Propagation probability and spread rates of self-sustained smouldering fires under controlled moisture content and bulk density conditions

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Abstract. The consumption of large areas of peat during wildfires is due to self-sustained smouldering fronts that can remain active for weeks. We studied the effect of peat moisture content and bulk density on the horizontal propagation of smouldering fire in laboratory-scale experiments. We used milled peat with moisture contents between 25 and 250\% (mass of water per mass of dry peat) and bulk densities between 50 and 150 kg m\(^{-3}\). An infrared camera monitored ignition, spread and extinction of each smouldering combustion front. Peats with a bulk density below 75 kg m\(^{-3}\) and a moisture content below 150\% self-sustained smouldering propagation for more than 12 cm. Peat with a bulk density of 150 kg m\(^{-3}\) could self-sustain smouldering propagation up to a critical moisture content of 115\%. A linear model estimated that increasing both moisture content and bulk density significantly reduced the median fire spread rate (which ranged between 1 and 5 cm h\(^{-1}\)). Moisture content had a stronger effect size on the spread rate than bulk density. However, the effect of bulk density on spread rate depends upon the moisture content, with the largest effect of bulk density at low moisture contents.

Additional keywords: fire behaviour, horizontal front, lateral, peat fire, peatland, propagation dynamics.

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Introduction

Smouldering is an incomplete form of combustion affecting organic materials such as the peat stored in peatlands and forest soils (Rein 2013). The propagation of smouldering fires is known to be very slow compared with flaming fires, moving at few centimetres per hour (Wein 1983; Frandsen 1991). The consumption of large areas of peat is often caused by self-sustained smouldering fires, which remain active and slowly propagating for weeks or months (Rein 2013).

During a peat fire, the carbon stored in the ground is released to the atmosphere. Incomplete smouldering combustion in peat produces a higher proportion of carbon emissions (e.g. CO, CH\(_4\)) than flaming fires in vegetation (Hadden 2011). These gases contribute significantly to global emissions of greenhouse gases (Turetsky et al. 2015). Smouldering peat fires also affect the roots of vegetation close to the surface, often causing lethal plant damage and habitat losses (Miyaniishi and Johnson 2002; Page et al. 2002; Davies et al. 2013). The landscape after a peat fire is often heterogeneous, as peat is consumed in irregular patches (Shetler et al. 2008). In the burnt areas, deep layers of dense peat become the new surface, with a different constitution and properties (Prat-Guitart et al. 2011). These post-burn surfaces are often opportunities for colonising species and have the potential to change biodiversity (Benscoter and Vitt 2008).

Factors driving smouldering fire ignition

The ignition of a smouldering fire in peat is often caused by a heat source near the surface, such as a lighting strike, adjacent flaming vegetation (Rein 2013) or burning pine cones (Kreye et al. 2013). The start of a smouldering fire is controlled by the properties of the ignition source (intensity and duration), peat conditions (primarily moisture content, bulk density and mineral content) and oxygen availability (Frandsen 1987; Ohlemiller 2002; Hadden et al. 2013; Huang and Rein 2014). Of these, peat moisture content is the main factor limiting the ignition of peat (Van Wagner 1972; Frandsen 1987, 1991). Water in peat acts as a heat sink, requiring a large amount of energy to evaporate the water before the peat reaches...
temperatures at which the pyrolysis process begins (Rein 2013). The probability of peat ignition and initial horizontal propagation of at least 10 cm from an ignition source has been estimated in previous studies (Frandsen 1997; Lawson et al. 1997; Reardon et al. 2007). When the moisture content (MC) of the peat is between 110 and 200% (gravimetric moisture content, mass of water per mass of dry peat expressed as a percentage), there is a 50% probability of starting a smouldering peat fire (Frandsen 1987; Frandsen 1997; Reardon et al. 2007; Rein et al. 2008). Frandsen (1997) predicted the probability of ignition and early horizontal propagation as a function of MC (%), mineral content (%) and bulk density (kg m$^{-3}$). Reardon et al. (2007), however, predicted the ignition and early propagation using only moisture and mineral content, suggesting that bulk density was implicitly included in the quantification of the other two peat properties.

Self-sustained smouldering propagation

Once ignited, a smouldering fire propagates by drying and igniting the fuel ahead of the smouldering front (Frandsen 1997; Huang et al. 2015). In smouldering combustion, peat particles undergo endothermic pyrolysis, forming char, also known as regime I, followed by exothermic oxidation reactions where char is converted to ash, regime II (Hadden et al. 2013; Huang et al. 2015). The energy released during the exothermal oxidations is transferred to the surrounding environment, some being radiated to the atmosphere and some conducted to the peat particles ahead of the smouldering front. If the combustion of peat particles in the smouldering front produces sufficient energy to overcome the heat losses to the surroundings, the smouldering front spreads away from the ignition point and becomes an independent self-sustained front (Ohlemiller 1985). A smouldering front can then propagate into the peat both vertically and horizontally. However, it is the front propagating horizontally that is primarily responsible for the large areas of peat consumed, as vertical propagation is generally extinguished by deeper layers of wet peat (Wein 1983; Miyanishi and Johnson 2002; Usup et al. 2004). The propagation mechanisms of smouldering fires in peats are complex and further research is needed to understand how peat conditions affect the dynamics of self-sustained fire propagation.

In this paper, we analyse the horizontal propagation dynamics of smouldering fires moving away from an ignition source under a range of controlled moisture content and bulk density conditions. We use $\beta$ regressions to estimate the propagation distance as a function of moisture content and bulk density. We also estimate the spread rate of the fire when self-sustained smouldering propagation was observed. Finally, we use a linear model to relate the properties of the peat to the spread rate of smouldering fires. The purpose of this experimental research is to enable key peat conditions (moisture content and bulk density) that influence smouldering propagation to be understood.

Materials and methods

Experimental set-up

Laboratory smouldering experiments were designed to control environmental and peat conditions. Commercial milled peat (Shamrock Irish Moss Peat, Bord Na Móna, Newbridge, Republic of Ireland) was used to be consistent with previous studies (Belcher et al. 2010; Hadden et al. 2013) and because commercially milled peat reduces extraneous sources of variation due to its homogeneous properties (Frandsen 1987, 1991; Zacccone et al. 2014; Prat et al. 2015). The peat was placed in a 22 × 18 × 6-cm insulated burnbox made of fibreboard with a thermal conductivity of 0.07–0.11 W m$^{-1}$ K$^{-1}$, similar to that of peat (Frandsen 1987, 1991; Benscoter et al. 2011; Garlough and Keyes 2011). Peats were oven-dried at 80°C for 48 h. Water was added to the dry peat until the required MC was achieved. The moist peat was sealed in a plastic bag for 24 h before the experiment to allow equilibration. The prepared peats had 25, 100, 150, 200 and 250% MC. This range of moisture contents represents peat conditions that are susceptible to smouldering ignition (Frandsen 1987; Rein et al. 2008; Benscoter et al. 2011).

A range of peat bulk densities (ρ, dry mass of peat per unit volume of wet peat) was included in our experimental data. Two bulk density treatments ($BD_1$, $BD_2$) were created for each moisture content: (1) the peat was spread into the burnbox until it filled the volume ($BD_1$); and (2) the peat was compressed into the burnbox until it filled the volume ($BD_2$). This second treatment increased bulk density by reducing the bulk volume and the air spaces inside the sample. The range of ρ obtained was representative of peat and duff from boreal and temperate peatlands (Frandsen 1997; Benscoter et al. 2011; Wellock et al. 2011; Davies et al. 2013; Thompson and Waddington 2014).

An electric igniter coil was situated along one side of the burnbox and used to ignite a 2-cm-wide section of dry peat (~0% MC). The coil delivered 100 W for 30 min, similar to the heat provided by surface burning vegetation (Rein et al. 2008). This ignition protocol was sufficient to start a smouldering front in the dry peat section, which then attempted to spread to the adjacent peat sample. An infrared camera (ThermaCAM SC640, FLIR Systems, Wilsonville, OR) was used to image the radiative energy flux from the smouldering peat surface (Prat-Guitart et al. 2015). The position of the smouldering front was identified using the infrared images, which provided information at a resolution of 0.05 × 0.05 cm (one pixel). The camera took images every minute, creating sequences of between 300 and 700 images for each burn test. Experiments for each combination of MC and bulk density treatment were replicated four times. Moisture evaporation from the peat was negligible in the absence of a smouldering front (Table S1 in the supplementary material, available online). We therefore assumed that moisture content of unburnt peat well ahead of the smouldering front was constant throughout the duration of the burning experiments.

Self-propagation distance of peat fires

Once the fire self-extinguished, we recorded the final distance ($D$) of the smouldering front from the igniter. A value between 0 and 1 indicated the fraction ($y$) of peat consumed along a transect across the width of the burnbox at distance $D$ from the igniter. These fractions were transformed to avoid zeros and ones by

$$y = \frac{(yN - 1) + 1/2}{N},$$

where $N$ is the sample size (Smithson and Verkuilen 2006). Beta regressions were used to estimate the association of $y_D$ with the peat bulk density $\rho$ (kg m$^{-3}$) and
moisture content \( MC \) with a logit link function for the expectation of \( y_D \) given by:

\[
P_{yD} = \frac{1}{1 + \exp(-\beta_D + \beta_{D1}D + \beta_{D2}MC))} \tag{1}
\]

where \( \beta_D \)s are the regression coefficients. A total of seven \( \beta \) regressions were fitted for values of \( D \) at 6, 8, 10, 12, 14, 16 and 18 cm. Each regression was a different analysis to avoid autocorrelation of residuals. A \( \beta \) regression can be viewed as a flexible form of logistic regression that allows for a continuous response variable (modelled by \( \beta \) distribution) and skew in the response distribution (modelled by the precision parameter of \( \beta \) distribution) (Cribari-Neto and Zeileis 2010). Similarly to our \( \beta \) regressions, logistic regressions were used in past studies with success or failure data to estimate the probability of peat ignition and early propagation 10 cm away from the ignition region (Frandsen 1997; Lawson et al. 1997; Reardon et al. 2007).

**Image processing**

The infrared images were corrected for the distortion caused by the angle of the infrared camera. The burnbox surface area was represented by \( \sim 150,000 \) pixels, each of them giving information about the dynamics of the smouldering front during the experiment. For every pixel, we built a profile of the radiated energy flux throughout the duration of the burn (Prat-Guitart et al. 2015). The radiative energy flux increased when an approaching smouldering front heated the area, indicating that the peat was being dried before the start of the combustion processes, pyrolysis and oxidation. The start of the smouldering combustion \( (t^s) \) was defined as the time a pixel’s radiative energy flux reached a rate of 10 \( \text{W m}^{-2} \text{min}^{-1} \) or more. For every experiment, we obtained a matrix of \( t^s \) giving the time when the leading edge of the smouldering front reached each pixel.

As a method to prevent boundary effects from the burnbox edges to the smouldering front, 2 cm of pixels close to the sides were removed from each image. The pixels from the 6 cm closest to the igniter were also excluded to avoid effects of the ignition heating coil. The area of pixels left, \( \sim 60\% \) of the burnbox surface, was used for the subsequent image analysis and estimation of the spread rates. Image processing was undertaken using *Matlab* and the *Image Processing Toolbox* (version R2012b 8.0.0.783, MathWorks Inc., Natick, MA).

**Estimation of horizontal spread rates**

For each burn, we split the \( t^s \) matrix into subregions of \( 2 \times 2 \) cm. We then estimated the spread rate and direction of spread for each subregion by fitting a generalised least-squares model, assuming a linear smouldering front across the subregion. This approach allows all the data within a subregion to inform our estimates of spread rate and direction. The fitted model is:

\[
t^s_i = \beta_{y0} + \beta_x x_i + \beta_y y_i + e_i \tag{2}
\]

\[
e_i \sim N(0, \sigma^2 A)
\]

where \( x \) and \( y \) are the position of the \( i^r \) pixel within a subregion. The coefficients \( \beta_x \) and \( \beta_y \) give the rate at which \( t^s \) increases per unit increase in \( x \) and \( y \) respectively; \( e_i \) is the error term assumed to be normal-distributed with mean zero and with variance-covariance matrix \( \sigma^2 A \). The spatial correlation structure of \( A \) was described with a Gaussian semivariogram (Pinheiro and Bates 2000). The model was fitted using a maximum likelihood. The spread rate of the leading front in the \( x \) direction was then estimated as:

\[
S = \frac{1}{\beta_x} \Delta x \tag{3}
\]

where \( S \) is the subregion spread rate and \( \Delta x \) is the length of a pixel (typically 0.05 cm). A spread rate was estimated for each subregion of the burnbox and then a median spread rate \( (\bar{S}) \) and median absolute deviation were estimated for each experimental burn.

We looked for detectable changes in spread rate during the long burns (burns lasting more than 7 h). We tested the constancy of the smouldering spread rate away from the igniter \( (x \) direction) across the entire burnbox by regressing the median time taken for the smouldering front to reach a pixel against linear and quadratic terms in the distance from the igniter (see supplementary material). The quadratic term is expected to be zero if spread rate is constant. For each treatment, the significance of the quadratic term was tested using the \( F \) test.

**Effect of moisture content and bulk density on the spread rate**

The effects of \( MC \) and \( \rho \) on \( \bar{S} \) were examined using a linear model. Even though the bulk density of the peat was based on a compression treatment \( (BD_1 \) and \( BD_2 \), we took bulk density to be a continuous variable. The two explanatory variables were standardised (by subtracting the mean and dividing by the standard deviation). Spread rates were log-transformed so that model residuals were close to normality. Forward stepwise model selection was used to arrive at a best-fit model that minimised the Akaike information criterion, AIC (Burnham and Anderson 2002). Only the model with the lowest AIC is reported in the results (Eqn 4):

\[
\log(\bar{S}) = \beta_0 + \beta_1 MCk + \beta_2 \rho_k + \beta_3 MCk \times \rho_k + e_k \tag{4}
\]

where \( \bar{S} \) is the median spread rate of each burn \( k \), \( \beta_{0k}, \beta_1, \beta_2 \) and \( \beta_3 \) are the coefficients of the dependent parameters and \( e_k \) is the residuals assumed to be normally distributed. The data analyses were done with *R* project statistical software (version 3.0.2, R Core Team 2013), the *betareg* package (Cribari-Neto and Zeileis 2010) the *ape* package (Paradis et al. 2004) and the *nlme* package (Pinheiro et al. 2015).

**Results**

The milled peats used had an intrinsic bulk density between 50 to 150 kg m\(^{-3}\) (Fig. 1). Each \( MC \) treatment had a range of bulk densities. Peats with low moisture content tended to have higher bulk densities than peats with high moisture content (Spearman correlation \( -0.4 \), \( P \) value 0.02).

The smouldering front always self-propagated across the entire box (20 cm) when the moisture content was 25 or 100% (Fig. 2). At these moisture contents, the smouldering fire was observed to propagate as a single linear front. The smouldering
front always self-extinguished before reaching the end of the burnbox in peats of 200 and 250% MC. The fronts that self-extinguished were irregular for the last 1–2 cm of propagation. Peats with 150% MC had intermediate behaviour, with fronts self-extinguishing in 75% of the experimental burns (Fig. 2a). Peats with 200 and 250% MC did not self-sustain propagation in cases with high bulk density. Only peats with 100% MC (low and high bulk density) and peats with 150% MC and low bulk density sustained smouldering for more than 7 h. For these long burns, we found no evidence that the spread rate was changing across the burnbox, as indicated by the non-significant quadratic term for each of the peat conditions (F tests for peats with 100% MC and low bulk density $F_{1,48} = 1.2, P = 0.28$; 100% and high bulk density $F_{1,49} = 2.9, P = 0.09$; and 150% MC $F_{1,31} = 2.0, P = 0.17$).

Expected self-propagation distances from an ignition source
Peats at low moisture content were more likely to sustain smouldering propagation for a longer distance independently of the peat density (Fig. 3). For example, at $D = 12$ cm, peats with 25 and 100% MC had an expected fraction of peat burnt ($P_{e,D}$) of 0.72. At short distances (between 6 and 10 cm from the ignition region), $P_{e,D}$ was associated with both the moisture content and the bulk density of the peat (Table 1), whereas $P_{e,D}$ at longer distances ($\geq 12$ cm from an ignition area) were mainly controlled by the moisture content of the peat (Table 1, $D = 12$ cm, Fig. S1).

Effect of peat condition on the smouldering spread rates
The spread rates estimated per subregion, $S$, ranged between 0.6 and 9.1 cm h$^{-1}$ (Table 2). Owing to self-extinction of the fire, experimental burns with moisture contents of 150, 200, 250% MC had a lower number of subregions where $S$ could be estimated.

The best-fit model is shown in Table 3. The spread rates, $S$, were well explained by the model ($R^2 = 0.77$). There was a significant effect of $MC$ and $\rho$ on the spread rates of smouldering fires, where the continuous increase of $MC$ had a stronger effect on the spread rates than the increase of $\rho$ (Fig. 4). The interaction term was also significant, indicating that for low $MC$, the change in $\rho$ had a small impact on the spread rates. However, the decrease of spread rates due to the increase of $\rho$ was stronger with higher $MC$ (e.g. $-0.015 \pm 0.005$ cm kg$^{-1}$ m$^{-3}$ h$^{-1}$ for peats with 25% MC and $-0.022 \pm 0.009$ cm kg$^{-1}$ m$^{-3}$ h$^{-1}$ for peats with 100% MC).

Discussion
Our results indicate that peat moisture content is the main factor predicting the self-sustained propagation of peat fires. High peat bulk density increases the effect of moisture content on the dynamics of smouldering propagation. Peats $\leq 100$% MC had a 70% probability of self-sustaining propagation beyond the initial 12 cm ($P_{s,D} \leq 0.72$). Under these conditions, oxidation reactions along the smouldering fronts produced sufficient energy to overcome heat losses, dry the peat and ensure

Fig. 1. Bulk density of the peat samples as a function of moisture content. Circles are peat samples with bulk density treatment $BD_1$, and triangles are peats treated with bulk density $BD_2$.

Fig. 2. Time taken by the smouldering front ($t_L$) to self-propagate through the peat sample until self-extinction. Circle, triangle, square, diamond and star correspond to 25, 100, 150, 200 and 250% moisture content respectively. (a) Uncompressed peats (treatment $BD_1$); and (b) compressed peats (treatment $BD_2$). Standard errors of the means are smaller than the symbol size. Lines are linear-regression fits. Only moisture contents where self-sustained smouldering propagation occurred are plotted.
Peats above 150% MC had a high probability of extinction after propagating through 12 cm of peat. This suggests that when the moisture content is higher than 150%, the amount of energy required to evaporate water ahead of the smouldering front is too high for propagation to be self-sustained for more than 12 cm. For distances of ≥12 cm, we found no effect of bulk density on propagation (Table 1). This could be because (i) the bulk density does not affect the fraction of peat burnt at $D \geq 12$ cm, suggesting that moisture content of the peat is the main predictor of $P_{1D}$, or (ii) there is an effect of bulk density on $P_{1D}$ when $D \geq 12$ cm but our data have limited power to detect this effect. To increase the power to detect effects of bulk density, future research should consider a larger sample size and greater variety of moisture content and bulk density treatments within the range tested.

The estimated $P_{1D}$ smouldering propagation for distances up to 10 cm from an ignition source is comparable with the probability of ignition and early propagation estimated in previous studies on natural peat soils (Frandsen 1997; Lawson et al. 1997; Reardon et al. 2007). In those studies, the 50% probability of ignition and 10-cm propagation had a moisture content threshold of 120% MC for *Sphagnum* and feather moss peats with bulk densities between 20 and 60 kg m$^{-3}$ and mineral contents below 30% (mass of mineral content per total mass of dry peat) (Frandsen 1997). In our analysis, peats below 160% MC and similar bulk densities have a $P_{1D} = 0.5$ at $D = 12$ cm, indicating that there is a 50% probability of self-sustained smouldering for more than 12 cm (Fig. 2). However, denser peats with 130 kg m$^{-3}$ have a $P_{1D} = 0.5$ at $D = 10$ cm only when the peat moisture content is below 113% MC (Fig. 3). Using milled peats, Frandsen (1987) established a comparable threshold for peat ignition and early propagation of 110% MC and bulk density of 130 kg m$^{-3}$.

Compared with peats with low bulk density, the peats with high bulk density produce more energy owing to the oxidation of a greater mass of peat particles (Ohlemiller 1985). However, the modification of bulk density through compression implies that high-bulk-density peats hold a larger mass of water per unit volume. For a successful self-propagation, all this water needs to be evaporated before combustion. These conditions cause slower spread rates and shorter propagation distances (Ohlemiller 2002; Belcher et al. 2010; Hadden et al. 2013). The effect of oxygen

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**Fig. 3.** Expected fraction of peat burnt ($P_{1D}$) to a distance $D$ away from the ignition region. $D$ values of 6, 8, 10 and 12 cm are shown; results from $D = 14$, 16 and 18 cm are similar to $D = 12$ cm (Table 1). Panels are for (a) 25%; (b) 100%; (c) 150%; (d) 200%; and (e) 250% moisture content. Symbols represent fractions of peat burnt ($y$) along a transect at distance $D$. 

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The spread rate in peats with high bulk density and low moisture contents (i.e. 25, 100% MC) is not affected as much as in peats with high moisture contents (i.e. 150–250% MC). Peats with high moisture content and high bulk density have a reduced rate of O$_2$ diffusion and a larger amount of water to be evaporated before combustion. These conditions cause slower spread rates and shorter propagation distances (Ohlemiller 2002; Belcher et al. 2010; Hadden et al. 2013). The effect of oxygen...
Table 1. Coefficient estimates from $\beta$ of peat burnt ($P_{s,0}$) at each distance ($D$) from the igniter (Eqn 1)

<table>
<thead>
<tr>
<th>$D$ (cm)</th>
<th>$\beta_0$</th>
<th>$\beta_2$ ($\rho$)</th>
<th>$\beta_0$ (MC)</th>
<th>Phi</th>
<th>Log-like</th>
<th>$R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>6.53 ± 1.18</td>
<td>*** -0.032 ± 0.008</td>
<td>*** -0.018 ± 0.003</td>
<td>*** 1.53 ± 0.38</td>
<td>*** 57.11</td>
<td>0.71</td>
</tr>
<tr>
<td>8</td>
<td>6.81 ± 1.19</td>
<td>*** -0.034 ± 0.008</td>
<td>*** -0.021 ± 0.003</td>
<td>*** 1.52 ± 0.37</td>
<td>*** 56.98</td>
<td>0.77</td>
</tr>
<tr>
<td>10</td>
<td>4.79 ± 1.16</td>
<td>*** -0.021 ± 0.008</td>
<td>** -0.018 ± 0.003</td>
<td>*** 1.09 ± 0.25</td>
<td>*** 53.36</td>
<td>0.68</td>
</tr>
<tr>
<td>12</td>
<td>3.23 ± 1.09</td>
<td>** -0.008 ± 0.008</td>
<td>&amp; -0.018 ± 0.003</td>
<td>*** 1.16 ± 0.26</td>
<td>*** 54.01</td>
<td>0.71</td>
</tr>
<tr>
<td>14</td>
<td>3.23 ± 1.09</td>
<td>** -0.008 ± 0.008</td>
<td>&amp; -0.018 ± 0.003</td>
<td>*** 1.16 ± 0.26</td>
<td>*** 54.01</td>
<td>0.71</td>
</tr>
<tr>
<td>16</td>
<td>3.23 ± 1.09</td>
<td>** -0.008 ± 0.008</td>
<td>&amp; -0.018 ± 0.003</td>
<td>*** 1.16 ± 0.26</td>
<td>*** 54.01</td>
<td>0.71</td>
</tr>
<tr>
<td>18</td>
<td>2.79 ± 1.09</td>
<td>* -0.003 ± 0.008</td>
<td>&amp; -0.018 ± 0.003</td>
<td>*** 1.22 ± 0.28</td>
<td>*** 53.07</td>
<td>0.73</td>
</tr>
</tbody>
</table>

MC is the moisture content, BD is the bulk density treatment, $\rho$ is the mean bulk density (±standard deviation). Wald test $P$ value significance has been added to the coefficients where *** < 0.001; **, 0.01; *, 0.05. Phi is the model precision, Log-like is the model log-likelihood and $R^2$ is the pseudo $R$-squared.

Table 2. Estimated spread rates of the experimental smouldering fires

<table>
<thead>
<tr>
<th>MC (%)</th>
<th>BD</th>
<th>$\rho$ (kg m$^{-3}$)</th>
<th>Num. burns</th>
<th>Num. subregions</th>
<th>$S$ min–max (cm h$^{-1}$)</th>
<th>$\bar{S}$ (cm h$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>25</td>
<td>$BD_{D_2}$</td>
<td>116 ± 9</td>
<td>4</td>
<td>191</td>
<td>2.3–7.2</td>
<td>4.33 ± 0.91</td>
</tr>
<tr>
<td>100</td>
<td>$BD_{D_1}$</td>
<td>80 ± 7</td>
<td>4</td>
<td>178</td>
<td>1.0–7.8</td>
<td>2.63 ± 1.08</td>
</tr>
<tr>
<td>150</td>
<td>$BD_{D_1}$</td>
<td>62 ± 9</td>
<td>4</td>
<td>96</td>
<td>1.0–4.8</td>
<td>2.07 ± 0.59</td>
</tr>
<tr>
<td>200</td>
<td>$BD_{D_1}$</td>
<td>60 ± 10</td>
<td>4</td>
<td>45</td>
<td>1.2–5.2</td>
<td>2.16 ± 0.62</td>
</tr>
<tr>
<td>250</td>
<td>$BD_{D_1}$</td>
<td>71 ± 9</td>
<td>3</td>
<td>6</td>
<td>1.0–2.2</td>
<td>1.42 ± 0.43</td>
</tr>
<tr>
<td>25</td>
<td>$BD_{D_2}$</td>
<td>141 ± 5</td>
<td>3</td>
<td>147</td>
<td>1.5–6.2</td>
<td>2.86 ± 0.75</td>
</tr>
<tr>
<td>100</td>
<td>$BD_{D_2}$</td>
<td>80 ± 8</td>
<td>4</td>
<td>179</td>
<td>0.6–9.1</td>
<td>1.71 ± 0.90</td>
</tr>
<tr>
<td>150</td>
<td>$BD_{D_2}$</td>
<td>111 ± 8</td>
<td>3</td>
<td>13</td>
<td>0.7–1.9</td>
<td>1.23 ± 0.45</td>
</tr>
<tr>
<td>200</td>
<td>$BD_{D_2}$</td>
<td>124 ± 11</td>
<td>3</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>250</td>
<td>$BD_{D_2}$</td>
<td>114 ± 3</td>
<td>3</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

Table 3. Best-fit linear model for median spread rates ($\bar{S}$)

<table>
<thead>
<tr>
<th>Estimate</th>
<th>Standard error</th>
<th>$P$ value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta_0$ (Intercept)</td>
<td>0.514</td>
<td>0.056</td>
</tr>
<tr>
<td>$\beta_1$ (MC)</td>
<td>-0.545</td>
<td>0.061</td>
</tr>
<tr>
<td>$\beta_2$ ($\rho$)</td>
<td>-0.325</td>
<td>0.058</td>
</tr>
<tr>
<td>$\beta_3$ (MC $\times$ $\rho$)</td>
<td>0.151</td>
<td>0.046</td>
</tr>
</tbody>
</table>

The spread rate of the smouldering fronts was analysed for the first time as a function of peat conditions. The effects of moisture content and bulk density on spread rates are consistent with the estimates of energy required to dry and heat the peat (estimated energy required to start thermal decomposition of peat for each peat moisture content and bulk density treatment is shown in Fig. S2 and Fig. S3). A greater mass of water per unit volume requires more energy to evaporate and start combustion (Fig. S2). However, peats with 100% MC and bulk density below 100 kg m$^{-3}$ have a higher energy demand and the fire propagated more slowly than in peats with 150 and 200% MC and bulk density below 75 kg m$^{-3}$ (Fig. S3). For a given moisture content, there is more energy needed to carry on smouldering combustion when the bulk density increases (Fig. S3). Increasing peat’s bulk density, there is a larger energy production during the oxidation of the larger mass of peat. However, this energy produced is less than the energy necessary to evaporate the water in the peat. As a consequence, the spread rate of the fire is slower or not self-sustained (Fig. 4).

Controlled smouldering tests

It should be noted that our experiments were at a laboratory scale and peat conditions were controlled. Therefore, caution should be taken when using our results at the field scale. The peat conditions (i.e. bulk density, mineral content, peat composition) can be very heterogeneous in real ecosystems (McMahon et al. 1980). Our laboratory-scale experiments intentionally removed these sources of variation. This allowed us to focus on the effect of two important peat conditions (moisture content and the bulk density) on the smouldering propagation dynamics.

Our burnbox size was designed to be suitable for the study of horizontal propagation across greater distances than in previous studies (Frandsen 1987; Frandsen 1997; Reardon et al. 2007), enhancing our understanding of propagation in larger sample.
sizes. The duration of our experiment and the size were limited by a maximum burn duration of 12 h in order to minimise the effect of diurnal variation in ambient temperature and humidity. The spread rates and the expected fractions of peat burnt were both estimated assuming constant moisture content and bulk density throughout the duration of an experiment. During our experiments, there were no moisture content changes that could have a substantial effect on the smouldering fire propagation (Table S1). However, substantial changes of moisture content or bulk density during the experiment duration could cause variation in the estimated spread rates with the distance.

The ignition of the peat along one side of the burnbox enabled a linear propagation of smouldering fronts moving perpendicularly to the igniter coil. This ignition method was developed to estimate spread rates from infrared images that assume linear propagation (Prat-Guitart et al. 2015). A depth of only 5 cm of peat was used in the present study to focus solely on horizontal smouldering propagation, avoiding vertical spread of the smouldering front and limiting the multidimensional spread of a peat fire. Previous experimental studies have examined peat ignition in deeper samples (Rein et al. 2008; Benscoter et al. 2011). However, deeper peat samples had smouldering fronts propagating horizontally and vertically, making the study of propagation dynamics more complex. The properties of the burnbox material created similar thermal insulation as if the peat sample were surrounded by more peat (Frandsen 1987, 1991; Benscoter et al. 2011; Garlough and Keyes 2011). In these insulated conditions, a sample depth of 5 cm has a small impact on our results and they can be compared with other experiments looking at horizontal propagation in bigger samples.

**Application to peatland fires**

In this study, the smouldering dynamics were studied in an area of $22 \times 18$ cm with homogeneous moisture content conditions, comparable with the size of a dry patch of peat moss (Petrone et al. 2004). In peatlands, the moisture content of the surface peat layers is regulated by the distribution of moss species and the position of the water table (Thompson and Waddington 2013b; Waddington et al. 2015). A heterogeneous distribution of *Sphagnum* mosses is likely to cause a heterogeneous spatial distribution of peat moisture content, creating patches of 20–50-cm diameter (Benscoter and Wieder 2003; Petrone et al. 2004). During drought, the surface layer dries owing to lack of rain, which may then be followed by a lowering of the water table (Chivers et al. 2009; Sherwood et al. 2013; Kettridge et al. 2015). In such circumstances, dry peats in the surface layers have less than 250% moisture content (Benscoter et al. 2011; Terrier et al. 2014; Lukenbach et al. 2015), thus being vulnerable to peat fires.

After a peat fire, the new surface layer is closer to the water table and consequently has a reduced fire danger. Previous studies suggested that peat fires are common in peatland ecosystem cycles (Turetsky et al. 2002). The consumption of surface layers of peat reduces the accumulation of organic material, allowing *Sphagnum* mosses to access the water table, being less dependent on external water inputs (Benscoter and Vitt 2008). Post-fire surfaces also enable the roots of
vegetation to take up ground water and nutrients from deep mineral layers.

In peatlands, peat bulk density strongly depends on the vegetation cover and temporal changes in the water table behaviour (Davies et al. 2013; Sherwood et al. 2013; Thompson and Waddington 2013a). Deep peat layers often have a higher degree of decomposition and a higher bulk density compared with surface layers (Benscoter et al. 2011; Thompson and Waddington 2014). Following turf-cutting in drained peatlands, new dense and dry layers of bare peat become exposed at the surface and are vulnerable to peat fires.

Peats with 25% MC were included in the analysis to have a representation of very dry peats in our sample. However, such dry peats are uncommon in natural peatlands (Terrier et al. 2014; Lukenbach et al. 2015), being restricted to the surface of drained peatlands under extreme drought. In the present study, bulk density was experimentally manipulated using two peat compression treatments, which produced a range of bulk densities. Dry peats (25% MC) were only experimentally tested with high bulk densities between 108 and 145 kg m⁻³. The high bulk density of 25%MC peats is due in part to the structure of milled peats and the low expansion of peat particles when a small quantity of water is added to the peat sample (Huang and Rein 2015). The reduced expansion of the dry peat (25% MC) compared with the greater expansion of relatively wetter peat (≥100%MC) caused the negative collinearity between moisture content and bulk density. If we exclude peats with 25% MC, we find no collinearity between MC and ρ (Spearman correlation −0.07, P value 0.7). Therefore, the negative collinearity between MC and ρ (Fig. 1) is caused by the peats with 25% MC. This collinearity could contribute to the interaction reported in the spread rate model (Table 3) and affect extrapolated predictions of spread rates (Dormann et al. 2013). The same spread rate model but excluding peats with 25% MC had similar β₀, β₁ (MC) and β₂ (ρ) coefficients but no significant interaction term. Therefore, the main effects of moisture content and bulk density on the spread rates are qualitatively not affected by the collinearity.

All the milled peats used in the present study had a low mineral content of less than 5%. Natural peats are characterised as having less than 20–35% mineral content (Turetsky et al. 2015) and often <6% (Benscoter et al. 2011). Previous studies have suggested that large quantities of mineral content could reduce the probability of peat ignition and posterior fire propagation (Frandsen 1987; Hungerford et al. 1995). Our peats had an intrinsic mineral content of 2.6 ± 0.2%, similar to the 3.7% of Frandsen’s (1987) peats. This implies that our low-mineral-content peats would give an upper limit on the spread rates and propagation distance. However, small quantities of certain minerals such as salts of calcium or magnesium, common in plant material and soil, have been shown to have no effect on propagation (Benscoter et al. 2011) or rather enhance heat conduction in the fuel media that could help the smouldering propagate faster (Frandsen 1998; Reardon et al. 2007).

Differences in bulk density can be associated with other properties of peat soils such as soil structure, particle size, pore space and decomposition (Ingram 1978). The variation of these physicochemical properties can also affect the energy produced during peat oxidation and the energy transferred through peat particles (Reardon et al. 2007; Huang et al. 2015). The presence of artefacts (e.g. roots, stones) may also play a role in creating variability in peat conditions that could affect the propagation of smouldering fires. Twigs and roots, for example, have been reported to promote the propagation of smouldering fires (Miyanishi and Johnson 2002; Davies et al. 2013); this is likely a result of local changes to MC around the root.

The hydrology of peatlands as well as peat properties should be carefully observed in order to estimate variations in moisture and bulk density as we have shown that these peat conditions strongly influence the propagation of smouldering fires even on a fine scale. The spatial variability and dynamics of peat conditions remains a challenge to studies of peat fires in the field (McMahon et al. 1980; Hungerford et al. 1995) and highlights why laboratory-scale studies are required to understand measured effects on smouldering. The control of individual properties such as moisture content and bulk density can then be used to piece together the broader relationship between peat conditions and smouldering in the natural environment. Milled peats like those used here have been the most utilised alternative to reduce the variability of natural peats and study the influence of external factors (moisture, mineral content, bulk density, oxygen availability, etc.) on smouldering combustion of peat (Frandsen 1987, 1991; Belcher et al. 2010; Hadden et al. 2013; Zaccone et al. 2014; Prat et al. 2015).

Conclusions
This study has built on previous work on ignition and early horizontal propagation of smouldering fires in peats. We coupled laboratory-scale observations of smouldering fires with statistical models to estimate and analyse the fire spread rate and the expected fraction of peat burnt at distance longer than 12 cm. Our findings enable an understanding of the effects of a variety of peat moisture content and bulk density conditions on smouldering propagation dynamics. Self-sustained fronts were observed to propagate in peats with moisture content below 150% MC. The bulk density of the peat was also found to affect the propagation of smouldering fires. The increase of bulk density enhances the effects of moisture content on the propagation dynamics.

Our approaches highlighted that laboratory-scale experimental research can contribute to the theoretical insights of the behaviour of smouldering fires. Data from this study are fundamental to integrate a wide range of realistic peat conditions and their associated horizontal and vertical dynamics to modelling approaches at larger scales.

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