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# Multi-Period OPF Model of Power Systems with HVDC Connected Intermittent Wind Power Generation

Abbas Rabiee, Alireza Soroudi

**Abstract**—This paper presents a model for a multi-period optimal power flow (MP-OPF) problem which includes offshore wind farm connected to the grid by line-commutated converter high-voltage DC (LCC-HVDC) link. The offshore wind farm is composed of doubly fed induction generators (DFIGs), and the DFIGs capability curve is considered in order to obtain a more realistic dispatch for wind farm. The uncertainties of wind power generation are also taken into account using a scenario based approach which can be adopted by system operator to obtain the optimal active and reactive power schedules for both thermal and renewable generating units. To illustrate the effectiveness of the proposed approach, it is applied on the IEEE 118-bus system. The obtained results demonstrate the capability of the proposed MP-OPF model for optimal operation of power system.

**Index Terms**—HVDC, wind power, OPF, scenario modeling, uncertainty.

## NOMENCLATURE

$t/s$	$t/s$ time interval and wind scenario index
$k$	Index of system buses
$m$	rectifier ( $m = r$ )/inverter ( $m = i$ )
$v_{in}^c$	Cut-in speed of wind turbine (m/s)
$v_{out}^c$	Cut-out speed of wind turbine (m/s)
$v_{rated}$	Rated speed of wind turbine (m/s)
$UR_{G_k}$	Ramp up limit of power generation of $k$ -th thermal unit
$DR_{G_k}$	Ramp down limit of power generation of $k$ -th thermal unit
$\lambda(s, t)$	Electricity price in scenario $s$ and time $t$ (\$/MW)
$\pi_s$	Probability of scenario $s$
$Pp(s, t)$	Power purchased from pool market in time $t$ and scenario $s$
$wp_s$	Percent of available wind generation capacity in scenario $s$
$P_{st}/Q_{st}$	Active/reactive power of DFIG's stator
$V_{st}/I_{st}$	Stator voltage/current of DFIG
$X_m/X_{st}$	DFIG's mutual/stator reactance
$sl$	DFIG's rotor slip
$\delta$	DFIG's load angle
$I_{rt}$	DFIG's rotor current
$P_{rt}/Q_{rt}$	Active/reactive power of DFIG's rotor
$P_{wg}/Q_{wg}$	Active/reactive power Output of DFIG
$P_{wg}^r$	Rated active power Output of DFIG
$\alpha_m$	Ignition angle
$V_{d0,m}$	Ideal no-load voltage at the terminals
$V_{d,m}$	DC magnitudes of voltages at the terminals
$B_m$	Number of series-connected bridges in a terminal
$T_m$	Tap ratio of HVDC's transformer

$V_m$	effective voltage magnitudes at the AC terminals of HVDC
$R_{c,m}$	Commutation resistances
$I_d$	DC current carried by the HVDC link
$B_{sh,m}$	Shunt admittance of Passive filters at the AC side of HVDC terminals
$Q_{sh,m}$	Reactive power compensation at the AC side of HVDC terminals
$R_{L,d}$	Resistance of HVDC line
$\varphi_m$	Angle difference between the fundamental line current and line-to-neutral AC voltage
$P_{d,m}$	Active power flowing through HVDC link
$Q_m$	Reactive power flowing into HVDC link
	AC network's variables and parameters:
$P_{G_k}/Q_{G_k}$	Active/reactive power generation by thermal unit located in bus $k$
$P_{L_k}/Q_{L_k}$	Active/reactive load in bus $k$
$V_k/\theta_k$	Voltage magnitude/angle in bus $k$
$S_\ell$	Flow of $\ell$ -th transmission line
$Y_{kj}/\gamma_{kj}$	Magnitude/angle of $kj$ -th element of admittance matrix

## I. INTRODUCTION

### A. Motivation and Approach

UTILIZATION of wind power generation technology is taking substantial attention around the world due to the economical and environmental concerns [1]. The problem of uncertainty modeling of wind generation facilities is still an important issue [2]. Hence, the appropriate modeling of wind power generation in optimal power flow (OPF) formulation is essential. The ultimate goal of the system operator is operating the system in a way that the total operating cost is minimized for a given operating horizon while satisfying a set of technical constraints. Such an optimization problem is called multi-period optimal power flow (MP-OPF) [3]. Generally, the objective of a MP-OPF problem is to find the steady state operation point of power system which minimizes generation cost or maximizes the social welfare and loadability, while satisfying a set of technical constraints such as power flow equations, limits on generators' real and reactive powers, line flow limits and output of various compensating devices [4], [5].

In many countries, the best locations for onshore wind farms are already developed, and the utilities are turning to offshore sites. The main reason of this attraction is the availability of enormous wind resources. The lack of obstacles such as hills, and generally smooth surface of the sea, also make the wind generation more reliable. The offshore wind farm is generally located far away from the onshore grid. If the distance is long or if the offshore wind farm is connected to a weak AC onshore grid, a high-voltage DC

(HVDC) transmission system may be a more suitable choice than the conventional high-voltage AC transmission [6]. Two types of HVDC transmission topologies, i.e., HVDC with voltage source converter (VSC-HVDC) using insulated gate bipolar transistors (IGBTs) and line-commutated converter HVDC (LCC-HVDC) are used nowadays for offshore wind farm connectivity [7], [8].

### B. Literature Review

Different OPF models have been proposed in the literature to consider the impacts of wind power generation. The objective functions cover a vast range of items such as :

- opportunity cost of wind power shortage & surplus [9]
- cost of environmental benefit loss [9]
- expected penalty cost for not using all available wind power [10]
- expected cost of calling up power reserves because of wind power shortage [10]
- risk due to expected energy not supplied (EENS) and total operating costs [11]
- location marginal prices, and reserve costs [11]
- minimizing losses within the wind farm and the HVDC transmission system and maximizing production output [12]
- voltage regulation of the electrical grid to which farms are connected [13]

The proposed approaches for handling the uncertainty of wind power generation are summarized as follows: Monte Carlo [9], triangular approximate distribution (TAD) [11], scenario based modeling [14], [15].

### C. Contributions

In this paper, a comprehensive model for MP-OPF is proposed, by including the uncertain wind power generation. The offshore wind farms are considered to be of doubly fed induction generator (DFIG) type. These farms are connected to the AC transmission system by LCC-HVDC links. Due to the importance of considering reactive power requirements of converters at both sides of the LCC-HVDC connection, capability curves of wind farm's DFIGs are also modeled. Considering the capability curves for DFIGs makes the generation schedule more realistic.

### D. Paper Organization

This paper is set out as follows: Section II presents problem formulation. Simulation results are presented in Section III and finally, Section IV summarizes the findings of this work.

## II. PROBLEM FORMULATION

Load flow equations of AC/DC networks, HVDC links steady state model and characteristics of wind power generation are formulated in this section. The assumptions, decision variables, constraints and objective function of the proposed MP-OPF are described as follows:

### A. Decision Variables

The decision variables of the problem include: hourly generation schedule and terminal voltage of thermal units, tap settings of on-load tap changers and HVDC link transformers. These variables are determined based on a set of wind generation

scenarios and remain the same for each scenario. These types of variables are called 'here and now' variables. On the other hand, there exist another set of variables which change with the scenarios like voltage of PQ buses, transmitted power by HVDC link and etc. These types of variables are called 'wait and see' variables [16].

### B. Capability Curve of DFIGs

1) *Stator current limit*: this limit models the stator heating due to the stator winding Joule losses. By considering all quantities in per-unit (pu), the relation between stator voltage, current and active/reactive power outputs can be expressed as follows [12]:

$$P_{st}^2 + Q_{st}^2 = (V_{st}I_{st})^2 \quad (1)$$

2) *Rotor current limit*: This limit considers the rotor heating due to the rotor winding Joule losses. In pu, the equation of active and reactive power output of DFIG's stator is as follows [17]:

$$P_{st} = \frac{X_m}{X_{st}} V_{st} I_{rt} \sin(\delta) \quad (2)$$

$$Q_{st} = \frac{X_m}{X_{st}} V_{st} I_{rt} \cos(\delta) - \frac{V_{st}^2}{X_{st}} \quad (3)$$

$$P_{st}^2 + \left(Q_{st} + \frac{V_{st}^2}{X_{st}}\right)^2 = \left(\frac{X_m}{X_{st}} V_{st} I_{rt}\right)^2 \quad (4)$$

3) *Steady state stability limit*: The steady-state stability limit shows the maximum reactive power absorption by the DFIG, which is obtained as follows:

$$Q_{st} = -\frac{V_{st}^2}{X_{st}} \quad (5)$$

Equation (5) gives a vertical line at  $[-\frac{V_{st}^2}{X_{st}}, 0]$ , in P-Q plane. It is noteworthy that  $\frac{V_{st}^2}{X_{st}}$  is the no-load reactive power absorption, which means that the DFIG becomes unstable when the reactive power consumption is greater than the no-load reactive power [12].

4) *Total Capability limit* ( $sl_{\min} \leq sl \leq 0$ ): The rotor active-power generation, neglecting stator and rotor resistance, can be expressed as follows:

$$P_{rt} = -sl * P_{st} \quad (6)$$

The grid-side inverter of the DFIG is usually operating with a unity power factor [12]. Hence, the injected power from the rotor is zero, and total reactive power output of DFIG is as follows:

$$Q_{rt} = 0 \quad (7)$$

The DFIG's total active and reactive power generations are obtained by adding rotor active/reactive powers to the stator active/reactive powers, as follows:

$$P_{wg} = P_{st} + P_{rt} = (1 - sl)P_{st} \quad (8)$$

$$Q_{ws} = Q_{st} + Q_{rt} = Q_{st} \quad (9)$$

By defining:

$$A = I_{st,\max}; B = \frac{1}{(1 - sl_{\min})^2}; C = \frac{X_m}{X_{st}} I_{rt,\max}$$

The maximum/minimum limits of reactive power output of DFIG are expressed as follows:

$$Q_{g,\max}^{(1)} = +\sqrt{(AV_{st})^2 - BP_{wg}^2} \quad (10)$$

$$Q_{g,\max}^{(2)} = +\sqrt{(CV_{st})^2 - BP_{wg}^2} - \frac{V_{st}^2}{X_{st}} \quad (11)$$

$$Q_{g,\max} = \min(Q_{g,\max}^{(1)}, Q_{g,\max}^{(2)}) \quad (12)$$

$$Q_{g,\min}^{(1)} = -\frac{V_{st}^2}{X_{st}} \quad (13)$$

$$Q_{g,\min}^{(2)} = -\sqrt{(AV_{st})^2 - BP_{wg}^2} \quad (14)$$

$$Q_{g,\min} = \max(Q_{g,\min}^{(1)}, Q_{g,\min}^{(2)}) \quad (15)$$

##### 5) Wind-Turbine maximum/minimum active power output limit:

The restrictions related to the maximum active power available at wind turbine, are expressed as follows:

$$0 \leq P_{wg} \leq wp_s * P_{wg}^r \quad (16)$$

The capability curve of the DFIG determines the feasible operation regime in P-Q plane [17] as shown in Fig.1. From this figure, the feasible operating area in P-Q plain, is the area specified by  $(z_1, z_2, z_3, z_4, z_5, z_6)$  coordinates.

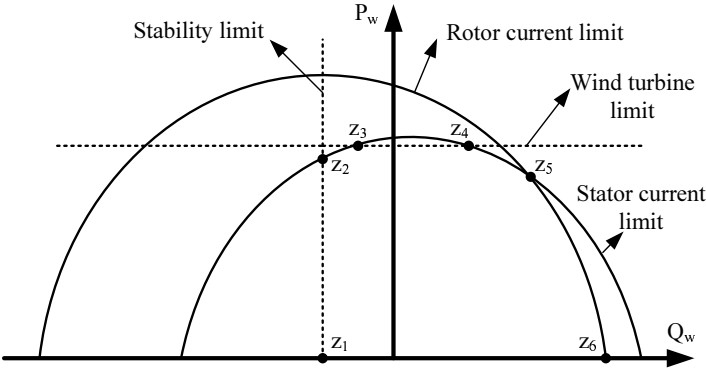


Fig. 1. Capability curve of DFIG

### C. HVDC Modeling

Load flow equations of the LCC-HVDC system are as follows. The schematic of the LCC-HVDC link is depicted in Fig. 2.

For  $m = r$ , i (r: Rectifier, i: Inverter):

$$V_{d0,m} = \frac{3\sqrt{2}}{\pi} B_m T_m V_m \quad (17)$$

$$V_{d,m} = V_{d0,m} \cos(\alpha_m) - B_m R_{c,m} I_d \quad (18)$$

$$I_d = \frac{V_{d,r} - V_{d,i}}{R_{L,d}} \quad (19)$$

$$\cos(\varphi_m) = \frac{V_{d,m}}{V_{d0,m}} \quad (20)$$

$$P_{d,m} = V_{d,m} I_d \quad (21)$$

$$Q_m = P_{d,m} \tan(\varphi_m) \quad (22)$$

### D. Uncertainty Modeling of Wind Power Generation

In this paper, a scenario based model is used to describe the wind power generation [18]. It is assumed that the probability density function of wind speed as well as the characteristic

curve of wind turbine is available. Using these data and scenario generation technique (described in Appendix B) the wind power generation is described and modeled in the proposed MP-OPF model.

### E. Load Flow Equations of AC Network

The AC load flow equations for  $k$ -th bus, is as follows:

$$P_{G_k}(t) - P_{L_k}(t) = P_k(s, t) \quad (23)$$

$$Q_{G_k}(s, t) - Q_{L_k}(t) = Q_k(s, t) \quad (24)$$

where,  $P_k(s, t)$  and  $Q_k(s, t)$  are injected active and reactive powers, respectively, which are calculated as follows:

$$P_k(s, t) = \quad (25)$$

$$\sum_{j=1}^{NB} V_k(s, t) V_j(s, t) Y_{kj} \cos(\theta_k(s, t) - \theta_j(s, t) - \gamma_{kj})$$

$$Q_k(s, t) = \quad (26)$$

$$\sum_{j=1}^{NB} V_k(s, t) V_j(s, t) Y_{kj} \sin(\theta_k(s, t) - \theta_j(s, t) - \gamma_{kj})$$

The magnitude of voltage in each bus  $k$  should remain between the safe operating limits during each scenario  $s$  and time  $t$ :

$$V_k^{min} \leq V_k(s, t) \leq V_k^{max} \quad (27)$$

Also, the flow of transmission lines must be below their corresponding limits:

$$|S_\ell(s, t)| \leq S_\ell^{max} \quad (28)$$

### F. Load Flow Equations at the Interface of AC/DC Networks

According to Fig. 2, at the inverter side of the HVDC connection (i.e. for  $k = i$ ), the power balance equations of AC/DC networks are as follows:

$$P_i(s, t) = P_{G_i}(t) + P_{d,i}(s, t) - P_{L_i}(t) \quad (29)$$

$$Q_i(s, t) = \quad (30)$$

$$Q_{G_i}(t) + B_{sh,i} V_i^2(s, t) + Q_{sh,i}(s, t) - Q_{d,i}(s, t) - Q_{L_i}(t)$$

Similarly, for the rectifier side (i.e. for  $k = r$ ), by neglecting the active power losses of the transformers connecting the WF to HVDC rectifier terminal, the power balance equations of AC/DC networks are as follows:

$$P_{wg}(s, t) = P_{d,r}(s, t) \quad (31)$$

$$Q_{wg}^{HV}(s, t) + B_{sh,r} V_r^2(s, t) + Q_{sh,r}(s, t) = Q_{d,r}(s, t) \quad (32)$$

where,  $Q_{wg}^{HV}(s, t)$  is total reactive power injected from the HV side of transformers connecting the WF to the HVDC link, in scenario  $s$  and time  $t$ . It is worth to note that passive filters are also connected to the HVDC rectifier and inverter terminals, which are represented by constant shunt admittance in (30) and (32).

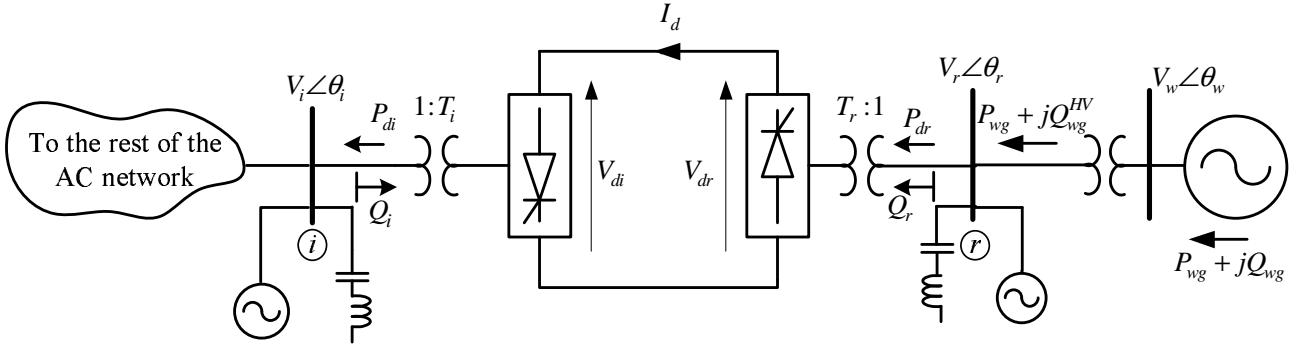


Fig. 2. One-line diagram of wind farm connection using LLC-HVDC link

### G. Thermal Generation Constraints

The following constraints are considered in order to model the cost and technical limits of thermal generation units [19]:

- 1) Total production cost of thermal units: the production cost of thermal units is defined as:

$$F_{k,t}(P_{G_k}(t)) = a_k P_{G_k}^2(t) + b_k P_{G_k}(t) + c_k \quad (33)$$

where  $a_k$ ,  $b_k$  and  $c_k$  are the fuel cost coefficients of the  $k$ -th generation unit.

- 2) Generation limits of thermal units:

$$P_{G_k}^{min} \leq P_{G_k}(t) \leq P_{G_k}^{max} \quad (34)$$

$$Q_{G_k}^{min} \leq Q_{G_k}(t) \leq Q_{G_k}^{max} \quad (35)$$

where  $P_{G_k}^{max/min}$  and  $Q_{G_k}^{max/min}$  are the maximum/minimum limits of active/reactive power outputs in  $k$ -th thermal unit.

- 3) Ramp up and ramp down constraints: the output power change rate of the thermal unit should be below the pre-specified limits called ramp rates. This is to avoid damaging the boiler and combustion equipments. These limits are stated as follows:

$$P_{G_k}(t) \geq P_{G_k}(t-1) - DR_{G_k} \quad (36)$$

$$P_{G_k}(t) \leq P_{G_k}(t-1) + UR_{G_k} \quad (37)$$

where  $UR_{G_k}$  and  $DR_{G_k}$  are the ramp up/down limits of the  $k$ -th thermal unit (MW/h).

### H. Objective function

The objective function of MP-OPF to be minimized is defined as the total cost paid by the retailer and is calculated as follows:

$$TC = \sum_{s,t} (\pi_s Pp(s,t) \lambda(s,t)) + \sum_{k,t} F_{k,t}(P_{G_k}(t)) \quad (38)$$

where  $Pp(s,t)$  is the purchased power from the pool market in time  $t$  and scenario  $s$ .

## III. SIMULATION RESULTS

The proposed probabilistic model for the MP-OPF problem is examined on the IEEE 118-bus test system. This system consists of 54 generator buses, and 186 transmission lines. The data of generating units along with the voltage limits and transmission lines flow limits are given in [20]. The purchased power from pool market is injected to the network through slack bus which is  $B_{69}$  in this network. Also, electricity price in scenario  $s$  and time

$t$ , i.e.  $\lambda(s,t)$ , is assumed to be even during the operating horizon and equal to 8 \$/h.

In this study, two wind farms (WFs) are considered. Each WF consists of 500 DFIG-based wind turbine. The characteristics of wind turbine are given in Table I. Hence, the total capacity of each WF is 1000 MW which is connected to the system via a 24-pulse LLC-HVDC link. HVDC links are bipolar with the rating of 1000 MW, and  $\pm 250$  kV. The data of these DC links are derived from [21], and are given in Table VI. As it is shown in Fig. 6, WF-1 and WF-2 are connected to buses  $B_{10}$  and  $B_{80}$ , respectively.

For the sake of brevity, three load levels ( $T_{1 \rightarrow 3}$ ) are considered for each day as 90%, 100% and 80% of the peak value. This multi-period load curve is depicted in Fig.3. Also, it is assumed

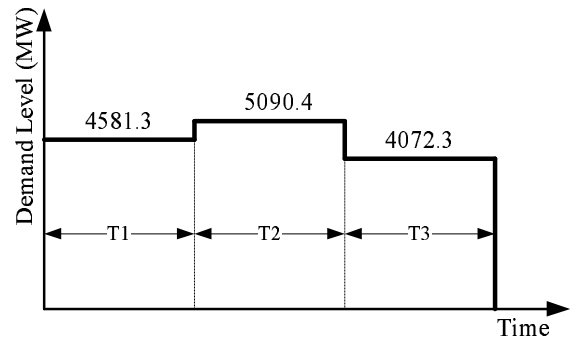


Fig. 3. Demand level values in different time intervals

that the total load of each period is distributed based on the initial load share of each bus, as given in [20].

Using the technique described in Appendix B, 12 scenarios are determined for each WF which are given in Table IV. The proposed algorithm is implemented in General Algebraic Modeling System (GAMS) [22] environment and solved by CONOPT solver [23].

Optimal active power generation schedules and voltage magnitude of generation buses, for all intervals are given in Figs. 4, 5, respectively. As mentioned earlier, these variables are 'here and now' control variables and the obtained optimal schedules for these variables are the same for all scenarios. The total cost of thermal generation units is equal to 161704.554 \$, whereas the cost paid for power procurement from pool market is equal to 4242.288 \$. The tap settings of transformers at both sides of the HVDC links, which are also 'here and now' control variables, are given in Table II, for all time intervals.

Table III gives the optimal schedule of HVDC links for all



TABLE I  
THE TECHNICAL CHARACTERISTICS OF WIND TURBINES

$v_{in}^c$ (m/s)	$v_{rated}$ (m/s)	$v_{out}^c$ (m/s)	$X_m$ (pu)	$X_{st}$ (pu)	$sl_{min}$	$I_{rt,max}$ (pu)	$I_{st,max}$ (pu)	$P_{wg}^r$ (MW)
4	14	25	2.7891	2.8421	-0.3000	1.3893	1.0500	2.0000

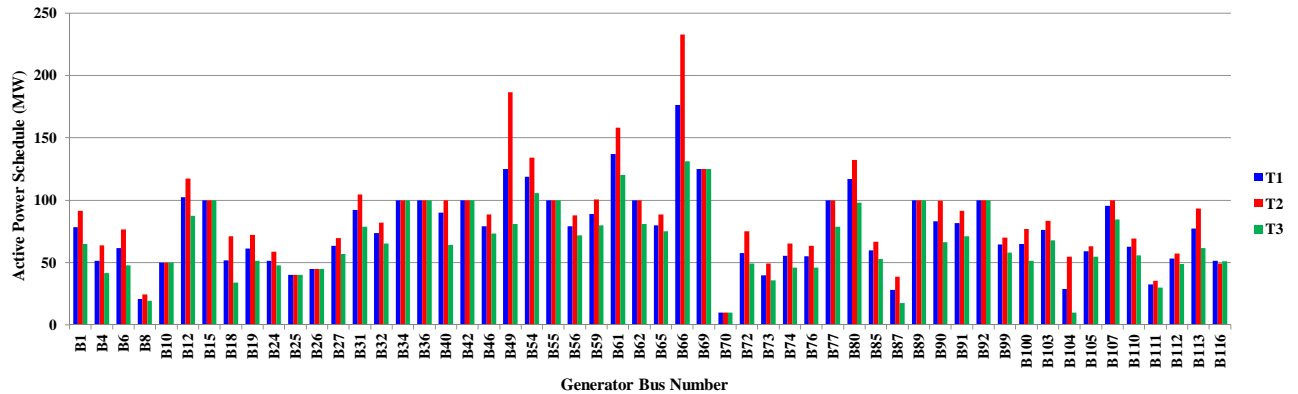


Fig. 4. Active power schedule of thermal generation units

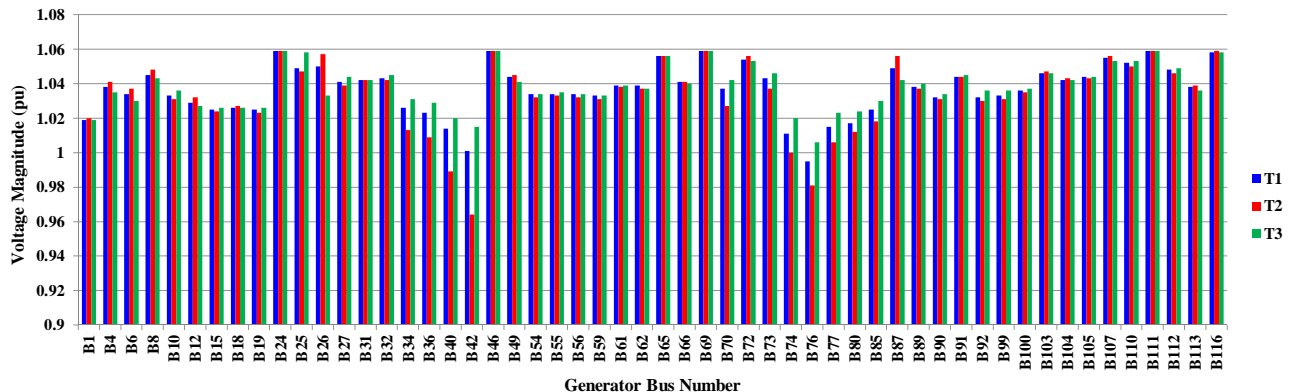


Fig. 5. Optimal voltage magnitude generation buses

scenarios in the studied horizon. for the sake of brevity, only the schedules of scenarios  $s_1 - s_6$  are given in this table. It is observed from this table that  $HVDC_1$  is loaded lightly, in comparison to  $HVDC_2$ . This is due to the capacity limit of the transmission line  $L_9$ , (between buses  $B_{10}$  and  $B_9$ ), which connects bus  $B_{10}$  to the AC network. But, for  $HVDC_2$ , bus  $B_{80}$  is connected to the system by several transmission lines (i.e. the lines  $L_{123}$ ,  $L_{124}$ ,  $L_{125}$ ,  $L_{127}$ ,  $L_{148}$ ,  $L_{151}$ ,  $L_{152}$  and  $L_{153}$ ), and hence, sufficient capacity is available for transmission of generated power of WF-2. Also, active and reactive power generation of WF-1 and WF-2 for all wind scenarios in the studied horizon, are provided in Table V.

TABLE II  
THE TAP SETTINGS OF HVDC LINKS

Link#	Time interval	Inverter	Rectifier
$HVDC_1$	$T_1$	0.450	0.456
	$T_2$	0.451	0.476
	$T_3$	0.449	0.476
$HVDC_2$	$T_1$	0.460	0.493
	$T_2$	0.462	0.489
	$T_3$	0.456	0.475

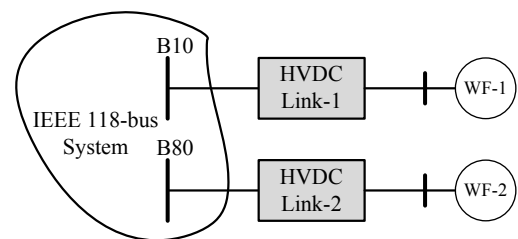


Fig. 6. The schematic of the system under study

#### IV. CONCLUSION

This paper presents a comprehensive multi-period optimal power flow (MP-OPF) model which describes a power system with uncertain wind power injections through LCC-HVDC links. The objective function of this MP-OPF is defined as minimizing the operating cost of the system in the presence of intermittent renewable energy resources like wind farms (WFs). Scenario based approach is utilized to model the uncertainty of wind power generation. One of the features of the proposed MP-OPF is to schedule both ‘here and now’ and ‘wait and see’ control

TABLE III  
THE SCHEDULES OF HVDC LINK VARIABLES

			$\varphi_r$ (Radian)	$\varphi_i$ (Radian)	$\alpha_r$ (Radian)	$\alpha_i$ (Radian)	$V_{d,r}$ (kV)	$V_{d,i}$ (kV)	$P_{d,r}$ (MW)	$P_{d,i}$ (MW)	$Q_{d,r}$ (MVar)	$Q_{d,i}$ (MVar)	$I_d$ (kA)	$V_r$ (kV)	$V_i$ (kV)	
HVDC <sub>1</sub>	s <sub>1</sub>	T <sub>1</sub>	0.35	0.09	0.35	0.09	550.00	549.81	5.23	5.23	1.92	0.48	0.01	233.20	227.13	
	s <sub>1</sub>	T <sub>2</sub>	0.17	0.18	0.08	0.09	550.00	544.65	147.02	145.59	25.48	25.74	0.27	216.98	227.06	
	s <sub>1</sub>	T <sub>3</sub>	0.18	0.18	0.08	0.09	550.00	544.34	155.56	153.96	27.58	27.88	0.28	217.28	228.08	
	s <sub>2</sub>	T <sub>1</sub>	0.35	0.35	0.35	0.35	518.62	518.41	5.23	5.23	1.92	1.92	0.01	219.90	227.13	
	s <sub>2</sub>	T <sub>2</sub>	0.17	0.18	0.08	0.09	550.00	544.65	147.02	145.59	25.48	25.74	0.27	216.98	227.06	
	s <sub>2</sub>	T <sub>3</sub>	0.35	0.35	0.35	0.35	518.60	518.35	6.70	6.70	2.46	2.46	0.01	214.88	227.64	
	s <sub>3</sub>	T <sub>1</sub>	0.34	0.18	0.30	0.09	550.00	544.44	152.81	151.27	54.07	27.19	0.28	232.27	227.56	
	s <sub>3</sub>	T <sub>2</sub>	0.35	0.35	0.35	0.35	518.66	518.66	0.00	0.00	0.00	0.00	0.00	214.62	226.66	
	s <sub>3</sub>	T <sub>3</sub>	0.35	0.09	0.35	0.09	550.00	549.76	6.70	6.70	2.46	0.62	0.01	227.87	227.64	
	s <sub>4</sub>	T <sub>1</sub>	0.17	0.18	0.08	0.09	550.00	544.44	152.81	151.27	26.90	27.19	0.28	232.34	227.56	
	s <sub>4</sub>	T <sub>2</sub>	0.17	0.18	0.08	0.09	550.00	544.65	147.02	145.59	25.48	25.74	0.27	216.98	227.06	
	s <sub>4</sub>	T <sub>3</sub>	0.18	0.18	0.08	0.09	550.00	544.34	155.56	153.96	27.58	27.88	0.28	217.28	228.08	
	s <sub>5</sub>	T <sub>1</sub>	0.09	0.09	0.08	0.09	550.00	549.81	5.23	5.23	0.45	0.48	0.01	219.77	227.13	
	s <sub>5</sub>	T <sub>2</sub>	0.17	0.18	0.08	0.09	550.00	544.65	147.02	145.59	25.48	25.74	0.27	216.98	227.06	
	s <sub>5</sub>	T <sub>3</sub>	0.38	0.18	0.35	0.09	550.00	544.34	155.56	153.96	62.49	27.88	0.28	230.56	228.08	
	s <sub>6</sub>	T <sub>1</sub>	0.18	0.39	0.08	0.35	518.45	512.55	153.01	151.27	28.26	61.40	0.30	209.90	227.56	
	s <sub>6</sub>	T <sub>2</sub>	0.17	0.18	0.08	0.09	550.00	544.65	147.02	145.59	25.48	25.74	0.27	216.98	227.06	
	s <sub>6</sub>	T <sub>3</sub>	0.18	0.18	0.08	0.09	550.00	544.34	155.56	153.96	27.58	27.88	0.28	217.28	228.08	
	HVDC <sub>2</sub>	s <sub>1</sub>	T <sub>1</sub>	0.45	0.30	0.35	0.08	549.63	530.35	529.83	511.25	254.46	158.53	0.96	228.83	223.63
		s <sub>1</sub>	T <sub>2</sub>	0.26	0.26	0.08	0.10	550.00	536.25	378.06	368.61	98.37	99.34	0.69	215.05	222.37
s <sub>1</sub>		T <sub>3</sub>	0.25	0.26	0.08	0.08	549.75	536.32	369.20	360.18	95.07	93.81	0.67	221.26	225.05	
s <sub>2</sub>		T <sub>1</sub>	0.30	0.30	0.08	0.08	549.63	530.35	529.83	511.25	161.74	158.53	0.96	215.67	223.63	
s <sub>2</sub>		T <sub>2</sub>	0.26	0.26	0.08	0.10	550.00	536.25	378.06	368.61	98.37	99.34	0.69	215.05	222.37	
s <sub>2</sub>		T <sub>3</sub>	0.30	0.30	0.08	0.08	548.58	529.34	527.86	509.35	160.93	157.95	0.96	223.53	225.05	
s <sub>3</sub>		T <sub>1</sub>	0.25	0.26	0.08	0.09	550.00	536.46	372.40	363.23	96.23	96.45	0.68	213.19	223.54	
s <sub>3</sub>		T <sub>2</sub>	0.43	0.30	0.32	0.08	549.72	530.27	534.69	515.77	243.41	160.63	0.97	228.56	222.37	
s <sub>3</sub>		T <sub>3</sub>	0.30	0.30	0.08	0.08	548.58	529.34	527.86	509.35	160.93	157.95	0.96	223.53	225.05	
s <sub>4</sub>		T <sub>1</sub>	0.42	0.26	0.35	0.09	550.00	536.46	372.40	363.23	167.04	96.45	0.68	226.22	223.54	
s <sub>4</sub>		T <sub>2</sub>	0.32	0.43	0.19	0.35	518.79	504.17	379.30	368.61	125.62	170.32	0.73	206.80	222.37	
s <sub>4</sub>		T <sub>3</sub>	0.25	0.26	0.08	0.08	549.75	536.32	369.20	360.18	95.07	93.81	0.67	221.26	225.05	
s <sub>5</sub>		T <sub>1</sub>	0.30	0.30	0.08	0.08	549.63	530.35	529.83	511.25	161.56	158.53	0.96	215.65	223.63	
s <sub>5</sub>		T <sub>2</sub>	0.41	0.27	0.33	0.11	549.25	535.49	378.08	368.61	163.15	101.42	0.69	226.37	222.37	
s <sub>5</sub>		T <sub>3</sub>	0.25	0.26	0.08	0.08	549.75	536.32	369.20	360.18	95.07	93.81	0.67	221.26	225.05	
s <sub>6</sub>		T <sub>1</sub>	0.42	0.26	0.35	0.09	550.00	536.46	372.40	363.23	167.04	96.45	0.68	226.22	223.54	
s <sub>6</sub>		T <sub>2</sub>	0.26	0.26	0.08	0.10	550.00	536.25	378.06	368.61	98.37	99.34	0.69	215.05	222.37	
s <sub>6</sub>		T <sub>3</sub>	0.25	0.26	0.08	0.08	549.75	536.32	369.20	360.18	95.07	93.81	0.67	221.26	225.05	

TABLE IV  
THE WIND POWER GENERATION SCENARIOS AND THEIR ASSOCIATED PROBABILITIES

	$wp_s$	$\pi_s$
s <sub>1</sub>	100.00	0.07843
s <sub>2</sub>	94.97	0.02500
s <sub>3</sub>	84.97	0.03265
s <sub>4</sub>	74.98	0.04509
s <sub>5</sub>	64.98	0.05011
s <sub>6</sub>	54.98	0.07728
s <sub>7</sub>	44.99	0.09121
s <sub>8</sub>	34.99	0.11222
s <sub>9</sub>	19.99	0.10365
s <sub>10</sub>	15.00	0.11233
s <sub>11</sub>	5.00	0.06610
s <sub>12</sub>	0.00	0.20594

variables for the given time horizon.

The proposed approach is implemented on the IEEE 118-bus system to demonstrate its applicability. Two offshore WFs are considered, which are connected to the onshore AC power network through LLC-HVDC links. It is observed from the numerical results that availability of transmission network capacity at the interface of AC/DC networks is a key factor affecting the utilization WF's power generation ability.

APPENDIX A  
DATA OF HVDC CONNECTIONS

The data of LLC-HVDC links are given in this appendix, which are derived from [21].

APPENDIX B  
WIND GENERATION MODELING [24]

It is assumed that the probability density function (PDF) of wind speed is available in the region under study, then

$$PDF(v) = \left(\frac{v}{c^2}\right) \exp\left[-\left(\frac{v}{\sqrt{2}c}\right)^2\right] \quad (39)$$

The probability of falling into scenario  $s$  and the corresponding wind speed  $v_s$  is calculated as follows:

$$\begin{aligned} \pi_s &= \int_{v_{1,s}}^{v_{2,s}} \left(\frac{v}{c^2}\right) \exp\left[-\left(\frac{v}{\sqrt{2}c}\right)^2\right] dv \quad (40) \\ &= \exp\left[-\left(\frac{v_{1,s}}{\sqrt{2}c}\right)^2\right] - \exp\left[-\left(\frac{v_{2,s}}{\sqrt{2}c}\right)^2\right] \\ v_s &= \frac{v_{2,s} + v_{1,s}}{2} \end{aligned}$$

where  $v_{1,s}, v_{2,s}$  are the starting and ending points of the wind speed's interval defined in scenario  $s$ , respectively.

The generated power of the wind turbine is determined using its characteristics as follows:

$$P_{wg}(v_s) = \begin{cases} 0 & \text{if } v_s \leq v_{in}^c \text{ or } v_s \geq v_{out}^c \\ \frac{v_s - v_{in}^c}{v_{rated} - v_{in}^c} P_{wg}^r & \text{if } v_{in}^c \leq v_s \leq v_{rated} \\ P_{wg}^r & \text{else} \end{cases} \quad (41)$$

Where,  $P_{wg}^r$  is the rated power of wind turbine. The generated power of wind turbine in scenario  $s$  is calculated using the obtained  $v_s$  and (41).

TABLE V  
THE PROBABILISTIC WIND POWER OUTPUTS OF WIND FARMS

Scenario#	Period#	WF-1		WF-2	
		Pw (MW)	Qw (MVar)	Pw (MW)	Qw (MVar)
s <sub>1</sub>	T <sub>1</sub>	5.23	-6.19	529.83	37.37
s <sub>1</sub>	T <sub>2</sub>	147.02	55.03	378.06	27.44
s <sub>1</sub>	T <sub>3</sub>	155.56	20.02	369.20	98.50
s <sub>2</sub>	T <sub>1</sub>	5.23	-4.92	529.83	29.88
s <sub>2</sub>	T <sub>2</sub>	147.02	68.67	378.06	41.67
s <sub>2</sub>	T <sub>3</sub>	6.70	0.72	527.86	247.77
s <sub>3</sub>	T <sub>1</sub>	152.81	31.36	372.40	160.06
s <sub>3</sub>	T <sub>2</sub>	0.00	40.74	534.69	94.95
s <sub>3</sub>	T <sub>3</sub>	6.70	41.98	527.86	43.95
s <sub>4</sub>	T <sub>1</sub>	152.81	70.76	372.40	10.00
s <sub>4</sub>	T <sub>2</sub>	147.02	-5.91	379.30	195.01
s <sub>4</sub>	T <sub>3</sub>	155.56	43.74	369.20	6.33
s <sub>5</sub>	T <sub>1</sub>	5.23	-5.16	529.83	249.74
s <sub>5</sub>	T <sub>2</sub>	147.02	49.88	378.08	229.38
s <sub>5</sub>	T <sub>3</sub>	155.56	86.32	369.20	131.34
s <sub>6</sub>	T <sub>1</sub>	153.01	21.01	372.40	233.69
s <sub>6</sub>	T <sub>2</sub>	147.02	-5.80	378.06	84.98
s <sub>6</sub>	T <sub>3</sub>	155.56	-2.04	369.20	90.80
s <sub>7</sub>	T <sub>1</sub>	4.47	-6.01	449.86	27.44
s <sub>7</sub>	T <sub>2</sub>	147.02	45.10	378.06	10.68
s <sub>7</sub>	T <sub>3</sub>	155.56	72.25	369.20	108.41
s <sub>8</sub>	T <sub>1</sub>	153.83	48.40	349.89	100.43
s <sub>8</sub>	T <sub>2</sub>	148.72	22.88	349.89	22.24
s <sub>8</sub>	T <sub>3</sub>	155.91	28.87	349.89	14.13
s <sub>9</sub>	T <sub>1</sub>	154.70	-5.51	199.94	72.42
s <sub>9</sub>	T <sub>2</sub>	150.55	-5.78	199.94	39.12
s <sub>9</sub>	T <sub>3</sub>	154.10	-1.96	199.94	-24.12
s <sub>10</sub>	T <sub>1</sub>	149.95	14.31	149.95	22.36
s <sub>10</sub>	T <sub>2</sub>	149.95	-2.79	149.95	21.88
s <sub>10</sub>	T <sub>3</sub>	149.95	-6.02	149.95	22.86
s <sub>11</sub>	T <sub>1</sub>	49.98	-3.41	49.98	-0.57
s <sub>11</sub>	T <sub>2</sub>	49.98	-242.61	49.98	0.33
s <sub>11</sub>	T <sub>3</sub>	49.98	-0.29	49.98	-0.06
s <sub>12</sub>	T <sub>1</sub>	0.00	0.00	0.00	0.00
s <sub>12</sub>	T <sub>2</sub>	0.00	0.00	0.00	0.00
s <sub>12</sub>	T <sub>3</sub>	0.00	0.00	0.00	0.00

TABLE VI  
THE DATA OF STUDIED HVDC LINKS

Parameter	Value	
No. of converters at each side of the HVDC link	2	
No. of 6-pulse bridges at each converter	2	
$R_{L,d}$ (per line)	10Ω	
$R_{cr}$ (per bridge)	6Ω	
$R_{ci}$ (per bridge)	6Ω	
$B_r (= B_i)$	4	
Rated voltage of line to line $V_r$ and $V_i$	220 kV	
$m = r, i$	min	max
$\alpha_m$ (radian)	0.08	0.35
$\varphi_m$ (radian)	0	$\pi/2$
$V_{d,m}$ (kV)	450	550
$P_{d,m}$ (MW)	0	1000
$T_m$	0.3	0.7

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