

# 1 **Energy Harvesting from Train Induced Response in** 2 **Bridges**

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**10 Abstract**

11           The integration of large infrastructure with energy harvesting systems is a growing  
12 field with potentially new and important applications. The possibility of energy harvesting  
13 from ambient vibration of bridges is a new field in this regard. This paper investigates the  
14 feasibility of energy harvesting for a number of trains considering their passage over a bridge.  
15 The power that can be derived from an energy harvesting device due to a train crossing a  
16 bridge for different speeds are compared against typical demands of small wireless devices  
17 and are found to be adequate for powering such devices. These estimates of harvested energy  
18 also relate to the individual signatures of trains. In this work, the modelled dynamic responses  
19 of a bridge traversed by trains are compared against full scale experimental analysis of train-  
20 bridge interactions. A potential application in structural health monitoring using energy  
21 harvesting has also been demonstrated and compared with laboratory experimental data.  
22 Consistent and monotonic damage calibration curves have been constructed using estimated  
23 harvested energy.

**24 CE Database Subject Headings**

25 Bridges; Smart Materials; Energy Methods; Monitoring;

**26 Authors keywords**

27 Train-Bridge Dynamics, Piezoelectric, Energy Harvesting, Structural Health Monitoring,  
28 Wireless Sensor Network, Experimental Data.

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**30 Introduction**

31           With the current advances in microsystems, and the potential that they create for  
32 autonomous sensing systems, substantial consideration has been placed on the supply of

33 power and the efficient use of such systems, particularly for wireless sensor networks. This  
34 requirement has resulted in significant investigations into the use of different energy  
35 harvesting techniques for the powering of wireless networks (Harb 2011), with much of the  
36 attention being focused on the use of vibration based electromagnetic, electrostatic and  
37 piezoelectric solutions (Beeby et al. 2006).

38         Of these energy harvesting techniques, devices based on the use of piezoelectric  
39 materials have proven to especially effective (Cook-Chennault et al. 2008; Sodano et al.  
40 2004; Anton and Sodano 2007). Significant research has been carried out to date on the  
41 optimisation of the design of the piezoelectric energy harvesters, including cantilever based  
42 applications (Jackson et al. 2013a; Jackson et al. 2013b; Erturk and Inman 2008), a bimorph  
43 cantilever (Ajitsaria et al. 2007) and a dual-mass vibration harvester (Tang and Zuo 2011).  
44 With large differences in the physical properties of piezoelectric materials, which range from  
45 ceramics to polymers, identifying the most suitable for specific applications is essential  
46 (Vatansever et al. 2011).

47         The potential use of energy harvesting systems for civil infrastructure (Sazonov et al.  
48 2009) has just recently begun to receive attention and the true potential for applications in the  
49 field of civil engineering has yet to be realised. A recent study (Ali et al. 2011) investigated  
50 the feasibility of using tuned piezoelectric energy harvesters as a method of powering  
51 microsystems through the parasitic harvesting of ambient structural vibrations from bridge  
52 infrastructure. Different methods of piezoelectric energy harvesting for bridges have also  
53 received attention (Erturk 2011).

54         Structural health monitoring (SHM) for civil infrastructure elements, on the other  
55 hand, is a field in a continuous state of development and evolution (Chang et al. 2003; Catbas  
56 et al. 2008; Moaveni et al. 2009; Pakrashi et al. 2013). Modern advances in the development  
57 of smart sensors has suggested the potential for the creation of wireless sensor networks for

58 use in the monitoring of infrastructure elements (Lynch and Loh 2006; Gangone and Whelan  
59 2011). Lead Zirconate Titanate (PZT) sensors have been embedded within reinforced  
60 concrete elements and compared against traditional methods of detection, namely strain  
61 gauges and Linear Variable Differential Transformers (LVDT), under different loading  
62 conditions (Song et al. 2007). PolyVinylidene Fluoride (PVDF) sensors have also been  
63 utilised for the wireless monitoring of tension conditions in cable stayed bridges (Liao et al.  
64 2001). Structural health monitoring of bridge infrastructure has also received some attention,  
65 with a number of methods proposed to determine the condition of bridges (Brincker et al.  
66 2003; Zhang et al. 2005; Sepe et al. 2005). One such method is using the dynamic response of  
67 train-bridge interaction and sensitivity analysis using stiffness variation for the detection of  
68 damage (Zhan et al. 2011; Shu et al. 2013). A Bridge Weigh-in-Motion (B-WIM) with  
69 accelerometers has also been implemented for the monitoring of actual traffic load (Karoumi  
70 et al. 2005; Liljencrantz et al. 2007; Liljencrantz and Karoumi 2009), but this is totally reliant  
71 on external power supplies. Consequently, evidence exists suggesting that the monitoring of  
72 train-bridge interaction under operational conditions may be beneficial for health monitoring  
73 of structures as the structure is not required to be closed for use.

74 This paper demonstrates that energy harvesting from vibration due to the response of  
75 train passages across bridges can provide sufficient power for small devices with low power  
76 demand. The additional advantage of this is that the harvested energy can be used for  
77 structural health monitoring. The levels of power which can be harvested from train-bridge  
78 dynamics under operational conditions have been investigated for:

- 79 • A range of passenger trains from international stock,
- 80 • A freight fleet from experimental data and
- 81 • A health monitoring system using the harvested energy as a metric.

## 82 **Energy Harvesting From Train Induced Responses**

### 83 **Piezoelectric Energy Harvesting System**

84 Significant research has taken place into the design and optimisation of piezoelectric  
85 energy harvesting systems, with emphasis being placed into the design of systems powered  
86 through the vibrations of the host structure (Erturk 2011). A limitation to the cantilever based  
87 energy harvester approach is the requirement to tune the harvester to the natural resonant  
88 frequency of the host structure to optimise energy harvesting potential (Ali et al. 2010).  
89 Potentially more effective is an energy harvesting system based on an adhesive patch which  
90 could be bonded to the host structure to generate power. This is achieved directly from the  
91 variation in the strain conditions from the surface to which it has been attached. It is  
92 envisaged that such an energy harvesting system could be used for multiple applications  
93 without the need for determining and tuning to the natural frequency of the host structure.  
94 Under such circumstances, it is important to assess the order of energy harvested from a  
95 certain system and assess the potential applications. For this paper, an adhesive patch energy  
96 harvesting system is evaluated for energy harvesting from bridge dynamics due the passage  
97 of trains and the potential applications of such a system identified and investigated.

### 98 ***Piezoelectric Materials***

99 Due to the large variations in the nature of piezoelectric materials, as described  
100 previously, it is imperative to investigate different materials for their use as an energy  
101 harvester in these applications. Two commercially available piezoelectric materials of  
102 rectangular geometry, PZT and PVDF, were chosen for use as the basis of the energy  
103 harvesting system. PZT is the most commonly used piezoelectric material for energy  
104 harvesting due to its excellent piezoelectric properties. A drawback of PZT, however, is its  
105 brittle nature since it is a ceramic material. This can lead to difficulty in terms of the design,  
106 handling and durability of the energy harvesting systems and as a consequence, may render it

107 be unsuitable for certain applications (Woo and Goo 2007). PVDF is a polymer which  
108 exhibits a high mechanical strength while retaining excellent flexibility (Vinogradov and  
109 Holloway 1999) and thus can be simply formed into different shapes. While it is not subject  
110 to the same physical limitations as PZT, its lower piezoelectric properties require higher  
111 strain conditions to produce a similar power output (Lin and Giurgiutiu 2006). The  
112 representative piezoelectric and physical properties of both energy harvesters considered in  
113 this paper are outlined in Table 1, including Youngs Modulus,  $E$ , the piezoelectric constant  
114  $d_{31}$  and  $e_{33}$ , and the length, width and thickness of the materials,  $l$ ,  $w$  and  $t$  respectively.

### 115 *Modelling of Energy Harvester*

116 In this work, energy harvesting systems are designed to be attached externally to the  
117 underside surface of the finite element model. The 31 mode, relating to the piezoelectric  
118 nature of the material whereby the material is poled in the vertical direction, 3, during its  
119 manufacture, and strain acts along the longitudinal direction, 1, is the mode of operation of  
120 the energy harvesting system (Anton and Sodano 2007). It is assumed that there is a perfect  
121 connection between the energy harvesters and the surface of the bridge and thus, almost  
122 identical strain conditions will act on both surfaces with no losses arising from an adhesive  
123 substrate. The model used for the calculation of the power output of the system is based on  
124 the piezoelectric principle for coupled electromechanical behaviour and the modelling of the  
125 voltage is obtained from Sirohi and Chopra (2000). The strain profile that acts upon the  
126 location at which the energy harvesters are to be positioned are evaluated and the potential  
127 voltage was subsequently calculated, (Eq.1), where  $\varepsilon$  is the evaluated strain averaged over the  
128 harvester length and  $C_p$  is the capacitance of the material, (Eq. 2). The power for each train  
129 passage was calculated from the root mean squared (RMS) of the generated voltage for the  
130 entire train passage, (Eq. 3), where  $R$  is the resistance, assigned a value of  $100k\Omega$ . The  
131 system would also incorporate an energy storage and power handling circuit which would be

132 able to consistently provide power to the low power sensors and enable them to become  
 133 autonomous wireless sensors. The design and modelling of the circuit is beyond the scope of  
 134 this paper and, thus, no reduction in power due to losses through the circuit is assumed in this  
 135 paper. Under operational circumstances, losses will not affect the order of the energy  
 136 harvested since the extent of losses will be small, dependent on the circuit. Circuit losses  
 137 range from 60 to 84% efficiency (Tabesh and Fr chet te 2010), with some circuits reporting a  
 138 96% efficiency rate (Magno et al. 2013). Furthermore, the losses would be a consistent value  
 139 over time and for each harvester, it can be expected that the losses would not influence the  
 140 relative power output potentials between different trains, the feasibility of using the energy  
 141 for devices with small power demand (Cook-Chennault et al. 2008) or potential applications  
 142 in structural health monitoring (Farrar et al. 2006).

$$143 \quad V_P = \frac{d_{31}Eb}{C_p l} \int \varepsilon dx \quad \text{Eq. 1}$$

$$144 \quad C_p = \frac{e_{33}lw}{t} \quad \text{Eq. 2}$$

$$145 \quad P = \frac{(V_{RMS})^2}{R} = \frac{\left( \sqrt{\frac{1}{T} \int_0^T V^2(t) dt} \right)^2}{R} \quad \text{Eq. 3}$$

## 146 **Train-Bridge Modelling**

### 147 ***Train Models***

148 Five international trains were chosen for the purposes of comparing the potential for  
 149 energy harvesting from train passages over a bridge (Fig. 1). These are the Irish *071Loco* and  
 150 *201Loco*, the French *TGV*, the German *I.C.E.* and the Japanese *Shinkansen* (Wang et al.  
 151 2003; Hagiwara et al. 2001). Each train was modelled with the same configuration as it  
 152 would have under operational conditions, including the number of motorcars and carriages

153 and the length and load of axles (Table 2). The *071Loco* and *201Loco* trains are powered by a  
154 single diesel motorcar, while the remaining are electric trains with locomotives located at  
155 both ends of the train. The *TGV* has a total of ten carriages, with the carriages connected to  
156 the motorcar being 21.9m in length and the remaining eight being 18.7m.

### 157 ***Modelling of Train Passage over Bridge***

158 For the purposes of modelling the change in strain conditions of a bridge that arise  
159 due to a train passage, a three dimensional finite element sectional model of the bridge was  
160 created using Strand7 finite element analysis system (Strand7 2010). The double tracks  
161 model was created using 20 node hexahedral bricks (Fig 2) and has dimensions 10.6m in  
162 length and 10m in breadth. The train axle loads were modelled as point loads at distances  
163 determined by the individual axle spacing for each train as outlined previously, acting along a  
164 load path along the length of the track. A total of seven speeds, ranging from 40 to 160km/hr,  
165 were chosen for the purposes of this investigation. The models were analysed along the base  
166 surface at the mid-span of the support beams, the position at which the energy harvesting  
167 system are located. Single train passage and double train passage with trains travelling in  
168 opposite directions were considered.

169 For the purposes of comparison with the finite element model, a differential equation  
170 model for train passages over a bridge was created for a simply supported bridge. A beam  
171 model proposed by Fryba (2001) was used in this regard. The input values were obtained so  
172 as to be identical to the finite element model and the trains as described in previous sections.  
173 The model was then solved for all single passage cases and the harvested energy output for  
174 each model was calculated from the evaluated strain. Finite element and differential equation  
175 models were compared for dynamic strain responses for each train passage (Fig. 3) and a  
176 good correlation in the appearance of the dynamic strain response was found. However, the  
177 magnitudes of the responses obtained from the finite element model were higher than those of

178 the comparable differential equation models. This response from the finite element models  
179 produced a 34.1%, 33.0%, 28.2%, 29.7% and 31.6% increase in the magnitude of the average  
180 strain for the *071Loco*, *201Loco*, *TGV*, *Shinkansen* and *I.C.E.* respectively, when compared to  
181 the differential equation counterparts. This is mostly due to the finite element model takes  
182 into account the non-centralised nature of the track and thus the transverse loading due to the  
183 train passages.

## 184 **Results**

### 185 ***Single Train Passage***

186 All train models were analysed for passages of different speeds and the harvested  
187 energy levels were evaluated from the dynamic strain responses from the finite element and  
188 differential equation model (Fig. 4). The power outputs from the PZT energy harvesting  
189 systems are higher than that of its PVDF counterpart, again due to higher piezoelectric  
190 coefficients of PZT. It was found that the PVDF power outputs were approximately 52% of  
191 the PZT power outputs, which corresponds to PZT having a power figure of merit, a non-  
192 dimensional figure of the piezoelectric constant squared over the dielectric constant, which is  
193 double of PVDF. The finite element models produced a higher power output than the  
194 differential equation, which was expected during comparisons of the strain profiles. The finite  
195 element models show a small increase in the power outputs with increasing train speed, while  
196 there is a relatively higher increase from the differential equations. The *201Loco* was  
197 observed to have the highest potential of power output per train passage. From the finite  
198 element PZT model, the power harvested ranged from 382 $\mu$ W at 40km/hr to 397 $\mu$ W at  
199 160km/hr, while ranging from 223 $\mu$ W to 363  $\mu$ W from the differential equations. The  
200 *Shinkansen* was observed to have the lowest estimated power outputs, ranging from 197 $\mu$ W  
201 at 40km/h4 to 203 $\mu$ W at 160km/hr from the finite element PZT model. The differential  
202 equation model ranged from 112 $\mu$ W at 40km/hr to 163 $\mu$ W at 140km/hr. Each train is

203 observed to have a signature power output which can be used to determine the identity of the  
204 train which has travelled over the bridge. This signature power output, and the subsequent  
205 potential of different trains towards energy harvesting, is consistent with existing  
206 investigations into the characterisation of different vehicles loading effect on bridges (Brady  
207 et al. 2006; O'Brien et al. 2009).

208 As shown even with a simplified differential equation model, the harvested energy for  
209 a single energy harvesting system for a single train passage is observed to be of the order of  
210  $100\mu\text{W}$ . The power requirement of an autonomous wireless sensor network in sleep mode  
211 requires on the order of 100's of nW (Magno et al. 2013) and typically requires  
212 approximately  $100\mu\text{W}$  (Torah et al 2008; Wang et al 2011) to operate in active mode. In  
213 structure health monitoring, the signal does not need to be transmitted after each passing  
214 train, but over an extended period of time. Hence, charge generated from each train can be  
215 stored and information transmitted periodically and through the highly routine nature of train  
216 networks, the time between cycles is highly predictable. Bridges which experience high  
217 levels of traffic and exhibit more dynamic behaviour would lend themselves to higher levels  
218 of harvesting. These are often the same bridges that require more attention in terms of  
219 monitoring. Consequently, a natural potential exists for the energy harvesters to be used as a  
220 monitor.

### 221 ***Double Train Passage***

222 After studying the effects of single trains on the models, the energy harvesting  
223 potential from double train passages was investigated (Fig. 5). For this, the finite element  
224 model was used exclusively and modelled with trains travelling in opposite directions. As  
225 previously found in the single passages, the PZT system produced a higher power output than  
226 the PVDF system. The highest figure of power produced was  $588\mu\text{W}$  from PZT system and  
227  $307.1\mu\text{W}$  from PVDF system for the *I.C.E.* trains, traversing the model in opposite directions

228 at a speed of 120km/hr. The *Shinkansen* again produced the lowest amount of power, ranging  
229 from 269 $\mu$ W to 285 $\mu$ W at speeds of 40 and 160km/hr respectively from the PZT harvesting  
230 system and 140 $\mu$ W to 149 $\mu$ W at speeds of 40 and 160km/hr respectively from the PVDF  
231 harvesting system.

232 As can be seen from the comparison of Fig. 4 and Fig.5, there is a considerable  
233 increase in power produced from passing trains when compared to single train passages.  
234 However, a double train passage does not result in a doubling of the power output. Instead it  
235 is dependent on the characteristics of the trains and their speed, with an increase in power  
236 output ranging 34 to 52%. This again is consistent with both theoretical and experimental  
237 investigations into the effects of vehicle loadings on bridges (O'Brien and Enright 2013;  
238 Brady and O'Brien 2006).

### 239 **Energy Harvesting – Experimental Data**

240 Full scale strain and acceleration measurements from train-bridge interaction were  
241 conducted at Skidträsk Bridge, located in Northern Sweden (Fig. 6). The bridge is a single  
242 span steel-concrete composite bridge which carries a single ballasted track, spans 36m and is  
243 6.7m in width. The rails are supported by concrete sleepers, 0.65m apart, which lie on a 0.5m  
244 layer of ballast and a 0.5m layer of sub-ballast. The ballast layers lie on a reinforced concrete  
245 slab, ranging in depth of between 0.3 and 0.4m, supported through two steel beams.

### 246 **Train Loading**

247 Two different cases have been investigated for the purposes of determining the potential  
248 of energy harvesting from real-time train-bridge interaction. The first case is a single  
249 locomotive passing over the bridge at speeds ranging from 60 to 180km/hr. The locomotive is  
250 10.4m long with two bogies, located 7.7m apart, with the two axles on each bogie a distance  
251 of 2.7m apart. The total load from the locomotive is 191.2kN. The second case considered for  
252 the purposes of this investigation is a loaded freight train, namely the *Steel Arrow*, a common

253 iron ore freight train in Sweden. The *Steel Arrow* comprises of two locomotives and twenty  
254 six wagons, with the locomotives the same as in the first case. The wagons are a total of  
255 10.4m in length, with two bogies 8.6m apart, with the bogie containing two axles 1.8m apart.  
256 The total load from each axle is 245.2kN. The train has a total length of 388m.

### 257 **Monitoring System**

258 The bridge was monitored by the Division of Structural Engineering & Bridges, KTH  
259 Royal Institute of Technology, Stockholm. Two monitoring systems, one permanent and one  
260 temporary, were installed on the bridge (Loireaux 2008). The permanent system consisted of  
261 four strain gauges measuring longitudinal strain on the main steel beams, two strain  
262 transducers measuring transverse strain on the concrete slab and three accelerometers  
263 measuring vertical bridge deck acceleration, all at varying points on the slab and steel beams.  
264 The temporary system consisted of four accelerometers installed on the sleepers and within  
265 the ballast. The speed of the passing trains was obtained from two optical laser sensors,  
266 placed a distance of 26.05m apart. The sensors output was used to determine the number of  
267 wagons of the train and the distance between two axles. This enabled the speed and length of  
268 the train to be determined through the distance between axles, bogies and wagons.

### 269 **Comparisons with Modelling**

270 Two computational models were created for comparison against the experimental data.  
271 The first is the differential equation model, which was referred to in the previous section. The  
272 second was a finite element model created using the LUSAS finite element analysis software  
273 (LUSAS 2012). A two dimensional simply supported beam model was created with five  
274 different cross-sections representing the variation in the Skidträsk Bridge. The elements used  
275 are 'BEAM' elements, which are 2 dimensional linear beam elements, at a mesh size of 0.1m.  
276 For both models, calibration was performed using actual properties and measurements of the  
277 Skidträsk Bridge. The experimental data, finite element model and differential equation

278 model all correlated well (Fig. 7). The power output from the train and locomotive passages  
279 were then evaluated for the experimental data and corresponding differential equation model.

## 280 **Results**

### 281 ***Locomotive Passages***

282 The potential power output obtained from a single locomotive passage was evaluated  
283 for speeds ranging from 61km/hr to 180km/hr (Fig. 8). Again, it was found that the PZT  
284 energy harvester generated more power when compared to its PVDF counterpart. For a single  
285 passage of the locomotive, a maximum of  $1.55\mu\text{W}$  was produced at a speed of 118km/hr  
286 from the experimental based PZT harvester, with a corresponding model value of  $1.31\mu\text{W}$ .  
287 From the same speed, the PVDF harvester produced  $0.83\mu\text{W}$  and  $0.7\mu\text{W}$  from the  
288 experimental and modelled data respectively. However, as the PVDF is less brittle than the  
289 PZT, the long-term reliability is believed to be significantly higher than PZT. Comparing the  
290 experimental power output with the finite element double track model bridge from the  
291 previous section, it can be determined that for energy harvesting, train passages are more  
292 efficient over short span bridges. While the energy harvested from a single train passage is  
293 relatively low for the locomotive passage, the energy harvested from multiple train passage  
294 can be stored to a predefined level which, when reached, is capable of powering a wireless  
295 communication device. With the highly timetabled nature of train networks, the system can  
296 be calibrated so as to act as a health monitoring tool.

### 297 **Steel Arrow Passages**

298 The estimated power outputs from single passages of the 388m long *Steel Arrow* train  
299 at varying speeds was found for speeds ranging from 65km/hr to 118km/hr (Fig. 9). The PZT  
300 harvester produced power outputs ranging from  $24.1\mu\text{W}$  to  $16.9\mu\text{W}$  at speeds of 65km/hr to  
301 118km/hr respectively from experimental data and power output of  $23.4\mu\text{W}$  and  $16.1\mu\text{W}$

302 from the models. The PVDF harvester produced  $12.8\mu\text{W}$  and  $12.4\mu\text{W}$  from the same  
303 experimental conditions and  $9\mu\text{W}$  and  $8.6\mu\text{W}$  from the models. The values are lower than the  
304 finite element modelling considered in the previous section but significantly higher than that  
305 produced by a single locomotive. Apart from the difference in stiffness characteristics of the  
306 bridge considered in this paper, the *Steel Arrow* being a freight train may also be a  
307 contributing factor as the spacing between the axles are far smaller than the passenger trains  
308 previously investigated. Again, with multiple train passages and through storage and  
309 calibration, the potential use of the energy harvesters to power small, low powered devices  
310 for the purposes of health monitoring is confirmed.

### 311 **Structural Health Monitoring Potential**

312 The use of the energy harvesting adhesive patch system as a method for the detection  
313 of damage and the structural health monitoring of bridges was subsequently investigated.  
314 With the change in stress conditions created as a result of damage to the structure (Pakrashi et  
315 al. 2010, Perry and Koh 2008), there will be a subsequent change in the levels of energy  
316 harvested from the structure. As the harvested power is related to the RMS voltage and to the  
317 accumulation of dynamic responses filtered by electromechanical coupling over the period of  
318 the train passage, the use of an energy harvesting system for health monitoring is not  
319 dependent on individual measurements over time. This is an advantage since the ratio of  
320 undamaged to damaged energy harvesting potential is less affected by localised noise and is  
321 expected to be more robust due to the natural averaging that is carried out while energy is  
322 harvested.

323 The calibration of the energy harvesting system for use in health monitoring is  
324 dependent on a number of factors. These include the power generated from a single passage  
325 over the undamaged bridge, the storage capacity of the system, the power requirements for  
326 the wireless transmitter and the number of train passages over the bridge for a given period of

327 time. Upon these parameters being determined, any damage to the bridge, be it instantaneous  
328 or gradual, would result in a change in the amount of energy harvested. This change in the  
329 energy harvesting levels can indicate the presence and position of the damage and through the  
330 factoring of this change against the undamaged levels, the magnitude of the damage can be  
331 determined, as outlined in the subsequent sections.

### 332 **Modelling of Damage**

333 The finite element model utilised in the previous sections for the determining of  
334 energy harvesting potential from train-bridge dynamics was employed for assessing the  
335 feasibility of structural health monitoring using the energy harvesting system. The *201Loco*  
336 train, travelling at 100km/hr, was chosen as an example to demonstrate how damage  
337 evolution and position can influence the energy harvested at a given device. Damage was  
338 modelled at two different locations, with varying Crack Depth Ratio's (CDR's) ranging from  
339 0.05 to 0.20, in increments of 0.05. Each 0.05 CDR increment represents an increase of  
340 40mm in the crack depth. Two crack widths were chosen, of width 400mm and 800mm, to  
341 investigate the relationship between increased width of damage and the effect on the energy  
342 harvesting system. A relatively localised damage is considered in this paper as opposed to  
343 diffused damage with larger influences on the global dynamics of the structure (Fig. 10).  
344 Consequently, successful application of SHM on this localised damage will ensure the  
345 potential of using energy harvesting for health monitoring in a wide range of damage  
346 situations.

### 347 **Damage Detection**

348 Structural health monitoring is a four step process with the detection of the presence  
349 of damage, the location of damage and the extent of damage respectively being the first three  
350 steps. The final step is the assessment of remaining service life and this is usually treated  
351 independently (Rytter 1993). The ability of the energy harvesting system to determine the  
352 presence, location and magnitude of the damage are investigated to determine whether it

353 satisfies the first three criterion of SHM. The power harvesting profile from the model with  
354 localised damage was evaluated and compared against the power harvesting profile for an  
355 undamaged model, with the undamaged situation providing a benchmark. Using a monotonic  
356 descriptor of damage detection is typically considered to be a good method for estimating the  
357 extent of the damage extent (Pakrashi et al. 2007). The influence of the damage was  
358 determined through the modelling of the energy harvesting system as an array located along  
359 the bottom beam supports of the finite element model. The locations of the harvesting system  
360 and the grid spacing can be made commensurate with resolution at which damage effects  
361 need to be identified and the consequences of damage at a certain location. Such locations or  
362 spacing may be assessed from standard static analysis. At each chosen position, the influence  
363 of damage was determined through the normalised calibration of the harvested energy against  
364 the energy harvested from the undamaged model case (Fig. 11). The damage was introduced  
365 centred about the mid-span of the central support beam, with the solid line signifying the  
366 normalised power with damage of 0.8m width and the broken line representing the  
367 normalised power with damage of 0.4m width. The region closest to the damage experiences  
368 the largest variation in the normalised power harvested and the normalised power for the  
369 damage of width 0.8m is more significant when compared to its 0.4m width damage  
370 counterpart. The effect of the damage can be detected along the length of the beam, with the  
371 proximity of the energy harvester to the location of the damage being directly related to the  
372 change in the normalised power harvested (Fig. 11a). For the 0.8m wide damage for CDR =  
373 0.20, at the location 3.9m from the edge of the damage the normalized power harvested was  
374 0.97, compared to 0.70 at the location of 0.4m. For the 0.4m wide damage, again at CDR of  
375 0.20, the normalized power was 0.98 at a location of 4.1m and 0.85 at a location 0.6m. At the  
376 location of damage, the normalized power increases dramatically (Fig. 11b). This ranged  
377 from 3.56 for damage width .8m and 2.50 for damage width 0.4m. This marked increase in

378 the normalized power can be used to identify the magnitude to which the damage has  
379 developed to in the structure, due to the monotonic nature of the curves upon the introduction  
380 of damage to the structure. The ability of the energy harvesting system to detect damage at a  
381 non-symmetrical location was also investigated. Damages, again of widths 0.4 and 0.8m with  
382 CDR ranging from 0.05 to 0.20, were introduced centralised about the quarter-span located  
383 2.65m from the support along the central support beam. The results of the quarter-span  
384 damage (Fig 12) are in keeping with that of the mid-span damage. The influence of the  
385 damage can again be detected through the reduction in the normalized power at locations  
386 situated along the length of the beam away from the position of damage (Fig. 12a), with the  
387 proximity to the damage location again being a critical factor. For damage of width 0.8m for  
388 CDR =0.20, the normalised power is 0.44 at a location .45m from the damage and for  
389 damage of width 0.4m for similar CDR, the normalised power is 0.68 at a distance of .65m.  
390 Due to the non-symmetrical location of the damage, between the support and the position of  
391 damage for both damage widths, there is an increase in the normalised power between CDR  
392 of 0.15 and 0.20. At the position of damage, there is a marked increase in the magnitude of  
393 the normalised power with increasing CDR (Fig. 12b). At the position of damage located  
394 closest to the support at a CDR of 0.20, the normalised power ranged from 48.51 for damage  
395 of width 0.8m to 37.74 for damage of width 0.4m. Again through the calibrated system, the  
396 magnitude of the damage can be determined, due to the quite monotonic nature of the  
397 normalised power harvesting curves once damage is detected. The presence, location and  
398 magnitude of the damage can be ascertained through the use of the energy harvesting system,  
399 thus satisfying the first three criteria of SHM.

#### 400 **Structural Health Monitoring – Experimental Data**

401 Experimental data from a laboratory scale experiment on damaged beam and model  
402 vehicle interaction was considered next (Pakrashi et al., 2010). This entailed a model two-

403 axle vehicle, with an axle distance of 0.11m, traversing a phenolic beam of length 0.91m.  
404 Damage was introduced in the form of an open crack located along the lower section of the  
405 beam, with CDR's of 0.167, 0.33 and 0.5. The vehicle was accelerated from a resting position  
406 by means of a string which was coiled around a motor located at the opposite side as the  
407 initial position. The response due to the bridge-vehicle interaction was recorded by means of  
408 two strain gauges, located at distances 4 and 6mm from the position of damage. The strain  
409 data was subsequently analysed and the normalised power harvesting for the varying CDR's  
410 was evaluated (Fig. 13). With increasing CDR, the normalised power increases, with  
411 proximity to the location of the damage being directly related to the magnitude, as was  
412 previously established in the finite element damage analysis.

#### 413 **Conclusions**

414 This paper presents the feasibility of using train-bridge interaction for energy  
415 harvesting and proposes a possible application in structural health monitoring. Two  
416 difference piezoelectric materials, PZT and PVDF, were compared for energy harvesting  
417 purposes. Although PZT showed a significant increase in power generated, the brittle nature  
418 of the material is a potential reliability risk. Therefore the PVDF material is believed to be the  
419 better option at this time. Five international trains were chosen to determine their potential for  
420 energy harvesting from train-bridge dynamics. A three dimensional finite element model was  
421 created and compared against differential equation based models. Full scale testing data,  
422 along with calibrated finite element and differential equation models for train-bridge  
423 interaction were used and potential power output of the energy harvesting system were  
424 determined. Piezoelectric harvesting systems were observed to be appropriate for harvesting  
425 energy to support wireless sensors with low power demand. Important trains were observed  
426 to have individual signatures of energy harvesting and potential towards harvesting for bridge  
427 structures. Multiple crossings of trains do not produce double the amount of energy as

428 compared to a single train passage. Train passages were found to produce power outputs up  
429 to  $588\mu\text{W}$  for passenger trains, namely the *I.C.E.*, and  $24.1\mu\text{W}$  for freight trains, the *Steel*  
430 *Arrow*, both from PZT based energy harvesting systems. Bridges with high dynamic  
431 responses, which are often identified as more in need of health monitoring than bridges with  
432 low dynamic responses, are more suited to energy harvesting from train passages over  
433 bridges. The use of energy harvesting systems for use in the structural health monitoring of  
434 train bridges was investigated. It was found that an array of energy harvesting systems have  
435 the potential for determining the location and the magnitude of damage throughout a bridge  
436 and compared against laboratory experiments. The extent of damage can be monotonically  
437 represented by the harvested energy.

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