DYNAMIC IMPACT OF HEAVY LONG VEHICLES WITH EQUALLY SPACED AXLES ON SHORT-SPAN HIGHWAY BRIDGES

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Abstract. Extremely large trucks with a weight exceeding the standard require a permit before they are allowed to cross the bridges of a specific route. For the purpose of safety, an escort is often employed to maintain a distance between vehicles and to ensure that the bridge load remain below the allowed maximum. Given that the speed of these large vehicles is quite slow and that the amplitude of vibrations normally declines when the vehicle mass is large, a minor dynamic amplification of the bridge response is expected. However, some of these large trucks have a unique feature characterized by "multiple equally-spaced axles", something that is uncommon in normal vehicle. The application of axle forces at equal intervals can dynamically excite bridges to a considerable extent, even at low speeds. These "critical" low speeds are estimated a priori from the axle spacing of the truck and the main frequency of vibration of the bridge. This paper demonstrates that when the "critical" speed is unavoidable, a relatively high dynamic allowance must be added to static calculations before granting a permit to a long heavy vehicle.

Keywords: bridge dynamics, critical velocity, dynamic amplification factor (DAF), expansion joint, large trucks, permit vehicles, vehicle bridge interaction (VBI).

1. Introduction

Special vehicles above normal legal weight limits have been generally found to govern bridge loading in short- and medium-span bridges (Enright, OBrien 2013). For this reason, there is a considerable amount of research on these traffic-loading scenarios, mostly focused on their static effect on bridges. For example, Casas and Aparicio (2001), and Correia and Branco (2006) analyse the likelihood of large vehicles moving on bridges. They consider various factors that have an impact on the passage of the vehicle over the bridge such as vehicle weight and configuration (i.e., axle loads, axle spacing) and bridge critical length, to provide bridge engineers with an extensive knowledge during the decision-making process of granting a permit. Vigh and Kollar (2007) put forward an algorithm for finding out the bridge safety levels, keeping in view overweight vehicles. The algorithm employs rapid and robust computations that require small amounts of input data like the span and width of the bridge, kind of superstructure, axle loads and axle spacing of the overweight vehicle. In 2013, Enright and O'Brien (2013) perform Monte Carlo simulation based on wide-ranging collections of Weigh-in-Motion (WIM) data from five countries. This data is used to examine the impact of various management policies on the regulation of special permit vehicles. Almost all vehicles weighing more than 100 tons are cranes or low loaders, and those vehicles exceeding 120 tons are low loaders. There are closely spaced axles in both, cranes and low loaders, , which typically have around eight or nine heavily loaded axles within an axle group. The length and type of bridge, as well as the load impact being evaluated, determine the intensity of the loading. According to the authors, it is not possible to draw conclusions regarding the effectiveness of regulating the type of vehicles issued a permit.

The bridge response to the movement of vehicles is an intricate issue as two structural subsystems (bridge and vehicle) interact with each other through a road surface. The total response has both static and dynamic components. Dynamic Amplification Factor (DAF) is a term widely used in the literature (Brady, OBrien 2006; Mohammed et al. 2014; Rezaiguia et al. 2015) to quantify the interaction between the bridge and vehicle. DAF is defined as the ratio of the maximum total response to the maximum static response during a vehicle crossing, for the load effect of the bridge being examined (i.e., bending moment at midspan section). This is the definition employed throughout the paper. A review of the factors affecting the dynamic increment with respect to the static component has been recently carried out by (Deng et al. 2014). It has been noted that given a bridge and road profile, there is a DAF-speed pattern associated with a vehicle. It is composed of various peaks and troughs that tend to increase with speed (Brady et al. 2006; Ding et al. 2009; Kwasniewski et al. 2006). The traffic laws of each country tend to limit the highest vehicle speed (Enright, O'Brien 2013), which is relatively lower for highway bridges as compared to high-speed railways (Yang et al. 2004). The vehicle speed is restricted further to permit vehicles due to their weight to ensure safety. Brady and O'Brien (2006) relate DAF peaks due to two moving loads to their spacing and critical speeds. Troughs develop due to destructive interference between both loads. Yang et al. (2004) explain that multiple moving loads can affect the impact factor of the bridge to a large or small extent depending on them being equidistantly spaced (i.e., causing resonance), or at an unequal distance from each other (i.e., cancelling effects). Therefore, Equation (1) defines the resonant speed due to a uniform axle spacing (Li, Su 1999).

$$v = \frac{f L_{v}}{n} (n = 1, 2, 3, ...), (1)$$

where v refers to the vehicle speed, m/s; L_v refers to the axle spacing of the vehicle, m; f – the main natural frequency of the bridge, in Hz.

Shi et al. (2008) adopt Equation (1) to forecast the resonant speeds for the HS20 truck (Section 3 of AASHTO code (2012)) moving across a short bridge of 8 m length. In this case, the truck has a far lower number of axle loads

than a train, but they argue that the multi-axle truckloads are perceived as recurring loads on smaller bridges. While the resonance phenomenon due to configurations made of equally spaced axles has received lots of attention in railway bridges (Cantero *et al.* 2015; Cantero, Karoumi 2016), the specific problem of quantifying DAF due to permit vehicles with uniform axle spacing has been insufficiently addressed for highway bridges. Cantero *et al.* (2011) compare DAF due to articulated 5-axle trucks to large cranes at typical highway speeds, but they overlook the resonance effect. This paper fills this gap by analysing the impact of speed, weight, configuration and transverse location of a permit vehicle on the bridge response. For this purpose, simulations are carried out employing Vehicle-Bridge Interaction (VBI) Finite Element (FE) models. The investigation is focused on short-span bridges where single traffic events involving a permit vehicle may be critical (Enright, OBrien 2013). The influence of road roughness, as well as troughs (or bumps) close to the expansion joints, on DAF is also discussed. Results are compared to a conventional 5-axle truck configuration, commonly found in the road network.

2. Finite element modelling of vehicle bridge interaction

A review performed by González (2010) discusses coupled and uncoupled methods employed in VBI simulations. An FE model consisting of 2D plate elements is built with MATLAB sofware to analyse the bridge response. An uncoupled VBI method, based on (Cantero *et al.* 2010), is preferred for computational efficiency. The uncoupled VBI method allows solving the equations of motion of the bridge and those of the vehicle as two subsystems (González 2010), which are solved by means of a Newmark-Beta direct integration scheme. Initial conditions of displacement, velocity, and acceleration are considered zero in all simulations. The following sub-sections discuss the bridge and vehicle models, the road profile and the interaction algorithm.

2.1. Bridge model

A simply supported bridge of 11 m width (i.e., allowing accommodating a 2-lane carriageway) and 15 m span length (i.e., allowing a single vehicle event made of a 5-axle truck to fit fully) is modelled as an isotropic thin slab of 0.75 m depth. OBrien *et al.* (2014) assume a solid slab section typical of short span bridges following guidelines. The FE slab model is discretised into 0.5 m x 0.5 m C1 plate elements. There are four Degrees Of Freedom (DOFs) at each node of a C1 plate element (González *et al.* 2008a): one vertical displacement, one twist and two rotations (in *X* and *Y* directions). When compared to the normal Kirchhoff plate element (Reddy 2002), there is one extra DOF per node in this element to avoid the discontinuity of slope across the edge elements. The moduli of elasticity in the longitudinal and transverse directions are adopted to be 35 GPa, and the shear modulus is 14 GPa. The material density is 2533 kg/m³, leading to the 1st frequency of vibration of 5.65 Hz. The damping ratio is adopted to be 0.03.

2.2. Vehicle model

3D models of a long 19-axle vehicle (i.e., simulating a permitted vehicle) and a standard European 5-axle truck are built to compare their influence on DAF. The 19-axle vehicle model (Figure 1) has two significant bodies: the tractor (resting on 3 axles) and trailer (resting on 16 axles), with an overall length of 33.7 m. The selected dimensions are obtained from the Mercedes Benz Trucks/Heavy duty modular trailer and concrete boom rigid truck configuration. Of relevance to this investigation, it is the uniform spacing of 1.5 m for the axles in the trailer. This 3D model has 44 DOFs distributed as follows:

- 9 DOFs in the tractor, which record the vertical displacement taking place individually by the six wheels, and the bounce displacement, pitch, and roll rotations developing in the body,
- 35 DOFs in the 16-axle trailer to account for each of the wheel displacements and body displacements and rotations.

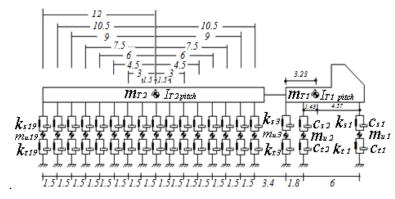


Fig. 1. Side view of 19-axle vehicle (all dimensions in meters)

Tractor and trailer are assumed two succeeding bodies having the same travelling speed. When no link exists between the tractor and trailer, the towed component in the long-vehicle is defined as a truck without trailer having the same travelling speed as the primary vehicle (Fafard *et al.* 1997). For all axles, the distance between the left wheel

and right wheel is assumed 2 m. Table 1 provide mechanical parameters of the long vehicle. Each wheel has a static weight of 28.31 kN in the 1st axle, 30.07 kN in the 2nd and 3rd axles, and 50.5 kN from the 4th to the 19th axles.

Table 1. Properties of 19-axle long vehicle (*R* and *L* refer to right and left wheel respectively)

Symbol	Property	Value Units		
m_{T1}	Tractor body mass	15 100 kg		
m_{T2}	Trailer body mass	147 400 kg		
$m_{u 1R}$, $m_{u 1L}$	Mass for each wheel of 1st axle of the tractor	350 kg		
m_{u} 2 R , m_{u} 2 L	Mass for each wheel of 2 nd axle of the tractor	550 kg		
$m_{u 3R}$, $m_{u 3L}$	Mass for each wheel of 3 rd axle of the tractor	550 kg		
<i>m</i> _u 4-19 <i>R to m</i> _u 4-19 <i>R</i>	Mass for each wheel of the trailer	550 kg		
I _{T1 pitch}	Pitch moment of inertia of the tractor body (about Y-axis)	$8.8319 \cdot 10^4 \text{ kg m}^2$		
$I_{T1 \ roll}$	Tractor rolling moment of inertia (about <i>X</i> -axis)	$6.3 \cdot 10^3 \text{ kg m}^2$		
I _{T2 pitch}	Pitch moment of inertia of the trailer body(about Y-axis)	7.9988·10 ⁶ kg m ²		
$I_{T2\ roll}$	Trailer rolling moment of inertia (about <i>X</i> -axis)	$61.4 \cdot 10^3 \text{ kg m}^2$		
Ks_{1R} , Ks_{1L}	Suspension stiffness for each wheel of 1st axle	$0.2 \cdot 10^6 \text{ N m}^{-1}$		
Ks _{2R} , Ks _{2L}	Suspension stiffness for each wheel of 2 nd axle	0.5·10 ⁶ N m ⁻¹		
Ks_{3R} , Ks_{3L}	Suspension stiffness for each wheel of 3 rd axle	$0.5 \cdot 10^6 \text{ N m}^{-1}$		
KS4-19R, KS4-19L	Suspension stiffness of each wheel of the trailer axles	0.5·10 ⁶ N m ⁻¹		
Cs_{1R} , Cs_{1L}	Suspension damping for each wheel of 1st axle	0.5·10 ⁴ Ns m ⁻¹		
Cs _{2R} , Cs _{2L}	Suspension damping for each wheel of 2 nd axle	1·10 ⁴ Ns m ⁻¹		
Cs_{3R} , Cs_{3L}	Suspension damping for each wheel of 3 rd axle	1⋅10 ⁴ Ns m ⁻¹		
CS4-19R, CS4-19L	Suspension damping of each wheel of the trailer axles	1⋅10 ⁴ Ns m ⁻¹		
Kt_{1R} , Kt_{1L}	Tyre stiffness for each wheel of 1st axle	0.875·10 ⁶ N m ⁻¹		
Kt_{2R} , Kt_{2L}	Tyre stiffness for each wheel of 2 nd axle	1.75·10 ⁶ N m ⁻¹		
Kt_{3R} , Kt_{3L}	Tyre stiffness for each wheel of 3 rd axle	1.75·10 ⁶ Nm ⁻¹		
Kt4-19R, Kt4-19L	Tyre stiffness for each wheel of the trailer axles	1.75⋅10 ⁶ N m ⁻¹		
Ct_{1R} , Ct_{1L}	Tyre damping for each wheel of 1st axle	1.5·10 ³ Ns m ⁻¹		
Ct_{2R} , Ct_{2L}	Tyre damping for each wheel of 2^{nd} axle 2.5			
Ct _{3R} , Ct _{3L}	Tyre damping for each wheel of 3 rd axle	$2.5 \cdot 10^3 \text{ Ns m}^{-1}$		
Ct4-19R, Ct4-19L	Tyre damping for each wheel of the trailer axles	$2.5 \cdot 10^3 \text{ Ns m}^{-1}$		

Figure 2 shows the 5-axle tractor-semitrailer modelthat is composed of two main sub-structures, tractor, and semitrailer depicted as grouped masses (Cantero *et al.* 2010). The model has 15 DOFs in the form of wheel hop displacements (by every of the 10 un-sprung masses of wheel), tractor bounce displacement, tractor pitch rotation, tractor rolling rotation, semi-trailer pitch rotation, and semi-trailer rolling rotation. Besides the geometry, number, and weight of axles, the articulation hinge in the 5-axle tractor-semitrailer is another feature that distinguishes it from the 19-axle vehicle in Figure 1.

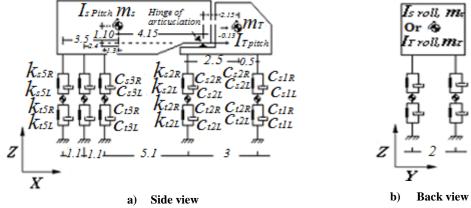


Fig. 2. General vehicle model sketch (all dimensions in meters)

Table 2 gives the mechanical properties of the vehicle. The static wheel weights are 24.94 kN, 54.39 kN, 39.02 kN and 39.02 kN for vehicle axles 1 to 5 respectively based on the distribution of gross vehicle weight proposed by (González *et al.* 2010). The mechanical parameters in Tables 1 and 2 are based on a range of values proposed in

the literature (Fu, Cebon 2002; Harris *et al.* 2007; Kirkegaard *et al.* 1997; Wong 2008), including publications dealing with large vehicles (Cantero *et al.* 2011; Lehtonen *et al.* 2006; Li 2005).

Table 2. Properties of 5-axle truck model (*R* and *L* refer to right and left wheel respectively)

Symbol	Property	Value Units		
m_T	Tractor body mass	4 500 kg		
m_s	Semi-trailer body mass	31 450 kg		
m_{u1}	Tractor front axle	700 kg		
m_{u2}	Tractor rear axle	1 000 kg		
m_{u3} to m_{u5}	The mass for each axle of the Semitrailer	1 100 kg		
I_{Tpitch}	Tractor pitch moment of inertia (about Y-axis)	$4~875~kg~m^2$		
$I_{T roll}$	Tractor rolling moment of inertia (about X-axis)	$3~000~\mathrm{kg}~\mathrm{m}^2$		
Is pitch	Semi-trailer pitch moment of inertia (about Y-axis)	$123\ 000\ kg\ m^2$		
$I_{s\ roll}$	Semi-trailer rolling moment of inertia (about <i>X</i> -axis)	$2\ 1000\ kg\ m^2$		
Ks_{1R} , Ks_{1L}	Suspension stiffness of tractor front axle	200·10 ³ N m ⁻¹		
Ks_{2R} , Ks_{2L}	Suspension stiffness of tractor rear axle	500·10 ³ N m ⁻¹		
Ks_{3-5R} , Ks_{3-5L}	Suspension stiffness of each of the semitrailer axles $500 \cdot 10^3 \text{ N}$			
Cs_{1-5R} , Cs_{1-5L}	Axles suspension damping 5.10			
K_{t1R} , K_{t1L}	Tyre stiffness of tractor front axle 875·10			
K_{t2R} , K_{t2L}	Tyre stiffness of tractor rear axle $1.750 \cdot 10^3 \text{ N} \text{ m}$			
K_{t3-5R} , K_{t3-5L}	Tyre stiffness of each of the semitrailer axles 1 750·10 ³ N m			
C_{t1-5R} , C_{t1-5L}	Axles tyre viscous damping	$3 \cdot 10^3 \text{ Ns m}^{-1}$		

Following a modal analysis, pitching and rolling body frequencies fall within 1.5 Hz to 4.5 Hz and axle hopping frequencies within 9 Hz to 16 Hz in agreement with the range published by Cebon (1999). In the case of the permit vehicle associated with Table 1, there are three main modes of vibration in the tractor body: bouncing at 1.59 Hz, pitching at 2.22 Hz and rolling at 2.88 Hz. There are also three main modes of vibration in the trailer body: bouncing at 1.39 Hz, pitching at 1.79 Hz and rolling at 2.46 Hz. Wheel hop frequencies of 8.82 Hz and 10.20 Hz are found for the first axle and the remaining axles respectively. In the case of the 5-axle truck associated to Table 2, the body masses have bouncing frequencies of 1.49 Hz for the tractor, pitching frequencies of 2.30 Hz for the tractor and 1.49 Hz for the semitrailer, and rolling frequencies of 3.01 Hz for the tractor and 1.59 Hz for the semitrailer. Axle hop frequencies of 8.96 Hz, 10.7 Hz, and 11.6 Hz are found for the first axle, second axle, and rear tridem respectively.

2.3. Road profile

2.3.1. Generation of road carpet

It is possible to create artificial road profiles through a stochastic process based on the power spectral density of vertical displacements combined with the inverse fast Fourier transform technique explained by Cebon and Newland (1983), in accordance with *ISO* 8608:1995 Mechanical Vibration-Road Roughness Surfaces Fifteen random carpets have been generated for *ISO* 8608:1995 road class A (very good) with a geometrical spatial means of $16 \cdot 10^{-6}$ m³/cycle and for *ISO* 8608:1995 road class B (good) with a geometrical spatial means of $64 \cdot 10^{-6}$ m³/cycle An average moving filter is applied to the randomly generated road profile heights. The filter has a span of 0.24 m in order to replicate the short wavelength disturbances brought about by the contact patch of the tyre (Harris *et al.* 2007; Sayers, Karamihas 1996). An example of class B road carpet located on the bridge surface is represented in Figure 3. A 100 m approach is added before the bridge to produce realistic initial dynamic equilibrium conditions of the vehicle prior to entering the bridge.

Transverse distance (m)

5.5

Longitudinal distance (m)

Fig. 3. Bridge surface based on a class B road profile

2.3.2. Trough near expansion joints

Troughs are likely to develop close to the expansion joints. When vehicles travel over troughs, an initial bounce may lead to high impact forces. Although this initial bounce of the vehicle will damp out with time, a high initial vibration is also injected to the bridge deck when the vehicle is close to the bridge support due to the significant kinetic energy accumulated in the vehicle (Moghimi, Ronagh 2008). Here, the troughs at the expansion joints are placed at a distance

of 0.5 m from the supports of the bridge. The trough is modelled with a sinusoidal shape of 100 cm length in agreement with Kim *et al.* (2007). The trough height is defined by a probabilistic normal distribution with a mean value of 20.4 mm and a standard deviation of 7.0 mm, following a national survey conducted on roadway bridges in Japan (Honda *et al.* 1982). Fifteen troughs heights are obtained for each expansion joint at both ends of the bridge. These troughs are added to the 30 road profiles carpets (15 profiles of class A and 15 profiles of class B) described in Section 2.3.1. Figures 4a and 4b show one of the troughs and the result of combining the two troughs with a class B road profile respectively.

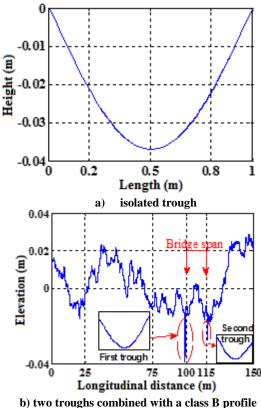


Fig. 4. Trough and road profile with troughs

2.4. Vehicle-Bridge Interaction Algorithm

Equations (2)–(3) give the equations of motion of vehicle and bridge respectively.

$$M_v \dot{w_v} + C_v \dot{w_v} + K_v w_v = f_v$$
,(2)

where M_v , C_v , and K_v are global mass, damping and stiffness matrices of the vehicle respectively; $\ddot{w_v}$, $\dot{w_v}$ and w_v are the vectors corresponding to nodal accelerations, nodal velocities and nodal displacements.

Cantero et al. (2010) and González (2010) explain how to form these matrixes from assembling mass, spring and damping elementary matrixes into a multi-body dynamics system. f_v is a vector containing the time-varying forces imposed on the DOFs of vehicles.

$$M_b \dot{w_b} + C_b \dot{w}_b + K_b w_b = f_b, (3)$$

where M_b , C_b , and K_b – global mass, damping, and stiffness matrices respectively of the plate model; $\ddot{w_b}$, \dot{w}_b and w_b – vectors containing nodal accelerations, velocities and displacements; f_b – the vector of external forces applied to the DOFs of the bridge.

An iterative process is implemented to ensure geometric compatibility between the position of the vehicle wheels and the displacement of the points in the bridge in contact with the wheels. For this purpose, Equation (3) is initially used to calculate f_v at the DOFs of the vehicle from the road excitation (i.e., the bridge is <u>disregarded</u> for this initial calculation). This equation is solved via application of the Newmark-Beta direct integration method with a time increment of 0.002 s and values for the integration constants of delta = 0.5 and beta = 0.25. Next, the forces at the DOFs in contact with the bridge or wheel forces (contained in f_v) are converted to equivalent forces acting on the bridge nodes (f_b) using Equation (4).

$$f_b = [L]_{n \times nf} f_v, (4)$$

where [L] is an $n \times n_f$ time, varying location matrix, which relates the n_f wheel forces to equivalent forces acting on the

n DOFs of the bridge model.

Full details about this matrix are avilable in (Mohammed, González 2017). The vector f_b is then employed in Equation (2) to calculate bridge displacements (w_b) using the same Newmark-Beta integration scheme. These displacements are added to the road profile to recalculate the vehicle forces f_v in a 2nd iteration and the process is repeated until the variation among the bridge deflections in two consecutive iterations is inferior to 2% of the highest bridge deflection. Once the latter is achieved, the forces of the vehicle are positioned at different coordinates on the bridge and the iterative process is repeated for thenext time step. The equations in this procedure are solved using MATLAB as further described by (Cantero *et al.* 2011). The algorithm has been validated against alternative VBI approaches (González *et al.* 2008b) and experimental data (González *et al.* 2010; Rowley *et al.* 2009).

3. Estimation of DAF-speed pattern using a vehicle model consisting of moving point loads

Here, DAF is defined as the ratio of maximum total (static + dynamic) Bending Moment (BM) to maximum static component at the mid-span section of the bridge because of a vehicle crossing. DAF versus speed patterns are vehicle-, bridge- and road-specific and they allow identifying the presence of critical speeds that cause a relatively higher dynamic response of the bridge. This section carries out a preliminary planar analysis where the bridge is modelled as a beam with the properties of the plate defined in Section 2.1. The vehicle is modelled using point loads to analyse the influence of general bridge characteristics and vehicle configuration on DAF in isolation from other factors such as road profile and vehicle dynamics. In the absence of a road profile (or "very good" road profiles), DAF-speed patterns have a smooth shape made of troughs and peaks located at critical speeds. The DAF-speed pattern for the 15 m beam bridge model under investigation due to a point load is shown in Figure 5a. The speed of the point load is varied from 10 km/h to 122 km/h (with a speed increment of 1 km/h). This figure is in agreement with Brady et al. (2006), who analyse the single point load case and identify combinations of vehicle speeds, bridge span lengths and bridge frequencies causing highest dynamic amplifications. They define a dimensionless load frequency parameter as the ratio of vehicular "frequency" (i.e., vehicle speed divided by bridge length) to first frequency of vibration of the bridge. It is possible to change the horizontal axis of Figure 5a from speed to a non-dimensional quantity of frequency ratios, which would make the graph applicable to any speed of the point load, bridge length or bridge frequency value. González et al. (2010) retrieve patterns of DAF for multiple point wheels crossing a bridge 3D model. They show that it is possible to find DAF-speed patterns by means of simple point load models, in models and simulations of greater complexity than a beam model, as well as in field trials. The number of axles, their spacing and maximum weights are static mechanical parameters are easily found about the permit truck, making it possible to derive a DAF-speed pattern for a specific bridge. Figure 5b describes the DAF-speed pattern for the planar long vehicle at speeds from 10 km/h to 122 km/h (with a speed increment of 1 km/h). This graph has been obtained from the response of the beam to a long vehicle model consisting of 19-point loads (one per axle) of value equal to the static axle weights and separated by the axle spacing defined in Section 2.2. There is one noticeable difference when compared to Figure 5(a) peak DAF values are generally smaller in Figure 5b, except for a sharp peak occurring at a relatively low critical speed of 30.24 km/h because of constructive interference between axle spacing, speed and main frequency of vibration of the bridge. Using 1.5 m for the equidistant spacing of trailer axles, Equation (1) gives a critical speed of 30.53 km/h, approximately the value in the figure except for inaccuracies derived from the discretization level. This low critical speed leads to a maximum DAF value of 1.066.

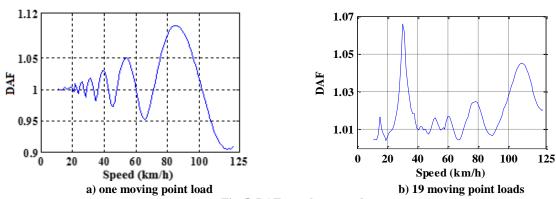


Fig. 5. DAF-speed pattern due to

Figure 6 shows the static and total bending moments at mid-span crossed by the long-vehicle at the critical speed of 30.24 km/h. Assuming a linear dynamic problem, the contribution of each axle is superposed to obtain the total response. The individual responses are separated here to understand why dynamic amplification occurs. Figures 7a and 8a depict these individual contributions for 30.24 km/h and 39.96 km/h respectively. According to Figure 7b, the contribution of each axle to the bending moment reaches the highest stage simultaneously, at 30.24 km/h. However, at 39.96 km/h, the contributed features interfere with each other (Figure 8b) leading to a lower DAF of 1.01 compared to 1.066 for 30.24 km/h.

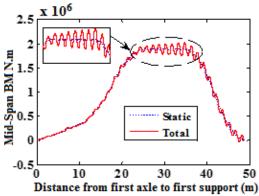
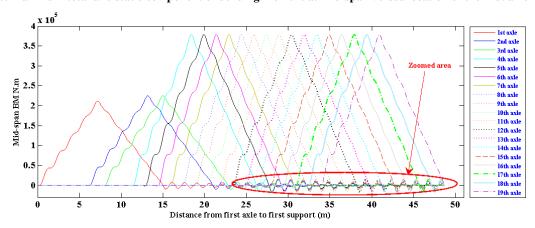


Fig. 6. Maximum total and static component of bending moment at mid-span versus location of the first axle



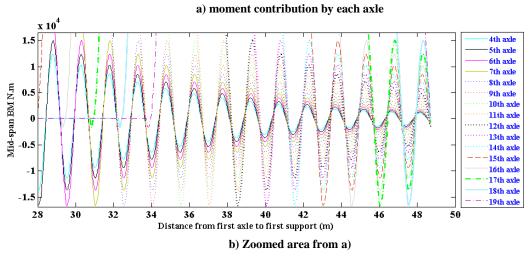
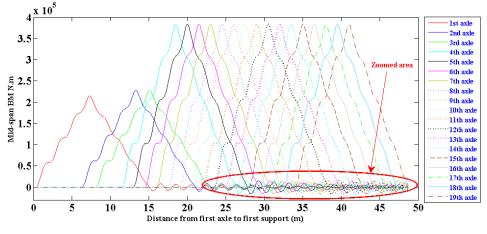


Fig. 7. Individual contributions of each axle to total bending moment at 30.24 km/h



a) moment contribution by each axle

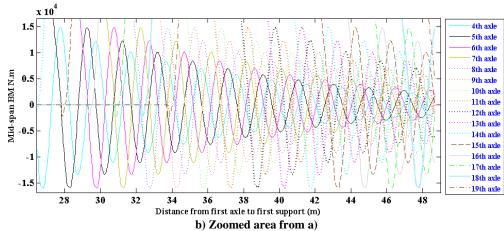
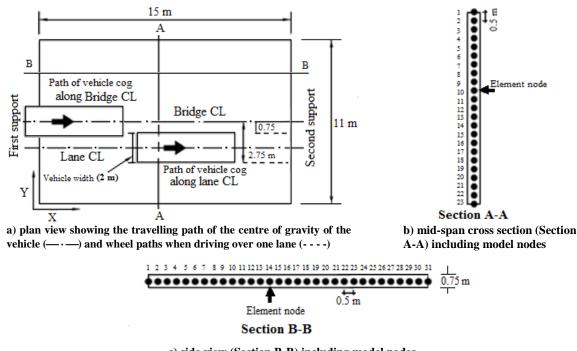


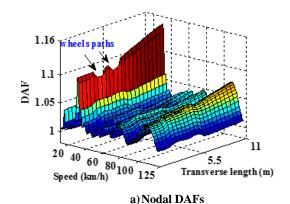
Fig. 8. Individual contributions of each axle to total bending moment at 39.96 km/h

This dynamic amplification is now explained by applying 38-point moving loads (19 point loads at each side), representing static wheel weights, to the 2D plate bridge model defined in Section 2.1. The path of the gravity-centre of the vehicle is employed to define its location on the bridge. The gravity-centre of the vehicle is driven centred in one lane (i.e., wheel paths within an axle at 0.75 m and 2.75 m from bridge centreline) as shown in Figure 9a. The model has 23 and 31 nodes in transverse (Section A-A in Figure 9b) and longitudinal (Section B-B in Figure 9c) directions respectively. A nodal DAF of bending moment is obtained for each of the twenty-three nodes at the midspan section (set apart by 0.5 m and labelled 1 to 23 in Figure 9b).



c) side view (Section B-B) including model nodes Fig. 9. Plate bridge model (add Reference if it is not yours)

It must be noted that maximum DAF through section A-A (Figure 9b) will typically take place at a different node than the one corresponding to the maximum total bending moment. Therefore, the values of maximum DAF and total bending moment are attained, together with their location. In this scenario, a highest nodal DAF of 1.15 is found for a total bending moment of 159.08 kNm in node 1 and a speed of 30.24 km/h (Figure 10a). The highest static bending moment is 204.23 kNm and the maximum total bending moment is 225.083 kN/m. Both taking place at node 23 (Nodal DAF = 1.102) at the critical speed of 30.24 km/h. Nodal DAFs of 1.076 (node 18) and 1.08 (node 13) corresponding to total bending moments of 215.03 kNm and 199.21 kNm respectively are found below the paths of the right and left wheel respectively at the critical speed. The sum of maximum total response for all 23 nodes is divided by the sum of the maximum static components for those 23 nodes to obtain a global (i.e., averaged) DAF for the mid-span section. The highest global DAF value is 1.11 (Figure 10b). There are differences between the DAF obtained in the beam (Figures 5–8) and plate (Figure 10) models due to the impact of eccentricity of the load and other 3D considerations, but as expected, Equation (1) successfully predicts the critical speed of the long vehicle in both models.



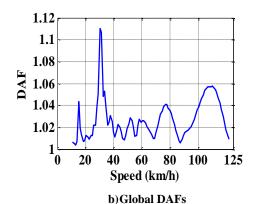


Fig. 10. DAF-speed pattern for plate model due to a series of 38 moving point loads travelling with an eccentricity with respect to the bridge centreline

4. Impact of road surface on DAF-speed pattern

While the simple model of point loads employed in Section 3 is useful to understand why DAF peaks occur at a relatively low critical speed for a long vehicle, the values of DAF may be unrealistic for a rough profile. For this reason, the next sub-sections take into account road roughness and vehicle dynamics to quantify the true impact of this resonance effect on the DAF of a plate bridge model.

4.1. Influence of road roughness on DAF

The mean and standard deviation of DAF values because of the long vehicle moving from 10 km/h to 122 km/h (with a 1 km/h increment) over the fifteen class A profiles are shown in Figure 11. The highest DAF of 1.13 (with standard deviation 0.044) occurs at node 1 (Figure 9b) for a total bending moment of 156.57 kNm and the critical speed of 30.24 km/h signalled in former sections. The position of the maximum static bending moment (204.23 kNm) is node 23, where the maximum total bending moment is 222.15 kNm and DAF is equal to 1.087 (standard deviation of 0.036) at the critical speed. DAFs of 1.063 (node 18) and 1.065 (node 13) are smaller under the wheel paths than at other nodes of the mid-span section at the critical speed due to the relatively larger static component of the response (Figure 11a). The latter corresponds to total bending moment values of 212.47 kNm and 196.48 kNm under the right and left wheels respectively.

DAF values rise when the road profile worsens and becomes bumpier, although similar DAF-speed patterns are observed for class B road profiles. The highest DAF value of 1.2 (with 0.07 standard deviation) develops in a class B for 30.24 km/h. The latter corresponds to a total bending moment of 166.31 kNm at node 1. The maximum total bending moment is 229.9 kNm (again at 30.24 km/h) and maximum static bending moment of 204.23 kNm take place at the same node 23 (DAF = 1.125 with a standard deviation of 0.065).

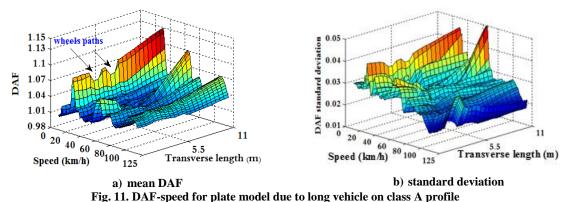
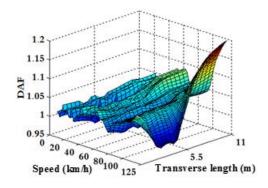
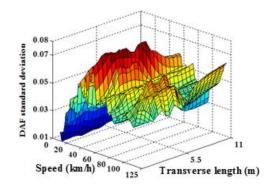


Figure 12 shows the results for the 5-axle truck defined in Section 2.2 moving on the same 15 class A profiles employed for the long vehicle. The highest mean DAF value is 1.2 (standard deviation 0.06) and corresponds to a total bending moment of 78.87 kNm at node 1 for a vehicle speed of 122 km/h. A maximum total moment of 108.68 kNm (for a speed of 98.28 km/h) is found for the position of the maximum static moment (103.80 kNm), which is located at node 18 (Figure 10b) (DAF of 1.05 with a standard deviation of 0.052). The randomness of the road profiles has a more profound effect on the response to the 5-axle vehicle than on the response to the long vehicle. As a result, the standard deviation for the 5-axle vehicle is larger than for the long vehicle, particularly at faster speeds.





a) mean DAF b) standard deviation Fig. 12. DAF-speed for plate model due to 5-axle truck on class A profile

Table 3 summarizes the highest DAF values obtained for the plate midspan, the two vehicles, the two road classes and the fifteen road carpets per class. The table also gives for reference the DAF value with a 95% Confidence Interval (CI) . Cantero *et al.* (2011) published values of DAF for a 15 m bridge considerably smaller than those in Table 3. They focus on a distribution of speed based on WIM data of mean 85.47 km/h and standard deviation 3.70 km/h for 5-axle trucks, and a distribution of mean 79.69 km/h and standard deviation 5.67 km/h for cranes. Therefore, they cover a narrower range of speeds that misses the critical speed for the crane.

Table 3. Mean value (μ) and standard deviation (σ) of DAF for road classes A and B (critical speed in km/h)

Vehicle Type -	Class type of road surface (without troughs)							
			A				В	_
	μ	σ	95% CI	speed	μ	σ	95% CI	speed
Long-vehicle	1.13	0.044	1.107 - 1.152	30.24	1.20	0.07	1.160-1.230	30.24
5-axle truck	1.19	0.060	1.160-1.220	122.00	1.20	0.12	1.139-1.260	122.00

4.2. Influence of troughs located at the expansion joint on DAF

This section combines troughs characterized by varying heights with the two road classes as described in Section 2.3.2. Then, the analysis carried out in Section 4.1.1 is repeated here for the resulting profiles. In the situation involving the long vehicle over a class A profile with troughs, the highest mean DAF turns out to be 1.19 with a standard deviation of 0.086 and takes place at node 1 for a total bending moment of 165.33 kNm at the critical speed of 30.24 km/h. The highest static and total bending moments are 204.23 kNm and 231.66 kNm (for a speed of 29.16 km/h) respectively (DAF of 1.156 with a standard deviation of 0.046), both taking place at node 23. In contrast to other transversal positions with the same speed (30.24 km/h), lower DAFs of 1.103 and total bending moment, value of 220.06 kNm is found for node 18, which falls under the path of the right wheel. Similarly, a relatively low DAF of 1.108 and total bending moment of 203.39 kNm is found at node 13 under the path of the left wheel. DAF figures are expected to experience an increase with the deterioration of the road profile and the pattern to become irregular; however, the DAF-speed pattern for class B road profiles combined with troughs still exhibits similar characteristics to the class A. The highest DAF value of 1.22 with standard deviation 0.07 takes place at node 1 with a maximum total bending moment of 169.78 kNm at the critical speed of 30.24 km/h. The highest static and total bending moments are 204.23 kNm and 236.27 kNm (for a speed of 30.24 km/h) respectively and they take place at the same node 23 (DAF value of 1.156 with a standard deviation of 0.046).

In the case of the 5-axle truck over the bridge with a class A and troughs, a highest DAF of 1.22 with a standard deviation of 0.064 is found at node 1 (for a speed of 122 km/h). Furthermore, the highest static and total bending moments are 103.80 kN and 113.45 kNm (at the speed of 44.28 km/h) respectively, and both take place at node 18, leading to a mean DAF value of 1.093 with a standard deviation of 0.048. Statistics of DAF values are summarized in Table 4 for the 30 carpets with troughs under investigation. The values of DAF in Table 4 are conservative because the highest DAFs are associated with regions with a comparatively small static moment, i.e., near the plate edge. Although DAF due to the long vehicle increases with rougher roads and troughs, DAF figures remain somewhat smaller than those corresponding to the 5-axle truck.

Table 4. Mean value (μ) and standard deviation (σ) of DAF for road classes A and B combined with troughs (critical speed in km/h)

Vehicle Type	Class type of road surface (with troughs)							
	A				В			
	μ	σ	95% CI	Speed	μ	σ	95% CI	speed
Long-vehicle	1.19	0.086	1.146-1.233	30.24	1.22	0.070	1.185-1.255	30.24
5-axle truck	1.22	0.064	1.187 - 1.252	122.00	1.23	0.125	1.166-1.293	122.00

The model based on point loads of Section 3 helps to understand the underlying constructive and destructive interferences among axles as demonstrated by Figures 7 and 8 respectively and to identify the critical speed for a long vehicle as shown by Figure 10. However, the peak DAF at the critical speed by a point load model leads to a value that differs from the one obtained with sprung models. The latter is explained by the height of road irregularities, which have changes comparable to the bridge deflections, more significantly the rougher the road surface. These irregularities have a strong impact on vehicle dynamic forces and subsequently on the bridge response. Hence, Table 3 shows a mean DAF of 1.20 for a road class B population, which is higher than the value of 1.13 obtained for a road class A. Similarly, when a trough is added at the expansion joint, mean DAFs increase from 1.13 (Table 3) to 1.19 (Table 4) for a class A and from 1.20 (Table 3) to 1.22 (Table 4) for a class B. Point loads are unable to capture the effect of road roughness. The highest nodal DAF of 1.15 is obtained using the 38-point load model on a plate model for the long vehicle, which is 6.1% smaller than the DAF value of 1.22 obtained using the sprung model on a class B profile with troughs. However, the DAF value provided by the 38-point load model is only 1.8% higher than the mean value of 1.13 obtained by the sprung model on a class A profile without troughs. This shows that a simplistic point load model can be used for preliminary assessment of DAF for smooth road profiles. The 3D nature of the problem has to be considered, particularly in the case of the vehicle driving eccentrically with respect to the bridge centreline. It has been seen how an equivalent 19-point load model on a planar beam model provides a DAF value of 1.066 at the critical low speed (Figure 5), which is considerably smaller than the global DAF factor of 1.11 found for the 38-point loads on the plate model. In the case of a class A road profile, the beam model underestimates the highest nodal dynamic amplification of 1.13 (at node 1), although it is relatively close to the DAF associated to the maximum static moment (i.e., DAF = 1.087 at node 23).

5. Conclusions

Extremely long and heavy trucks need to have a traffic permit before travelling on the roads. The road authorities must carefully examine how particular truck configurations affect the safety of the bridges across the route decided for the vehicle. In the case of large forces generated by the truck being close to the loading capacity of certain bridges, the bridge response must be evaluated accurately, i.e., allowing for the dynamic increment resulting from the interaction between the vehicle and the bridges. Only then, the engineer will be in a position to take a precise decision on the permit. For two vehicle types and two road profile classes, this paper has provided an insight into the DAF of the mid-span bending moment of a 15 m long simply supported bridge. The bridge has been modelled as an isotropic thin plate. The analysis has covered the influence of road roughness, with and without damaged expansion joints, and the configuration, transverse location and speed of the vehicle on DAF. The results have indicated that:

- 1. A considerable amplification of the dynamic response takes place for a long vehicle comprised of evenly spaced axles travelling at a low speed of 30.24 km/h. This finding appears to be counterintuitive given the large gross vehicle weight, long rigid configuration, and low speed. However, when the recurrence of equally spaced axles at a critical low speed synchronizes with the primary period of the vibration of the bridge, the response waves produced by each wheel force add together causing a resonance effect. The critical speed is calculated from the axle spacing in the vehicle and the main frequency of the vibration of the bridge.
- 2. When the critical speed is unavoidable, a dynamic allowance must be added to static calculations of the bridge response (i.e., via the application of a DAF) before granting a permit to long heavy vehicles comprised of evenly spaced axles. The shape of the DAF-speed pattern is brought about by utilizing a simple model based on point loads. The variability of these patterns increases with the worsening of the road condition and the introduction of troughs (i.e., larger mean DAFs and larger standard deviations the poorer the road condition). The impact of road roughness on DAF is shown to be less important for the long vehicle than for a 5-axle vehicle.

Even though this paper has focused on a specific vehicle and bridge, the conclusions are applicable to other scenarios. I.e., similarly to the phenomenon investigated here, loads by several trucks driving at equal distances will be sensitive to critical speeds related to the bridge frequency. This scenario is found in a convoy where similar truck configurations travel at a uniform speed with a similar headway. Therefore, the findings in this paper have the potential to be extended to future developments in the field of electronic tow bars for convoys.

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