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<tr>
<th><strong>Title</strong></th>
<th>Thickness variation of self-processing acrylamide-based photopolymer and reflection holography</th>
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Abstract. There are many types of holographic recording material. The acrylamide-based recording material examined here has one significant advantage: it is self-processing. This simplifies the recording process and enables holographic interferometry to be carried out without the need for complex realignment procedures. However, the effect that the polymerization process has on the grating thickness must be examined. This question is fundamental to the material’s use in holographic optical elements, as thickness variations affect the replay conditions of the produced elements. This paper presents a study of this thickness variation and reports for the first time the production of reflection holographic gratings in this material.

Subject terms: holographic recording material; nondestructive testing; holography; holographic optical elements; reflection holography; photopolymer.

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2 Material Thickness Variations

Changes in the grating thickness affect the replay conditions of holograms and holographic optical elements. A thickness change in the form of either shrinkage or swelling will result in a change in the value of the replay angle for which maximum diffraction efficiency (DE) is obtained. This change is due to a change in fringe spacing in the thickness direction. In the case of slanted gratings, the fringe pattern recorded is slanted with respect to the surface of the recording layer, and any change in volume is due to expansion, which is perpendicular to the surface of the material. Such changes can be observed in slanted transmission and reflection gratings, but not in unslanted transmission gratings. In an unslanted grating the fringes are perpendicular to the surface of the material, and so thickness changes in the material do not affect the period of the fringes or the slant angle. This is demonstrated in Fig. 1, in which the angular scan data of an unslanted transmission grating show no change in on-Bragg angle as the material is bleached (exposed). Bleaching was carried out after recording, using a white light source. This process results in the polymerization of the remaining monomer. Any resulting material thickness variation was then monitored using angular scan data. The grating is replayed with a HeNe probe laser with wavelength 633 nm, which was chosen because it is outside the wavelength sensitivity region of the recording material.

The gratings were recorded with a slant angle of 25 deg, using unsealed 120-μm-thick layers. The angular scans of the gratings produced were obtained: (1) after recording, (2) after bleaching, and then (3) at hourly intervals up to 14 h. This process enabled us to observe any thickness changes during the recording and the bleaching stages.

The effects of swelling of the material can be seen clearly when the grating tested is slanted rather than unslanted. Typical angular scans for the slanted case are shown in Fig. 2. The six angular scans show the movement of the on-Bragg replay angle during the bleaching process. The angular deviations of the on-Bragg maxima of the scans were taken and are plotted in Fig. 3. The movement of the on-Bragg angle indicates that the material swells during the initial stages of bleaching and then appears to shrink or relax after a period of 5 h. The material layer, which was initially ≈120 μm thick, is shown to swell to ≈128 μm after a period of 5 h and then to relax to ≈124 μm after a further 7 h. This material thickness variation is illustrated in Fig. 4.

The changes in the replay conditions due to material thickness variation are modeled as follows. A schematic diagram of the effect of swelling on the grating geometry is shown in Fig. 5. This diagram shows that the swelling of the material by an amount Δd results in a change ΔΛ in the period of the grating. The effect that such a grating thick-

Table 1 Specifications of the photopolymer recording material used in the experiments.

<table>
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<th>Specifications</th>
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<tr>
<td>Monomers: Acrylamide and N,N′-methylenebisacrylamide</td>
</tr>
<tr>
<td>Wavelengths: 514 and 633 nm</td>
</tr>
<tr>
<td>Diffraction efficiency: 90%</td>
</tr>
<tr>
<td>Spatial-frequency response: 500–2500 lines/mm</td>
</tr>
<tr>
<td>Sensitivity: 96% DE at 78 mJ/cm²</td>
</tr>
</tbody>
</table>

Fig. 1 Bragg replay angle is shown to be unchanged for unslanted grating (14 angular scans over 14 h).

Fig. 2 Variation in on-Bragg replay angle due to material thickness variations. Initial thickness=120±10 μm (micrometer screw gauge), initial slant angle=25 deg, initial spatial frequency = 1000 lines/mm, λ = 633 nm.

Fig. 3 Change in the Bragg angle for a slanted transmission hologram due to thickness changes caused by the bleaching process. Initial thickness=120 μm, initial slant angle=25 deg, initial spatial frequency=1000 lines/mm.
ness change has on the fringe spacing and the on-Bragg replay angle can be determined as follows.

The period of the grating before swelling, $\Lambda_0$, is

$$\Lambda_0 = \frac{\lambda}{2n_{av,0} \cos(\phi_0 - \theta_{B,0})},$$  \hspace{1cm} (1)

where $\theta_{B,0}$ is the initial on-Bragg replay angle, $n_{av,0}$ is the initial average refractive index before swelling, $\phi_0$ is the initial slant fringe of the grating, and $\lambda$ is the replay wavelength. The period of the grating after swelling is

$$\Lambda_1 = \frac{\lambda}{2n_{av,1} \cos(\phi_1 - \theta_{B,1})},$$  \hspace{1cm} (2)

where the subscript 1 indicates that the parameter corresponds to the grating after swelling. It can be seen that

$$\Lambda_1 = \Lambda_0 + \Delta \Lambda_z.$$

We now take $\Lambda_{z,0}$ to be the original period of the grating in the $z$ direction, and $\Lambda_{z,1}$ to be the period in the $z$ direction after swelling. The difference between the fringe spacings before and after swelling is given by

$$\Lambda_{z,1} = \Lambda_{z,0} + \Delta \Lambda_z.$$

From Fig. 5, we see that

$$\Lambda_{z,0} = \frac{\Lambda_0}{\cos \phi_0} \text{ and } \Lambda_{z,1} = \frac{\Lambda_1}{\cos \phi_1}.$$  \hspace{1cm} (5)

The difference in the fringe spacing can therefore be rewritten as

$$\frac{\Lambda_1}{\cos \phi_1} - \frac{\Lambda_0}{\cos \phi_0} = \Delta \Lambda_z.$$  \hspace{1cm} (6)

The fractional change in fringe spacing in the $z$ direction, $\Delta \Lambda_z/\Lambda_z$, is equal to the fractional change in grating thickness, $\Delta d/d$:

$$\frac{\Delta \Lambda_z}{\Lambda_z} = \frac{\Lambda_1 \cos \phi_0 - 1}{\Lambda_0 \cos \phi_1} = \frac{\Delta d}{d}.$$  \hspace{1cm} (7)

We can also see from Fig. 5 that

$$\frac{\Lambda_1}{\Lambda_0} = \frac{\sin \phi_1}{\sin \phi_0}.$$  \hspace{1cm} (8)

We can therefore write the expression for the fractional change of the grating thickness as

$$\frac{\Delta d}{d} = \tan \phi_1 - 1.$$  \hspace{1cm} (9)

This expression can be rearranged to find an expression for the slant angle after swelling,

$$\phi_1 = \tan^{-1}\left[1 + \frac{\Delta d}{d}\tan \phi_0\right].$$  \hspace{1cm} (10)

Substituting this expression for $\phi_1$ into Eq. (8) gives us an expression for the ratio of the grating periods before ($\Lambda_0$) and after swelling ($\Lambda_1$):

$$\frac{\Lambda_1}{\Lambda_0} = \frac{\sin[\tan^{-1}\left[1 + \frac{\Delta d}{d}\tan \phi_0\right]]}{\sin \phi_0}. $$  \hspace{1cm} (11)

This change in fringe spacing is also equal to Eq. (3); therefore,

$$\frac{\Lambda_1}{\Lambda_0} = \frac{n_{av,0} \cos(\phi_0 - \theta_{B,0})}{n_{av,1} \cos(\phi_0 - \theta_{B,1})}. $$  \hspace{1cm} (12)
Equation (11) has been used to generate Fig. 6, which shows the relationship between the fringe spacing and the thickness of the grating. From Fig. 6 we see how the fringe spacing is dependent not only on the grating thickness but also on the slant angle of the grating. Three different slant angles are plotted to show that the effect is more pronounced the greater the slant angle.

This change in fringe spacing coupled with the change in slant angle causes the on-Bragg replay angle to increase or decrease. The relationship given in Eq. (12) is plotted in Fig. 7. Therefore, by recording the angular scan of the grating as a function of time and using these curves to find the position of the on-Bragg maxima, it is possible to estimate the effective grating thickness variations by comparison with the theoretical predictions. The thickness variation corresponding to the movement in the on-Bragg angle, shown in Fig. 3, can be calculated using Eq. (12), assuming that the average index of the material before and after swelling is constant (an assumption that is almost certainly incorrect). The material thickness variations over the course of the bleaching process calculated from the experimental data are shown in Fig. 4.

This experiment can be carried out using an automated recording and testing rig. The rig allows the above experiments to be carried out automatically, allowing more detailed analysis.

The angular scans obtained for slanted gratings in these experiments showed no variations in the on-Bragg angle during the recording stage. This result indicates that there is no change in the thickness of the material during the recording step.

3 Reflection Holography Experiments

The study of slanted holographic gratings as described above shows that there is no dramatic swelling or shrinkage of the material at slant angles of 25 deg. However, as shown, the effect of material variations is more pronounced at higher slant angles. Therefore an attempt to record a reflection-geometry hologram was made. The hologram discussed here has a slant angle of 85 deg. The ability to record such a grating would further corroborate the previous result that the material does not swell appreciably at a spatial frequency of 1000 lines/mm.

The spatial frequency of a grating is determined by the recording wavelength and the angles of incidence of the recording beams used to produce it. The spatial frequency of an unslanted reflection-geometry grating is given by

$$f = \frac{2n_0 \cos \theta_B}{\lambda},$$

where

- \(f = 1/\Lambda\) = spatial frequency
- \(n_0\) = refractive index of the recording medium
- \(\lambda\) = wavelength of the recording beams
- \(\theta_B\) = angle of incidence of the recording beams within the material.

Given the material resolution limitations, experiments were carried out to record gratings that were well within the spatial frequency response range. The spatial frequency chosen for the experiments was 1000 lines/mm. Transmission holograms recorded at this spatial frequency have been produced experimentally with diffraction efficiencies of \(\approx 78\%\), as can be seen in Fig. 8.

We assume that the two recording beams make the same angle with the material (i.e., an unslanted recording geometry) and the refractive index is approximately 1.5. The recording angles required are very high, \(\approx 70\) deg, with respect to the normal of the recording material. This large
angle of incidence introduces a large Fresnel boundary reflection,\textsuperscript{16} causing a large drop in the optical power entering the recording material. The Fresnel reflections can be reduced by using a prism to couple the light into the recording material. However, the use of a prism coupler introduces the need for a suitable index-matching fluid. A number of liquids were examined for compatibility with the recording material. The index-matching liquids were required to be thermally stable, commercially available, of controlled quality, and inert (nontoxic).

### 3.1 Index-Matching Fluid

It is necessary to index-match the prisms to the surface of the recording material. This is achieved with the use of an index-matching fluid. The recording material has a refractive index similar to glass (i.e., \(n \approx 1.5\)). The index-matching fluid initially used was ortho-xylene. It is a volatile chemical, which might have some effect on the recording processes in the material. Therefore it was decided that other index-matching fluids should be investigated. The refractive index values of several oils were measured using a Bellingham and Stanley Ltd refractometer. The absorbance of each of these liquids was measured using a Shimadzu UV 2101 PC absorption spectrophotometer in the DIT Spectroscopic Facility. A number of different index-matching fluids were examined, as shown in Table 2. The index-matching fluid chosen for use was silicone 702, as it is both stable and inert and has both a low absorption at the recording wavelength and a refractive index close to that of glass.

### 3.2 Recording Geometry

The recording geometry used in these experiments is shown in Fig. 9. The plate in this geometry is held perpendicular to the mount, which has the advantage that the two recording beams have TE polarization with respect to the recording material. Thus the visibility of the recording fringes is maximized. This prism setup produces an angle of 10.52 deg to the surface of the recording material, i.e., an angle between the recording beams of 21.04 deg. The grating produced using this geometry has a spatial frequency of 1066.43 lines/mm and is unslanted. The slanted arrangement, which was used for the reflection-holography experiments, produces a similar spatial frequency, 1066.13 lines/mm, as the prisms are only rotated by a small angle, \(\approx 5\) deg.

The recording material was desiccated, sealed,\textsuperscript{12} and then index-matched to the two prisms using silicone 702 oil. The recording material and the prisms are oriented so to produce a slanted grating, \(\phi_0 = 3.1^\circ\). This ensures that the diffracted beam and the reflected beam, which arise from imperfect index matching, do not overlap. Thus the low-intensity diffracted beam can be observed with greater ease. Using this method, it was possible to record reflection gratings reproducibly with a typical diffraction selectivity (DS)—i.e., the ratio of the diffracted beam intensity to the throughput beam intensity outside the prisms—of \(\approx 18\%\).

### 3.3 Reflection Results

The experimental setup has been used to record reflection gratings in this photopolymer material for the first time. Typical results obtained were a DS of \(\approx 18\%\). The DS of a grating is defined as

\[
\text{DS} = \frac{I_D}{I_T + I_D},
\]

where

\begin{align*}
I_D &= \text{diffracted light intensity outside the prism} \\
I_T &= \text{transmitted light intensity outside the prism} \\
\end{align*}

The DS result does not compensate for the Fresnel reflections from the prism air boundaries. Therefore it is necessary to calculate the diffraction efficiency of the grating with compensation for these boundary reflections. A schematic diagram of the replay conditions is shown in Fig. 10. The angle of incidence, \(\alpha\), and the transmitted angle, \(\beta\), can be used to find the Fresnel reflection coefficients\textsuperscript{17} and so the optical power reflected at each boundary. The power reflected at a boundary can be calculated using the expression for the reflectance \(R\), which is given by

\[
R = \frac{\sin^2(\alpha - \beta)}{\sin^2(\alpha + \beta)}. \tag{15}
\]

The reflected power \(I_{\text{ref}}\) from the first glass-air boundary is

\[
I_{\text{ref}} = RI_{\text{in}}, \tag{16}
\]

where \(I_{\text{in}}\) is the incidence power; and the input power reaching the recording material, \(I_{\text{inside}}\), is

\[
I_{\text{inside}} = I_{\text{in}} - I_{\text{ref}}. \tag{17}
\]

---

**Table 2** Some index-matching fluids and the absorbance of each at the recording wavelength 514 nm.

<table>
<thead>
<tr>
<th>Index-matching liquid</th>
<th>Refractive index (n)</th>
<th>Absorbance at (\lambda = 514,\text{nm})</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>KSO 5VK</td>
<td>1.452</td>
<td>0.025</td>
<td>18</td>
</tr>
<tr>
<td>Mouldlubric 8035</td>
<td>1.480</td>
<td>0.030</td>
<td>18</td>
</tr>
<tr>
<td>KSO1</td>
<td>1.474</td>
<td>0.035</td>
<td>18</td>
</tr>
<tr>
<td>Silicone 702</td>
<td>1.510</td>
<td>0.020</td>
<td>19</td>
</tr>
<tr>
<td>o-Xylene</td>
<td>1.5058</td>
<td>0.010</td>
<td>19</td>
</tr>
</tbody>
</table>
Similarly, the diffracted power inside the prism is given by

\[ I_{d,\text{inside}} = \frac{I_{d,\text{outside}}}{1 - R}, \]

where \( I_{d,\text{outside}} \) is the diffracted beam power outside the prism and \( I_{d,\text{inside}} \) is the power inside the prism. Therefore the DE of the holographic optical element is given by

\[ \text{DE} = \frac{I_{\text{inside}}}{I_{d,\text{inside}}}. \]

The DE of the reflection grating described was calculated to be \( \approx 21\% \), which is larger than the DS, as is expected.

Several such recordings were made. Thus, although some shrinking or swelling may occur, we have demonstrated that the material must be sufficiently stable to allow relatively low-DE reflection holograms to be recorded.

4 Conclusions

In this paper we report the initial shrinkage of an acrylamide-based photopolymer material followed by a swelling period during the recording and bleaching recording stages. There appears to be no appreciable swelling during the recording stage at a spatial frequency of 1000 lines/mm. Earlier research regarding low-spatial-frequency elements has reported swelling of the material at low spatial frequencies and suggested that this behavior is expected from the thermodynamic model of hologram formation.\(^\text{11}\) A study of the response of this material at low spatial frequencies may lead to the establishing of a conclusive connection between these two effects.

This paper also reports, to the best of our knowledge, the first example of reflection gratings produced in such an acrylamide-based dry photopolymer system. The DE of the recorded elements is low, \( \approx 21\% \)—lower than might be expected in view of the efficiencies achieved for comparable transmission gratings with spatial frequencies of 1000 lines/mm. This low DE may be due to the material’s high-order sensitivity or to average-refractive-index effects. Improvement of the material’s stability using aerosol sealant is currently under examination.\(^\text{12}\)

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References

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