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Towards Solving Multi-channel RF-SoC Integration Issues Through Digital Fractional Division

S.Amir Reza Ahmadi Mehr, Student Member, IEEE, Massoud Tohidian, Student Member, IEEE, Robert Bogdan Staszewski, Fellow, IEEE

Abstract—In modern RF-SoCs the digital content consumes up to 85% of the IC chip area. The recent push to integrate multiple RF-SoC cores is met with heavy resistance by the remaining RF/analog circuitry, which creates numerous strong aggressors and weak victims leading to RF performance degradation. A key such mechanism is injection pulling through parasitic coupling between various LC-tank oscillators as well as between them and strong transmitter outputs. Any static or dynamic frequency proximity between aggressors (i.e., oscillators, transmitter outputs) and victims (i.e., oscillators) that share the same die causes injection pulling, which produces unwanted spurs and/or modulation distortion. In this paper, we propose and demonstrate a new frequency planning technique of a multi-core transmitter where each LC-tank oscillator is separated from other aggressors beyond its pulling range. This is done by breaking the integer harmonic frequency relationship of victims/aggressors within and between the RF transmission channels using digital fractional divider based on a phase rotation. Each oscillator center frequency can be fractionally separated by $\sim$28% but, at the same time, both producing closely spaced frequencies at the phase rotator outputs. The injection pulling spurs are so far-away that they are insignificantly small (-80 dBc) and coincide with a second harmonic of the carrier. This method is experimentally verified in a two-channel system in 65-nm digital CMOS, each channel comprising a high-swing class-C oscillator, frequency divider, and phase rotator.

Index Terms—Digitally controlled oscillator (DCO), digital fractional divider, frequency pulling, injection locking, multi-core radio, system-on-chip (SoC), RF-SoC.

I. INTRODUCTION

The abundance of wireless connectivity (e.g., WiFi, Bluetooth) and cellular (e.g., GSM, WCDMA, LTE) communication standards has made the multi-band, multi-mode radios in mobile devices a pervasive trend. There is a relentless push towards a system-level integration and, recently, multi-core radio integration enables to manufacture less bulky equipment that is much cheaper and consumes less power. At the same time, allowing multiple radios to simultaneously coexist within a single silicon die leads to a hostile environment with various aggressors and victims affecting each other. An example of such a scenario could be a coexistence of LTE with 2.4 GHz WLAN and Bluetooth [1]. Moreover, modern radios need to support features such as frequency division duplex (FDD) and carrier aggregation for high data-rates, which further worsen the coupling problem.

Furthermore, the use of nanoscale CMOS processes allows for an unprecedented degree of scaling and integration in digital circuitry, but complicates the implementation of traditional RF and analog circuits, of which linear transistor operation, keeps on getting worse with each CMOS process node advancement in almost every aspect. On the other hand, the raw digital capability, in terms of processing sophistication and speed, is improving. Consequently, a need has arisen to find digital architectural solutions to the RF functions [2].

A major coexistence problem on the transmitter (TX) side is caused by injection pulling, which degrades signal integrity and creates unwanted emissions. Any oscillatory system, such as an LC-tank-based PLL, is generally vulnerable to injection pulling through parasitic coupling. This pulling will likely be the main cause degrading spectral purity of the TX output [3].

Nowadays there is a strong push to integrate a power amplifier (PA) with the rest of TX due to cost reasons. This has already happened in wireless connectivity (e.g., Bluetooth, WiFi) and is now happening in cellular mobiles. On the basestation side, integrating a 200 W PA on the same die as the TX is not seriously considered yet. However, there are attempts to integrate the RF front-end portion with the PA within the same package [4]. In these scenarios, the harmonics of the PA output or even the TX output driver are typically not attenuated enough and can injection-pull the oscillator. In practice, it has been shown that even very weak signals injected into the LC-tank oscillator can have dramatic consequences on the RF system performance [3]. Single-chip RF system solutions have the potential problem of signal integrity, stemming from the fact that the switching digital circuitry and the sensitive analog circuits share the same substrate. This issue is becoming exponentially more severe in multi-radio systems that share the same die. In a single-radio RF system, the output PA can pull the oscillator; however, in...
multi-radios not only the output PAUs but also all oscillators can pull each other. Generally, there are three sources of parasitic coupling [5]. As shown in Fig. 1, each oscillator and PA can couple resistively, magnetically and capacitively to each other. In many cases, due to the low resistivity substrate, which is the case for the scaled CMOS technology, noise/interference can pass throughout the entire chip. Thus, the analog circuits nearby the noise/interference sources will suffer the most. Fig. 1 illustrates the aggressor/victim scenarios in the most recent multi-core radios.

In this paper, we first investigate the negative pulling effects in a two-channel system (Section II). Afterwards, in Section III we propose and investigate frequency planning by means of a fractional ratio \(f_{\text{osc}} \neq k \cdot f_0, k \in \mathbb{N}\) between the LC-tank oscillators resonating at \(f_{\text{osc}}\) and the PA stages operating at \(f_0\). This way, the near-integer harmonic relationship between the aggressors and the victims will be eliminated [6] and the pulling issues due to various multiple paths can be prevented. A low-power architectural solution for the fractional frequency translation is proposed in Section IV. Section V presents the detailed circuit implementation and measurement results providing insight into the selection of proper pulling countermeasures.

II. INJECTION PULLING EFFECTS

The effects of injection locking and pulling of an oscillator by a periodic signal were first studied by Adler [7] and then thoroughly investigated in [8]–[11]. As elaborated in [8], the oscillator can maintain lock to the injected signal only within a limited frequency lock range \(\omega_L\), estimated as:

\[
\omega_L = \omega_0 \cdot \frac{I_{\text{inj}}}{I_{\text{osc}}} \cdot \frac{1}{\sqrt{1 - \frac{I_{\text{inj}}^2}{I_{\text{osc}}^2}}} \quad (1)
\]

where, \(\omega_0 = 2\pi f_0\) is the natural angular resonant frequency of the tank and \(Q\) is its quality factor. The lock range depends on the injection current \(I_{\text{inj}}\) versus the oscillator current \(I_{\text{osc}}\), and \(Q\)-factor: the weaker \(I_{\text{inj}}\) the lower the chance for locking, and the lower the \(Q\) the wider the locking range. The pulling phenomena have been studied for a single oscillator under injection. However, as mentioned above, mutual coupling between two or more oscillators will happen in increasingly more applications [9], [12].

Furthermore, integrated transmitters contain a PA or its driver (“pre-PA”), whose large-swing signals can couple to various parts of the system including the sensitive LC-tank oscillators. An output power greater than just a few mW might thus cause appreciable degradation during an 8-PSK modulated transmission [13]–[15]. In order to study the serious effects of pulling in advanced integrated transmitters, and to offer potential solutions, a two-channel system with ~8 GHz oscillators is realized in 65 nm digital CMOS. Non-dotted blocks in Fig. 1 were implemented on the IC, whose micrograph is shown in Fig. 2a.

The two oscillators with overlapping tuning range are placed 200 \(\mu\text{m}\) apart on the same CMOS die (center-to-center distance between the inductors is 700 \(\mu\text{m}\)). This may correspond to the tight floorplanning environment of today’s commercial multi-channel SoCs. The two oscillators have separate bias and frequency tuning bits. It is important to stress that each oscillator simultaneously plays both aggressor and victim roles. The assigned roles are based on a context. If the injected frequency of the aggressor oscillator is out of the lock range, the victim oscillator can be pulled and, if it is near the lock range, the victim will be quasi locked. By moving the frequency just beyond the lock range, the oscillator will be in a fast beat mode [8]. Measured spectra of these two modes are shown in Fig. 3. Based on calculations in [11], the spectrum is confirmed to be asymmetric and the sidebands on one side decay very rapidly. The power of the biggest injection pulling spur under a weak injection can be calculated as:

\[
P(\omega_{\text{spur}}) \approx \left( \frac{\omega_0}{4Q} \cdot \frac{I_{\text{inj}}^2}{I_{\text{osc}}^2} \cdot \frac{1}{\omega_m} \right)^2 \quad (2)
\]

For an injection signal far away from the lock range, the oscillator center frequency \(\omega_0\) may not pull much; however, it creates spurs of equal power around \(\omega_0\) with offset frequency of \(\omega_m\), with levels proportional to \(1/\omega_m^2\). We verify this equation for three different cases. In the first test, the oscillators are on the same die (see Fig. 2a). Then, the oscillators are separated by dicing the chip (with a saw) at its center (see Fig. 2b). Finally,
an additional grounded metal shield is inserted in-between to reduce electromagnetic coupling (see Fig. 2c). In this design, the ground and voltage supply lines of the two channels are completely separated on-chip and are connected outside at the PCB. Moreover, the supply and ground pads of two oscillators have enough distance in order to avoid coupling to each other through their wirebonds.

It is well known that the phase noise of an injection-locked oscillator can improve if locked to a clean source. Intuitively, the injecting source can correct the zero crossings of the oscillator at regular intervals, thus lowering the accumulated jitter [8]. Phase noise improvement depends on the injection source power as long as it is within the locking range. Fig. 4 shows the measured phase noise, while free running and in locked conditions, in two scenarios, i.e., (right) with the common substrate, and when the chip is diced and with the grounded shielding (left). Two interesting points can be observed when the coupling is reduced: first, the locking range is reduced and, second, the amount of improvement in the phase noise is also decreased. According to (1), as the measured lock range is proportional to the injection current \( I_{inj} \), which is proportional to the coupling strength, the coupling factor reduction is calculated to be 3. Fig. 5 shows the measured highest generated spur power versus the frequency difference between the aggressor and victim. It confirms the 6 dB/octave slope evident from eq. (2) and indicates that the substrate is the dominant coupling path. Coupling of the diced chips is reduced by \(~8\) dB. Moreover, by putting metal shield in-between, another \(~3\) dB of spur reduction is achieved, which shows that a significant, but non-dominant part of the coupling is electromagnetic. This agrees with the locking range method in Eq. (1): \( 20 \log_{10}(3) = 9.5 \) dB, which is quite close to the measured \( 8 + 3 = 11 \) dB. One might suspect that using a PLL around the oscillator can solve the pulling problem, but that would not be the case. As shown in [3], [9], based on s-domain modeling and measurements, the injection pulling has a band-pass response in the PLL the sideband magnitudes vary with the frequency offset of injection; their magnitudes approach zero for both very near to and far away from the center frequency, while having a peak in-between exhibiting a band-pass behavior. This is because the PLL suppresses the effect of pulling if \( (\omega_{inj} - \omega_0) \) is within the loop bandwidth and the oscillator pulling becomes less of an issue when \( (\omega_{inj} - \omega_0) \) is large. The situation is exacerbated when the injection source has a variable envelope modulation (output of a PA or its driver in case of a power modulation). In that scenario, there will be a parasitic frequency modulation, which degrades the spectral purity.

Table I shows the injected current calculated based on the measurements and using (2) for three different test cases. It is evident that in case of the common substrate, the injected current is much larger than in other cases. For example, comparing the common substrate with the one diced and shielded, the injected current is 4x smaller (which is close to the value calculated from the lock range, with the difference due to inaccuracy in estimating the exact value of the internal oscillator voltage swing and measuring the lock range since it is highly dependent on the biasing conditions).

### Table I

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<th>Spur frequency</th>
<th>Common</th>
<th>Diced</th>
<th>Diced and shielded</th>
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<td>10 MHz</td>
<td>72</td>
<td>29</td>
<td>20</td>
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The measurement results are also validated against a behavioral model suggested in [16]. Fig. 6a shows simulation results for circuit parameters of an oscillator shown later in Fig. 16 and the injected current of Table I, which is derived from (2). The simulated results are in agreement with the measured results in Fig. 5. To have an estimation on the oscillation center frequency shift \( (\omega_{\text{pulled}}) \) and the pulling-induced spur locations, we repeat here, for convenience, (11) and (23) from [11] as (3) and (4) below. They are verified with the model mentioned above.

\[
\omega_b = \sqrt{\frac{\omega_0^2}{2Q} \cdot \frac{I_{inj}}{I_{osc}}}^2
\]
where $\omega_p$ is the beat frequency.

$$\omega_{\text{pulled}} \approx \omega_0 + \frac{\omega_m}{2Q} \cdot \frac{I_{\text{inj}}}{I_{\text{osc}}} \cdot \frac{1}{\omega_m} \cdot 2$$

Injecting a current at frequency close to the lock range will put the oscillator in a fast beat mode, as in Fig. 3 and Fig. 6b (for simplicity, the injected current in this simulation is set larger than normally).

It is evident from these equations and simulations that if the injection current is larger, the oscillator center frequency would be pulled in stronger. As a result, the amplitude of oscillation will decrease since the tank impedance also decreases due to this frequency shifting. In addition, spur spacing will decrease, therefore the stronger injection current creates more closely spacing spurs. In summary, if the internal voltage (therefore the stronger injection current creates more closely this frequency shifting. In addition, spur spacing will decrease, since the tank impedance also decreases due to be pulled in stronger. As a result, the amplitude of oscillation (for simplicity, the injected current in this simulation is set larger than normally).

III. INJECTION PULLING MITIGATION METHODS

The previous section has demonstrated that the injection pulling produces strong unwanted spurs. There are well-known solutions attempting to reduce them. The most straightforward one is to reduce the coupling strength by increasing the physical distance between the strong aggressor and the sensitive victim and further isolating them with guard rings. Moreover, ground pickup connections can be used in between the two parts to absorb the interference. In addition, putting sensitive analog/RF parts in a deep N-well can be beneficial. These solutions, however, increase the chip fabrication cost, which is not desirable in high-volume consumer electronics.

Furthermore, multiple LC-tank oscillators will couple magnetically to each other. At the same time, an inductor present in the matching network of the last stage of a PA can also interact with other PAs or with the oscillators. Wire bondings of the adjacent critical pads can also magnetically couple. One solution to solve the magnetic coupling is to employ 8-shape inductors [17]. As reported in [18], 30 dB of magnetic coupling reduction could be achieved. However, other coupling paths remain unaffected in addition to a larger area and Q-factor degradation of the inductor. The third mechanism is through the interaction of the interconnects inside the chip as well as PCB traces that can capacitively couple to each other. The capacitive coupling should be reduced by a careful PCB layout design.

Considering the above experiments, analysis and examples, the injection pulling cannot be realistically solved through physical isolation or merely through the coupling strength reduction. Consequently, the pulling mitigation via architectural transformation must be sought instead.

A. Fractional Divider

The injection pulling has been traditionally mitigated by operating the oscillator at integer multiples of the output RF carrier. Unfortunately, that arrangement does not entirely eliminate the pulling since the PA harmonics still coincide with the oscillator center frequency. Another approach is to employ a fractional divider, which prevents the oscillator from both direct and harmonic pulling [19]–[22]. The fractional division could be achieved through a mixer following an oscillator [19]. It is then followed by a distribution network. However, this technique typically requires an LC band-pass filter or digital-calibration to suppress the lower side-band spurs. In [20] a further modification was introduced, called inductor-less LO distribution, that eliminates filtering of harmonics in LO path while not increasing the noise levels. However that technique uses complicated analog circuits and consumes large area. Unfortunately, generated harmonics from LO buffers and also the mixing of the oscillator harmonics and divider output is still a concern.

Another method to create the fractional frequency relationship is to use a frequency multiplier, $\times N$, following the oscillator, such that the PA harmonics would pull the oscillator. However, the generation of a quadrature output clock (e.g., required by the upconversion mixer) becomes more difficult. If, for example, poly-phase filters were to be used, high insertion loss and high power consumption would be a major disadvantage [23].

Third method is using a digital technique known as a phase rotation approach. This technique is well suited for scaled CMOS. It is more power and area efficient but could require some calibration. There are various such structures, e.g., a multi-modulus divider [24], but they are typically not suitable as they
must lie on the direct feedforward RF path leading to an antenna. Phase switching divider [21], [22], [25]–[27] belongs to another group of fractional dividers. It has fewer elements operating at the full clock rate. The circuit generates equidistant phases and then rotates selection between the different phases. Our proposed solution uses a reliable phase selection of the multiplexer. From the noise point of view, the choice of the phase generating circuit and multiplexer is of great importance. Previously reported pulling mitigation methods through a phase rotation introduce an excessive amount of noise since a number of devices is inserted in the RF feedforward path [21], [27]. For instance, [21] introduced a four-phase rotation in which each phase is divided by 5 using a Johnson counter (it contains 5 latches), whose output is sampled by the corresponding phase using a set-reset latch, each adding its own phase noise contribution. That might be acceptable for wireless connectivity applications but less so for cellular applications. In the next section, a low phase noise fractional divider will be introduced.

B. Frequency Planning

In this work, we propose a digital fractional divider architecture suitable for the pulling-free frequency planning scheme for multi-channel transmitters. Fig. 7 (top) shows the scenario in which the two oscillators operate at almost the same frequency\(^1\). Since the coupling strength is high, it leads to high spurious content in the spectrum of both oscillators. If two oscillators' center frequencies are separated, as per (2), the coupling effects will decrease, as shown in Fig. 7 (bottom). Since the output frequencies of the two channels need to be the same (on average), a non-integer (fractional) type divider should be used afterwards. Employing a fractional frequency divider, as shown in Fig. 8, is the proposed method here to prevent both the direct and harmonic PA pulling within and between the channels. As an example, consider a two-channel system with \(f_{TX} = 2\) GHz output. Employing an integer \(\pm 4\) divider leads to two oscillators with center frequencies at 8 GHz. However, using divide by \(N_1/M_1 = 3.5\) and \(N_2/M_2 = 4.5\) puts the center frequencies at \(f_{osc1} = 7\) GHz and \(f_{osc2} = 9\) GHz, which ensures enough separation, thus giving immunity to the injection pulling.

\(^1\)Their average frequencies could be identical but, for example, due to modulation, they could be a bit different at a given time instance.

IV. PROPOSED FRACTIONAL DIVIDER FOR PULLING MITIGATION

The reason for using an 8-phase rotation (\(\pm 4\) and then phase rotator) is as follows: the integer \(\div 2\) in Fig. 9a has a disadvantage of two oscillators operating at the same frequency, causing their strong mutual pulling. Second harmonic of the PA can also pull both oscillators. Using a higher integer division (\(\pm 4\) in Fig. 9b) is beneficial from the PA harmonic power perspective but it still exhibits another significant problem: the two oscillators’ center frequencies coincide, which can create their mutual injection pulling. Here, the fourth harmonic of the PA has lower energy than in Fig. 9a to pull the oscillators. However, the divider design could become difficult, although at this frequency inductors feature a higher Q-factor (at least at 65 nm and finer nodes) thus producing lower phase noise.

Another option would be using a \(\div 2\) followed by a 4-phase rotator (see Fig. 9c). Now, the two oscillators’ center frequencies are well separated by 2 GHz and are thus immune to pulling. However, one of the output of the \(\div 2\) divider could be 500 MHz away from the other oscillator, which could lead to pulling. Moreover, third harmonic of the \(\div 2\) divider can be placed again 500 MHz away from the oscillator. Another component comes from the second harmonics of the PA output, which places it 1 GHz away from both oscillators. Further disadvantage of this scheme is that one of the oscillators operates at 3 GHz, where the inductors are expected to have a lower Q-factor, thus worse phase noise performance. Fig. 9d shows the proposed method that uses a divide-by-4 followed by an 8-phase rotator. In this way, we reap all the aforementioned advantages and only third, fourth and fifth harmonics of the PA output are placed 1 GHz away from the oscillators, thus being sufficiently attenuated to be harmless.
well as between the outputs and the oscillators is no longer problematic. There will be the trade-offs of choosing different ratios employed in the fractional divider to accomplish the pulling mitigation. Using higher number of phases is beneficial for two reasons. First, more variety of fractional ratios can be achieved and, second, in nanoscale CMOS technologies, peak inductor $Q$-factors are pushed to higher frequencies. From the above reasoning, the design of a high purity oscillator favors higher division ratios. However due to matching non-idealities of this type of divider, higher division ratios could lead to more close-in fractional spurs which may violate the spectral mask. It also consumes more power. From the above reasoning, the $\div 4$ that generates 8 phases was chosen here as the optimal trade-off. Moreover, using a lower division ratio would place the oscillator center frequency closer to the PA harmonic, which makes it more prone to pulling again (e.g., here the 5 GHz spacing will reduce to 1 GHz with $\frac{1}{8}$.)

Fig. 11 shows internal waveforms when the Fig. 10 rotator is commanded to rotate its 8 phases counterclockwise (i.e., constant phase retarding). By picking a rising edge of the next retarded divider phase, the output clock edges lag, thus resulting in the period increase by $\frac{1}{8}$. The other rotator operates in the opposite direction.

System level block diagram and circuit details of the phase rotator are shown in Fig. 12a. The rail-to-rail CMOS $\div 4$ divider (see Fig. 12b) generates eight equidistant phases. Out of four different configurations, Fig. 12b(1) divider topology was chosen for its better noise performance and shorter propagation delay. Adding back-to-back inverters improves delay matching at the cost of small degradation in the phase noise. The rotating system contains a ring counter with set/reset to control the normal pass-through or the fractional division (see Fig. 12c). When 'set' is asserted, only one of the mux select signals will be active and it operates as a normal $\div 4$. If 'reset' is deasserted, logic '1' circulates in the ring counter and generates the proper selection signal. Edge-triggered D flip-flops retime the ring counter outputs for the appropriate edge selection. The 8:1 mux uses complementary pass-gates, whose eight outputs are wired-OR and the following internal buffer provides strong driving capability. As stressed above, to minimize the phase noise degradation of the output clock, extreme care must be taken to limit the device count on the feed-forward path to the absolute minimum (which was not done in [21]), thus putting all the signal processing complexity on the non-critical feedback path. According to simple equations, $\div 4$ dividers can generate additional divide ratios of 4.5 and 3.5: $T_{out1} = 4 \times \frac{9}{8} \times T_{osc1} = 4.5 \times T_{osc1}; T_{out2} = 4 \times \frac{7}{8} \times T_{osc2} = 3.5 \times T_{osc2}$.

In order to have a reliable selection (glitch-free) of the edges, the multiplexer select signal should come in the shaded area of Fig. 11. To guarantee this, consideration of the worst-case timing uncertainty is needed. The critical timing delay (see Fig. 12a) mainly comprises CLK-to-Q in the ring counter and CLK-to-Q delay for the retimer with enough setup time to have reliable selection in different process corners. In order to relax
the timing, an edge-triggered flip-flop was chosen that exhibits small setup and hold times. Taking into account these delays results in choosing the appropriate signal phase (P1–8) to retime the counter output to generate correct select signals for the multiplexer (S1–8).

A. Analysis of the mismatch

A disadvantage of the phase-rotating dividers is that they are sensitive to inherent mismatches and can generate significant spurs. Fig. 13 shows a four-phase rotation example (for the sake of simplicity) and the effect of the timing mismatch $\Delta T$ of one of its phases. The mismatch appears at the output every four cycles, therefore $f_{spur} = f_{out}/4$ (for the 8-phase rotation it would happen every 8 cycles).

It is possible to relate the maximum tolerable phase mismatch given the spurious-free dynamic range (SFDR) required at the output of the divider [28]. Another way to calculate the spur power is using Fourier series. In this paper we use the Fourier method similar to [28] and derive a formula for phase-switched dividers. We consider a random mismatch in each phase, rather than only in a single phase as in [28].

Fig. 14 continues with the four-phase rotation of Fig. 13 considering the timing mismatch $\Delta T$ in the single phase. By taking Fourier series of the waveform derived from the difference between ideal output and output with mismatch and performing a number of simplifications, Fourier series coefficient $b_k$ in (5) can be derived as:

$$b_k = \frac{4A}{\pi k} \sin\left(\frac{k\pi}{2(N + 1)}\right) \sin\left(\frac{k\pi \Delta T}{(N + 1)T_{old}}\right)$$

where $N$ (e.g., $N = 4, 8$) is the number of divider phases, $A$ is the amplitude, $T_{old}$ is specified in Fig. 11 and the $\pm$ sign is either $+$ for up-translation or $-$ for down-translation.
\[ S(t) = \sum_{k=1}^{\infty} b_k \cdot \sin \left( \frac{k \pi t}{(N \pm 1)T_{old}} \right) \]  

(6)

Fig. 14a plots the first six coefficients that are normalized to the carrier (note that \( k = 4 \) corresponds to the fundamental frequency), indicating harmonic distortion versus the timing mismatch in the single phase. By considering 0.5% mismatch in a single phase (e.g., \( T_{old} = 400 \) ps), plotting different harmonics reveals that some of them have a stronger level (see Fig. 14b). This is a simplified scenario, but in a practical case the mismatch will appear at each phase. Hence, this may increase the spur power at one frequency location (e.g., \( k = 6 \)), while the other locations (e.g., \( k = 2,3 \)) are reduced.

In order to see the net effect of mismatch in each phase at the output, statistical simulation with \( 10^6 \) points was employed. Each mismatch is a random variable with Gaussian distribution of \( \sigma = 2 \) ps. Results are shown in Fig. 14c for the two strongest spur levels. Fig. 15a shows the probability density function (PDF) of the fractional spurs with same statistical mismatches in each of \( N = 8 \) phases. Fig. 15b illustrates the effect of the random mismatches on the worst case spur level in two modes of the divider (divide by 9/8 and 7/8). These spur levels are typically non-essential when the fractional dividers are used in the feedback path of a frequency synthesizer [22], [29].

The presented divider is obviously not limited to the 3.5 and 4.5 division ratios. By further modifying the selection path, other division ratios can be achieved. Closer inspection of the waveforms reveals that equations such as \( T_{new} = T_{old} \times 2 + T_{old}/2 \) and \( T_{new} = T_{old} \times 2 + T_{old}/2 + T_{old}/8 \) can be derived (\( T_{old} \) and \( T_{new} \) were specified in Fig. 11), which give ratios of 10 and 5.25. Further investigating proves that ratios of 4.75, 6, 7, 8 and 9 can also be achieved.

It should be mentioned that besides the injection pulling mitigation, the fractional divider can be used to further extend the frequency range for multi-band radios. It should be noticed that based on (7), the location and the power of the divider output spurs can be estimated. For the \( \div N \) divide:

\[ S_{div}(t) = A \cdot \cos \left( \frac{2\pi f_{ct} t}{N} + \beta \cdot \sin \left( 2\pi f_{m} t \right) \right) \]  

(7)

where, \( S_{div}(t) \) is the first Fourier component of the clock after the division and \( \beta \) is the spur level modeled as FM with \( f_{c} \) being a center frequency and \( f_{m} \), a modulating frequency. The frequency of the carrier is divided by \( N \). However, the location of the spurs remains the same but its power in dB reduces by \( 20 \cdot \log(N) \).

In summary, the proposed techniques are applicable to single-chip radios by using the fractional divider between the oscillator and the (pre-)PA, as well as to multi-radio SoCs by operating such fractional dividers at different ratios in each path. In the latter case, the closest of the (pre-)PA output harmonics will be separated at least 1 GHz away from the oscillator. The resulting oscillator pulling will be very small, unlike in a conventional integer-N divider where some harmonics fall exactly on top of the oscillator thus leading to a strong pulling.

**V. EXPERIMENTAL VERIFICATION**

The two oscillators, whose schematic is shown in Fig. 16, operate in a modified high-swing class-C architecture inspired from [30], in which the tail current source in [31] is removed. Instead, an automatic amplitude control is introduced to settle the oscillation voltage swing at the maximum swing. Two transistors in the current control circuit (M3, M4) mirror the currents of the core transistors (M1, M2). These currents are summed up and then compared to a reference current, \( I_{ref} \). Then they are RC low-pass filtered to generate \( V_{ctrl} \), which is fed back to the oscillator core and biases the gates of ac-cross-coupled NMOS transistors. This forms a negative feedback loop to control the swing. In steady-state, the total dc current of the core is \( I_{ref} \) multiplied by the mirror ratio (i.e. \( (W/L)_{1,2} / (W/L)_{3,4} \) which is 4 in this implementation). Hence, the power consumption and the oscillation amplitude can be controlled by adjusting \( I_{ref} \).

The headroom-enhancing transformer introduced in [30] was
removed here in order to save area and improve $Q$-factor of the LC-tank. Instead, a standard center-tapped inductor is used together with a switched-cap varactor bank. The whole tank’s $Q$-factor is 16.

The two oscillators use overlapping tuning ranges (see Fig. 16, top). The first oscillator is tunable from 6.45 GHz to 8.5 GHz and the second from 7.15 GHz to 9.2 GHz. Thus, the measured tuning range of each oscillator is around 26%. Both oscillators have a 5-bit binary-weighted coarse MOM capacitor bank, a 2-bit fine MOM capacitor bank, and a linear varactor (used expediently in this chip only) for a continuous tuning range of 15 MHz. For reliability reasons, all the oscillator core transistors are thick oxide devices. The oscillator core area is 0.18 mm$^2$. An ac-coupled resistive-feedback inverter is cascaded with a digital inverter to drive a rail-to-rail CMOS $\div 4$ divider that generates the eight phases. The measured oscillator FoM at 3 MHz offset over the entire tuning range is 185 dB. Its phase noise is -143.6 dBc/Hz at 3 MHz offset from the divided 2 GHz output (see Fig. 17). Moreover, the noise floor measures -156 dBc/Hz and varies around 1 dB by activating the edge rotation. Simulation shows that the divide by 4 noise floor is about -160 dBc/Hz and the excess noise is coming from the rotator and output buffers. The measured current drain of each oscillator is 12 mA at 1.7 V, and 1.3 mA at 1.2 V for each resistive buffer. The estimated (i.e., mixture of measurements and simulations) current drain is 2.5 mA for the $\div 4$ divider and 0.5 mA for the 2 GHz 8-phase rotator, both at 1.2 V.

The injection pulling scheme has been successfully verified with RF performance satisfying the intended cellular basestation transmitter system. Fig. 18 demonstrates the proper functionality of the two fractional dividers by shortening the output period by 1/8 for the first channel (Fig. 18a: $4 \times f_{osc1} = \frac{8}{4} f_{osc1}$) and elongating it by 1/8 for the second channel (Fig. 18b: $4 \times f_{osc2} = \frac{8}{4} f_{osc2}$) when the rotators are engaged. The spurious tones due to the rotator timing mismatch are located at $k \cdot (f_{osc1}/4)/7$ for the up-translator and $k \cdot (f_{osc2}/4)/9$ for the down-translator, where $k$ is the spur harmonic number. For $f_{osc1} = f_{osc2} = 8$ GHz, the fundamental spur locations are 285.7 MHz and 222.22 MHz, respectively. The worst-case measured spurious tones are -42 dBc for the up-translation and -39 dBc for down-translation, which corresponds to around $\sigma = 2.5$ ps timing mismatch at each phase, based on the analysis of (5) with $N = 8$, which is illustrated in Fig. 15a and also in line with [28]. This spur level is acceptable for the intended operation in cellular basestation transmitters, which use large external cavity band-pass filters, but it could be reduced for other applications using an adaptive delay mismatch calibration [22]. Note that the new nanoscale CMOS technology nodes will further improve this mismatch.

Since the two oscillators are separated by only 200 $\mu$m, their mutual coupling is expected to be high. The next set of experiments quantifies it. We first set the center frequencies of both oscillators at 8 GHz, while measuring the spur level due to the injection pulling. Fig. 19 shows the relationship of the spur level vs. frequency offset, which follows the 6 dB/octave fit of eq. (2). With closer than 700 kHz separation (it will change with different injection power levels), the two oscillators

\[ \text{Spur (dB)} \approx -20 \times \log \left( \frac{f}{1 \text{MHz}} \right) - 23 \]

Fig. 19. Measured (a) injection-pulling spurs at the divider output versus separation of the two carriers; (b) spectrum of spurious tone (right); and near injection locking (left).
experience injection locking. Fig. 19b (left) plots a spectrum of one oscillator just before it gets injection locked. Fig. 19b (right) shows the generated spurs due to the injection pulling at a given spacing from the carrier frequency. In order to avoid the injection locking and to suppress the injection pulling in the normal system operation, the phase rotators can be activated at the same time, but in the opposite directions, thus separating the resonant frequencies by about 2 GHz. As desired, both outputs are again at the same frequency, although at different duty cycles, which is corrected up-stream in our intended system. However, the pulling is now almost non-existent due to large separation (28%) of the two resonating frequencies. Through extrapolation of the injection pulling equation given in Fig. 19a, the generated spur level would be insignificantly small below -80 dBc at the oscillator side and located 2 GHz away from the main carrier, which would anyway disappear in the second harmonic of the output.

Fig. 20 shows how the largest spur varies across the tuning range for both oscillators at three different supply voltages. It is clear that for the desired operating range with the nominal supply voltage of 1.2 V, there will be no timing violations. If an extended operation range is desired, putting the rotator at a lower supply voltage would be helpful. As indicated in Fig. 11. in order to have the best selection, the select signal should come in the shaded area (best at the center). Setup and hold timing violations of the retimer or the multiplexer will result in significant spurs as this happens at some frequencies in Fig. 20 when the divider supply is increased to 1.3 V. It should be emphasized that these spurs are located very far from the main carrier and they will be filtered out downstream. At mid frequency of 2 GHz, the supply voltage for both dividers is swept as shown in Fig. 21. Increasing the divider supply voltage improves the rising edges of the waveforms that reduces mismatches between the branches, hence improving the spurious level. Table II compares this fractional divider to prior published work. This divider features the highest frequency of operation at lowest power consumption and best noise performance.

### VI. Conclusion

In this paper, various coupling mechanisms and methods to mitigate them for the purpose of multi-core RF-SoC integration are studied and experimentally verified in a two-channel transmission sub-system realized in digital 65 nm CMOS. One of the consequences of the coupling is an injection pulling of an LC-tank oscillator, which creates unwanted spurs in the transmitted spectrum. Dicing the 2-channel silicon die to physically separate two oscillators shows that the coupling through the common substrate is the most dominant coupling mechanism. In order to solve the problem of injection pulling, we propose a fractional divider based on an 8-phase rotator. Inserting the rotator between the oscillator and a PA or PA driver in a 2-channel communication IC allows the oscillators to resonate at frequencies far away from each other (center frequencies separated by ~28%) and from the common output frequency. This way, the injection pulling effect on the generated spurs would be virtually eliminated. In order to meet the noise floor requirements of wireless transmitters, circuit complexity is put in the feedback path to relax the feedforward RF path. This produces a noise floor of only -156 dBc/Hz at ~2 GHz. This proves attractiveness and competitiveness of the digital RF approach, whose goal is to replace RF functions with high-speed digital logic gates.

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