classical estimation: the best set solutions given by all the algorithms. All of the metrics we use are known to be good ones for the comparison of sets of non-dominated solutions [28].

- We use the Hypervolume (HV) is one of the most popular metrics to assess the quality and the diversity of the sets of solutions. The Hypervolume computes the space between all solutions from the non-dominated set of solutions and a reference point. The exact Pareto front produces the best HV, as its solutions get the best values in every objective. Because of its well-known utility, popularity and good performance when it comes to comparing solutions, the HV is our favourite metric (and many of our experiments will only consider this one).
- The second metric, which focuses on quality, is the generational distance (GD) which computes the average Euclidean distance between solutions from the result of an algorithm and the nearest solution from our approximation of the exact Pareto front (to minimise).
- The third metric is the inverted generational distance (IGD), similar to the generational distance but computes the minimum distance between the result set of an algorithm and the approximated Pareto set. IGD is to be minimised for both a better diversity and quality.
- The generalised spread metric (GS) computes the spread of a population using the lower and upper bounds of objective values found and can be used for the diversity of solution sets. GS is useful if the sets of solutions have similar qualities. For the GS, the lower the better.
- We also use the Pareto front size metric (PFS), which returns the number of solutions in the result set of an algorithm that also belongs to the Pareto front. PFS is diversity-oriented, and the higher the better for PFS.
- Finally, our last metric is the epsilon metric ($\epsilon$), which estimates the minimal distance to transform every solution of a result set into a solution on the Pareto front. The lower $\epsilon$ the better are diversity and quality.

In our work, we aggregate results of all algorithms over the different runs as an approximation of the Pareto front.

B. Data-Set

We have picked 6 out of 10 subjects based on recent and/or widely considered state-of-the-art studies [5], [7]. We also selected larger subjects, doing what we think is a thorough analysis. We summarise the most interesting characteristics of the subjects in Table I. In particular, we report the number of lines of code (LOC) and number of tests. All the subjects (see Table I) are C programs, obtained from the Software-artifact Infrastructure Repository (SIR [29]), a large repository of software artefacts popular in academia.

We use the tool Gcov to measure the coverage metrics. Gcov is a source code coverage analysis and profiling tool that gives which line/instruction/branch is executed by which test. We also collected the execution time of all tests – which gives us the cost value for each test.
C. Algorithms

We have compared our own solution (GREAT) against two well-known evolutionary algorithms: NSGA-II [18] and MOEA/D [30]. They are both executed in the exact same conditions as our solution. NSGA-II is one of the most popular genetic algorithm – note that we use NSGA-II in the second phase of GREAP (see Section IV-B). MOEA/D has recently been used in a multi-objective test selection work [7] and has proven to have very good results.

Note that we did not have access to the implementation provided by the authors of [7] and [18]. We decided to stay as generic and impartial as possible, and we used the MOEA framework [31]. MOEA is a free and open source Java library with a panel of multi-objective evolutionary algorithms implemented and ready to use. Our algorithm is also implemented in Java, and also use the MOEA framework for its second phase (NSGA-II). The parameters used for the two algorithms and for its second phase are the default values from MOEA framework (population sizes equal to 100).

D. Setting the Time Budget for Each Phase

GREAT is a three step hybrid algorithm, and we need to allocate an execution time for each of the steps. We have selected 12 different triplets of parameters, each parameter representing the percentage of time allowed to the corresponding phase. We ran GREAT 10 times with each triplet on one of the hardest problem (i.e., Schedule with 4 objectives) and evaluated the average results on all our metrics.

Table II reports the triplets alongside their average result metrics with the following format: a triplet “a,b,c” corresponds to a% of the time allowed on the first phase, b% on the second phase and c% on the last. In bold are the best values. The results show the importance of the first and third steps: the average results on all our metrics.

Table I

<table>
<thead>
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<th>Data-set</th>
<th>gzip-v3</th>
<th>gzip-v4</th>
<th>space-v38</th>
<th>schedule-v2</th>
<th>totinfo-v1</th>
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<tr>
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<td>150</td>
<td>2650</td>
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</table>

<table>
<thead>
<tr>
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<th>space13k-v38</th>
<th>grep</th>
<th>sed</th>
<th>make-v1</th>
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<td>14427</td>
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<td>13585</td>
<td>809</td>
<td>370</td>
<td>1044</td>
</tr>
</tbody>
</table>

E. Experimental Process

Our experiments were run on the 10 subjects presented earlier, for the three combinations of objectives (two, three, four) and the three algorithms (NSGA-II, MOEA/D and our own GREAP). Because evolutionary algorithms and our greedy step are stochastic methods, we performed 30 runs and averaged the results for for each set up to reduce the impact of randomness.

We varied the number of objectives for the problem, using 2, 3 or 4 objectives by taking (in this order): (i) the cost, (ii) the line coverage, (ii) the branch coverage and (iv) the MC/DC coverage. The more objectives there are in the problem the more difficult the problem is. We also varied the time budget (see Table III) for the algorithms, starting with a value $T$ that corresponds to what was allowed in [7] for the six first subjects – we then decreased that value to $T/2$ and $T/4$. We also evaluated the algorithms on a larger budget, $2T$ to see how well the algorithms performed in a less constrained environment. Note that in the work of [7] they do not run their experiments on Space with three or four objectives, therefore we chose arbitrary times, similar to the ones used for the two versions of gzip. For Space13k, also not used during previous papers, we allow a big arbitrary time for 2 objectives, but afterwards for 3 and 4 objectives, times are computed using a similar scale as the increase of times alongside objectives for the three big data-sets (Tcas, Totinfo and Schedule). Finally for Make, Grep and Sed, also arbitrary times are used, picked to have similar behaviour than other data-sets.

VI. Experiments

We aim at answering the following four questions:

- **RQ 1**: Is GREAP robust against the increase of the number of objectives, which is known to be challenging?
- **RQ 2**: Is GREAP more effective (better quality and diversity) than the others evolutionary algorithms?
- **RQ 3**: How does GREAP compare to other algorithms when the time budget shrinks?
- **RQ 4**: Does GREAP react well to an increase of the test suite size (when we vary the test subjects)?

All the results presented in the current section are average values of ten runs. In order to be more readable, the values are rounded; yet, in all cases we kept enough decimals to still be able to compare the algorithms.

Values in bold are the best values from a particular perspective (described in the tables) and by default they are statistically significant (we used a Mann-Whitney U test) with a p-value below 0.05. These (best) values (in bold) are followed by an asterisk (*) when not statistically significant.

A. RQ1: Robustness against a Varying Number of Objectives

In Table IV, we report the evolution of Hypervolume when the number of objectives increases (from 2 to 4). The time used in the experiments is $T$ – as this is the typical time budget in related studies. In short, we fix the metric (HV) and the time ($T$) and only vary the number of objectives.

In general, the results show better performance for GREAP than for the other algorithms. Furthermore, the values are always statistically significant. However, these values are close for small subjects (the two versions of Gzip and Space), but this gap tends to increase with the size of the subjects (for medium subjects such as Grep and Sed but also for...
First, we notice that GREAP gets significantly better quality results (based on HV, IGD, GD and ϵ) than the other algorithms. The only quality result for which GREAP is not the best is GD for Tcas and Grep, and IGD for Sed. This is a good demonstration that GREAP is the best algorithm on all quality metrics (37 best values out of 40), with at least 3 out of 4 metrics showing better results for GREAP for all subjects.

Regarding the diversity metrics (PFS and GS), results show that many more solutions are provided by GREAP than by the two evolutionary algorithms. The generalised spread of the solutions is not always in favour of GREAP though, but when another algorithm gets better results than GREAP, this algorithm has very poor quality and size values – which to some extent beats the purpose of multi-objective optimisation.

We can conclude from this set of experiments that GREAP provides better solutions in terms of quality and produces solution sets with better diversity. Consequently, we conclude a better efficiency for GREAP than for evolutionary algorithms.

### C. Impact of the Time Budget on the Algorithms

Now (see Table VI), we answer **RQ 3**, and show the ‘aggressive’ behaviour of GREAP. In this set of experiments we decrease the time budget (from T to T/2 and then T/4) assigned to the algorithms, making the problem more difficult. We also increase the time budget (2T) to evaluate whether this has a different impact on the other algorithms than on GREAP.

First, all the results show statistically better performance for GREAP. Furthermore, we observe an increase of this improvement when the time budget decreases. This says that while the other evolutionary algorithms are impacted substantially by the decrease in time budget, GREAP keeps good Hypervolume values - especially for the six hardest subjects (Grep, Make, Space13k, Schedule, Totinfo and Tcas). For these six subjects, the other algorithms perform really poorly (Hypervolume values can even tend to 0 in the hardest cases) while GREAP does not vary much. Note that for the small subjects the impact on the other algorithms’ performance is limited, due to the simpler nature of these subjects.

GREAP always keeps good Hypervolume values even with smaller time budgets. The decrease in performance is not significant for small subjects and stays acceptable for larger ones. Furthermore, because of the small evolution of the Hypervolume in some cases, GREAP seems to have already converged to good solutions in four out of the ten subjects (The two Gzip versions, Space and Schedule), for the smallest time (T/4). For the other subjects, good solutions are already found at T/4, but GREAP keeps improving a bit the solutions. It’s only for Space13k, the hardest subject, that GREAP improves the Hypervolume significantly after T/4.

In terms of improvement, if we look at the impact on the algorithms performance when the time budget is reduced from T to T/4, we see that GREAP loses only 1% of quality, while NSGA-II (39%) and MOEA/D (47%) are impacted much more and cannot get any solution in some cases (Space13k, Schedule and Tcas). If we focus on a time budget of T (reminder: we have 4 objectives here) then GREAP is 178% better than the other algorithms (when they find any solutions at all).

### D. Impact of Subjects Size

Finally, looking at the previous three tables, we can evaluate the quality and the diversity of the solutions produced by the three algorithms when the size of the subjects vary. To simplify the analysis, we classify the subjects into: small-scale (Gzip

<table>
<thead>
<tr>
<th>Data-set</th>
<th>2 objectives</th>
<th>3 objectives</th>
<th>4 objectives</th>
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<tr>
<td>gzip-v3</td>
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<td>224.01</td>
<td>335.38</td>
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<tr>
<td>gzip-v4</td>
<td>179.38</td>
<td>254.06</td>
<td>319.70</td>
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<td>schedule-v2</td>
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<td>tcas-v1</td>
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<tr>
<td>tot_info-v1</td>
<td>294.38</td>
<td>297.70</td>
<td>335.00</td>
</tr>
<tr>
<td>Space-v38</td>
<td>170.00</td>
<td>240.00</td>
<td>310.00</td>
</tr>
<tr>
<td>Space13k-v38</td>
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<td>1,100.00</td>
<td>1,200.00</td>
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<tr>
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<tr>
<td>sed</td>
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</tr>
<tr>
<td>make</td>
<td>295.00</td>
<td>300.00</td>
<td>340.00</td>
</tr>
</tbody>
</table>
The answer to RQ 1: Is GREAP robust against the increase in the number of objectives, which is known to be challenging? is Yes.
we would like to explore further the combination of the three reliable and more robust than the state-of-the-art techniques, as GREAP, is faster at finding good solutions, and is more robust.

Now that we have proven that a three step method, such as GREAP, is faster at finding good solutions, and is more reliable and robust than the state-of-the-art techniques, we would like to explore further the combination of the three steps. We know from observation that each step has a different impact on the solutions. We would also like to use our 3 step method on other Software Engineering problems to evaluate how general this technique is, as on test suite minimisation which is really close to our problem.

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REFERENCES


